

# Performance Modeling: Queueing Networks

Software Design  
2DV608

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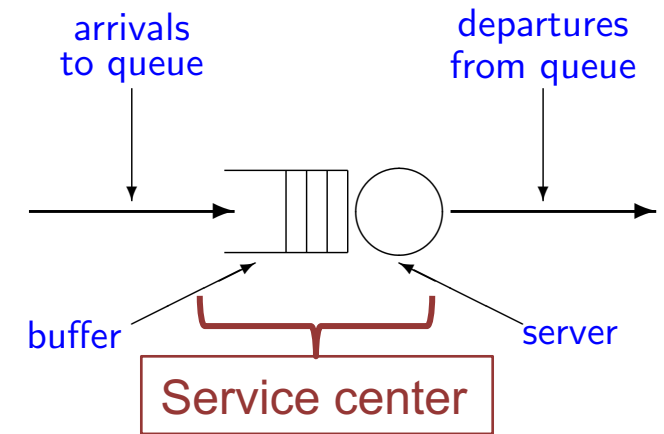
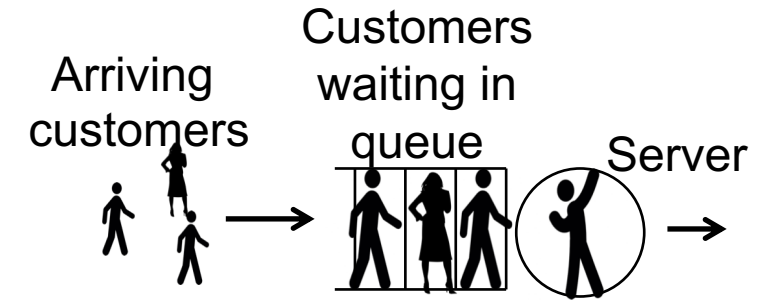
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Credits: Raffaella Mirandola



# Basic behavior of a single queue

- Customers, who belong to some population, arrive at the service center.
- The service center has one or more servers who are capable of performing the service required by customers.
- If a customer cannot gain access to a server it must join a queue, in a buffer, until a server is available.
- When service is complete the customer departs, and the server selects the next customer from the buffer according to the service discipline.





# Service Center

- Arrival
- Service
- Queue
- Population



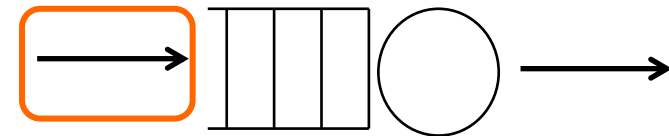
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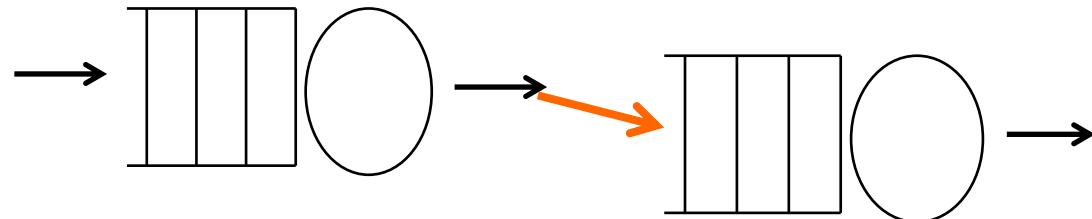
Arrivals represent jobs entering the system: they specify how fast, how often and which types of jobs the station serve.

Arrivals can come from:

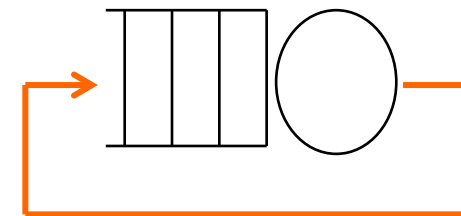
- an external source



- from another service center



- or from the same center, through a loop-back arc

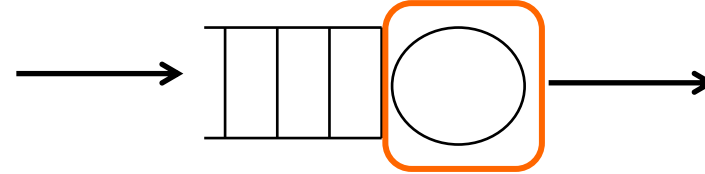


We will use the metric: **average arrival rate ( $\lambda$ )**

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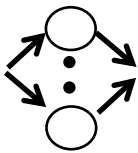
*The service part represents the time a job spends being served.*



We will use the metrics: **average service rate ( $\mu$ )**  
**average service time ( $1/\mu$ )**

**Number of servers:**

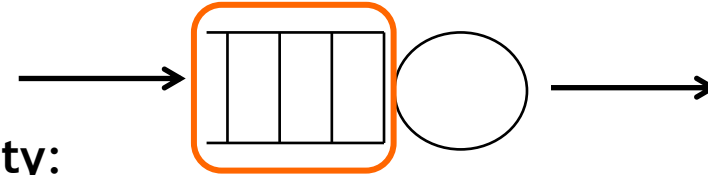
- **single server**: the service center has the capability to serve only one job at a time; waiting jobs will stay in the buffer until chosen for service.
- **c servers**: the service center has the capability to serve up to “c” jobs at a time.
- **infinite server**: there are always at least as many servers as there are jobs, so that each job can have a dedicated server as soon as it arrives in the center. There is no queueing. The service center acts as a delay.



# Service Center

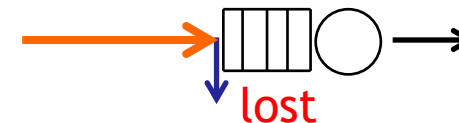
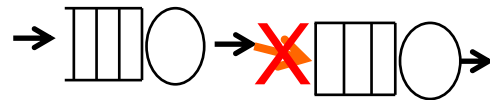
- Arrival
- Service
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Jobs who cannot receive service immediately must wait in the **queue** until a server becomes available.



Queue capacity:

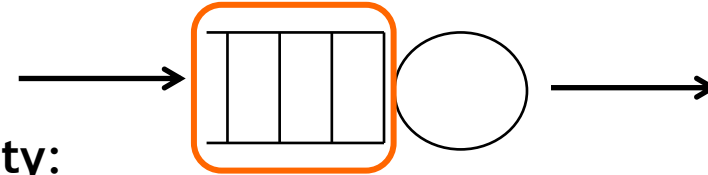
- **Finite capacity:** two alternative behaviors when the buffer becomes **full**
  - The fact that the center is full is passed back to the arrival process and **arrivals are suspended** until the center has spare capacity again
  - Arrivals continue and arriving **jobs are lost** until the center has spare capacity again.



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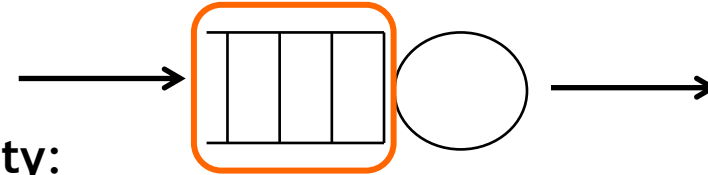
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Service discipline: First Come First Served (FCFS), LCFS, Random Selection, Round Robin, Processor Sharing, Priorities





# Service Center

- |   |  |
|---|--|
| <ul style="list-style-type: none"><li>• Arrival</li><li>• Service</li><li>• Queue</li><li>• <b>Population</b></li></ul> | <ul style="list-style-type: none"><li>• Ideally, members of the population are indistinguishable from each other.</li><li>• When this is not the case we divide the population into <b>classes</b> whose members all exhibit the same behavior.</li><li>• Different classes <b>differ</b> in one or more characteristics, for example, arrival rate, service demand, execution priority.</li></ul> |
|---|--|





# Example

Consider a wireless access gateway:



- Measurements have shown that packets arrive at a mean rate of 125 packets per second, and are buffered.
- The gateway takes 2 milliseconds on average to transmit a packet.
- The buffer currently has 13 places including the place occupied by the packet being transmitted. Packets that arrive when the buffer is full are lost.

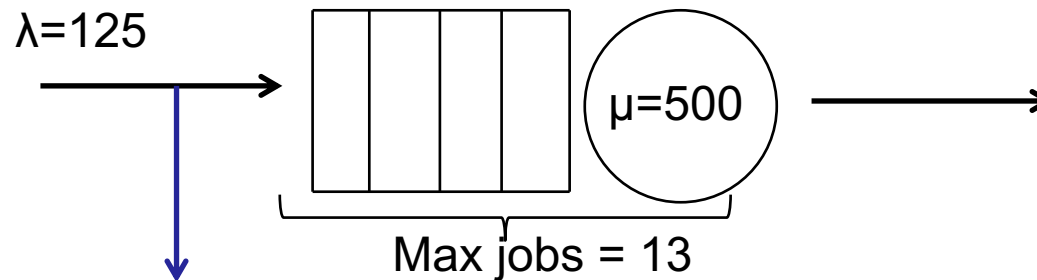


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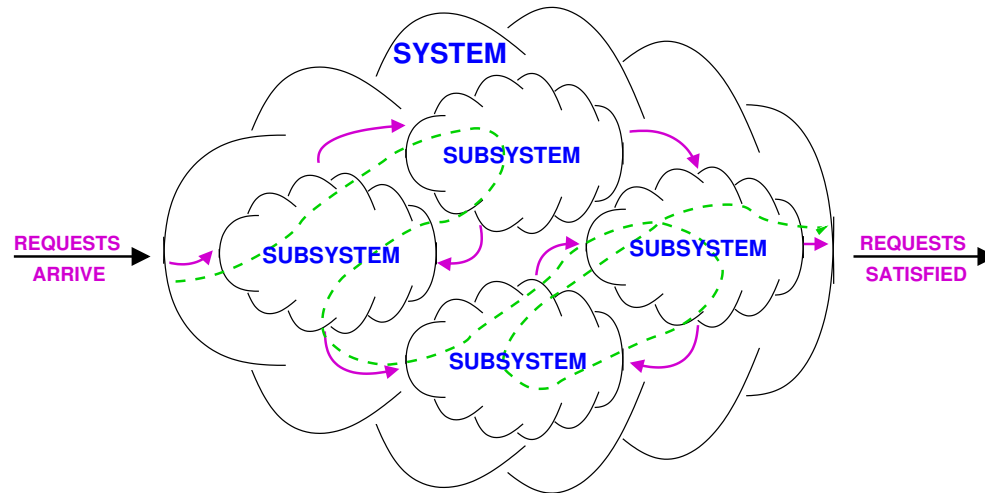


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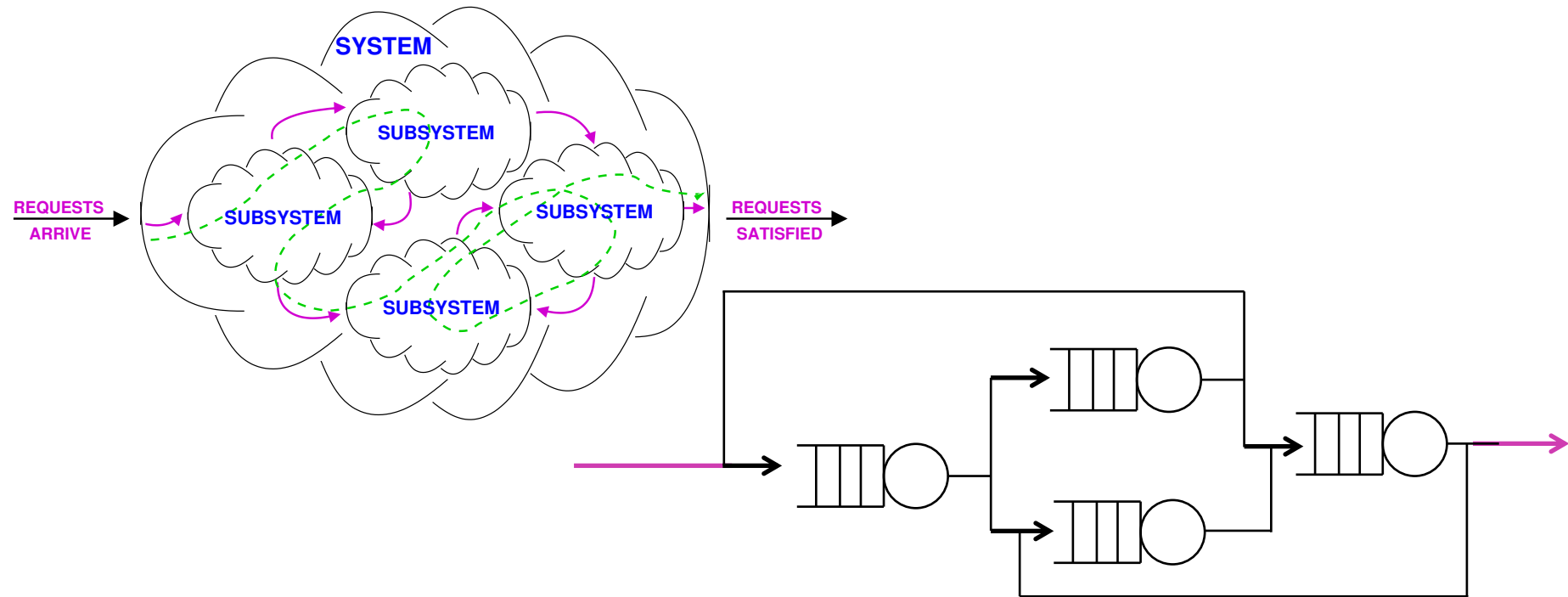
# Queueing network

- For many systems we can adopt a view of the system as a collection of service centers with customers or jobs circulating between them



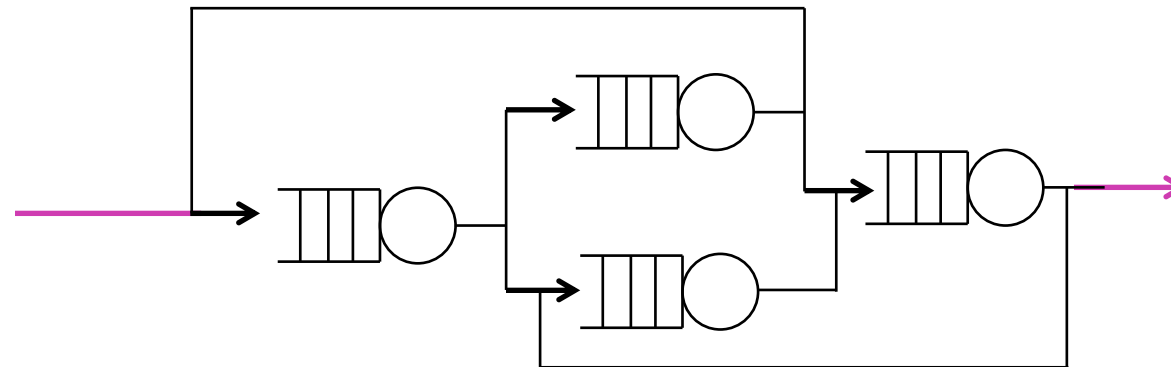
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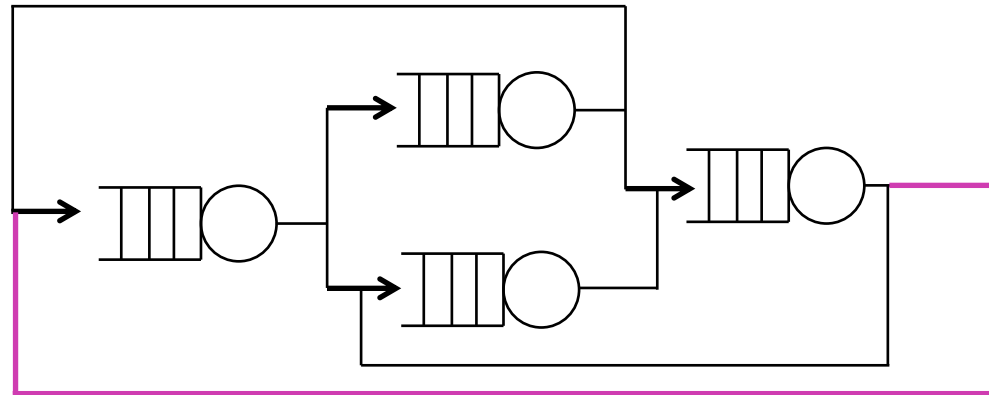
# Queueing network

- A network may be:
  - **open**, jobs may arrive from, or depart to, some external environment; or
  - **closed**, a fixed population that remains in the system;
    - Interactive
  - **mixed**, there are classes of jobs within the system exhibiting open and closed patterns of behavior respectively.



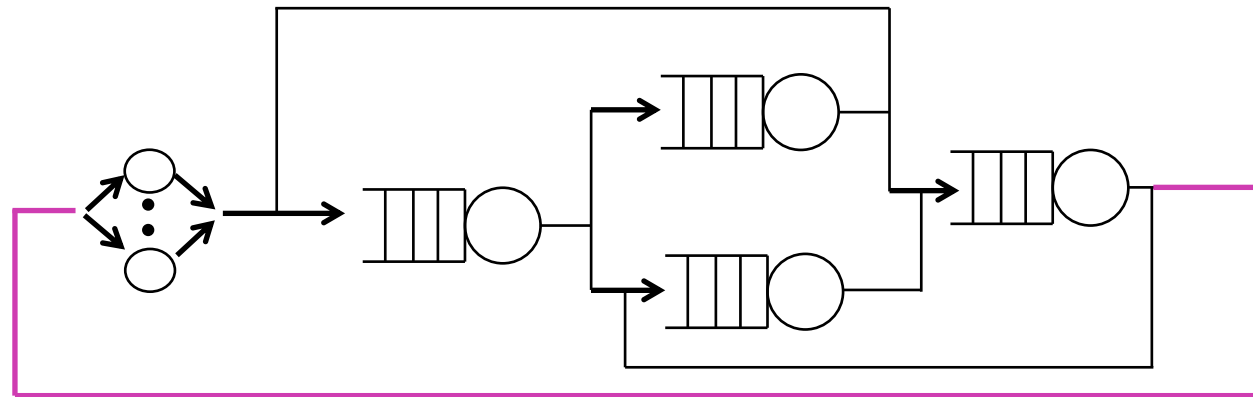
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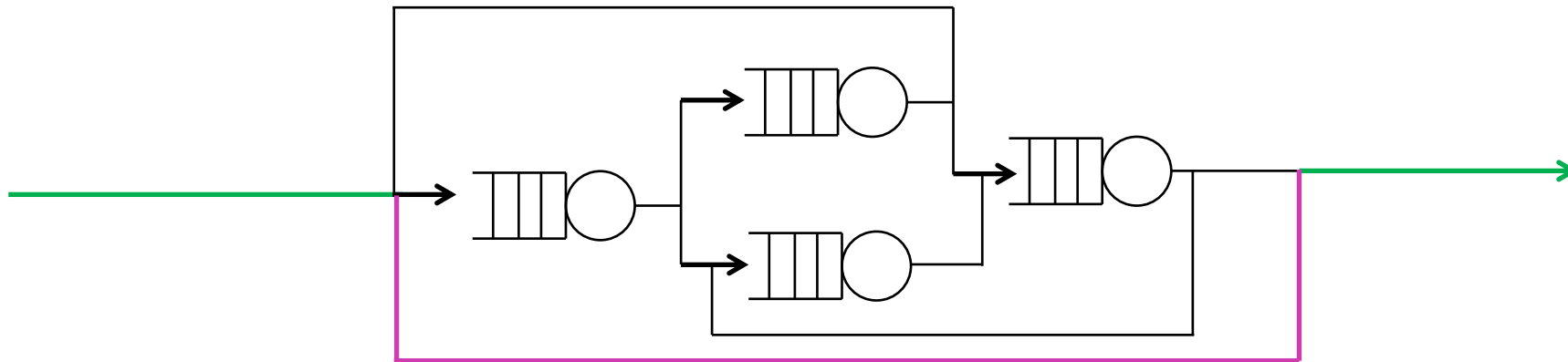
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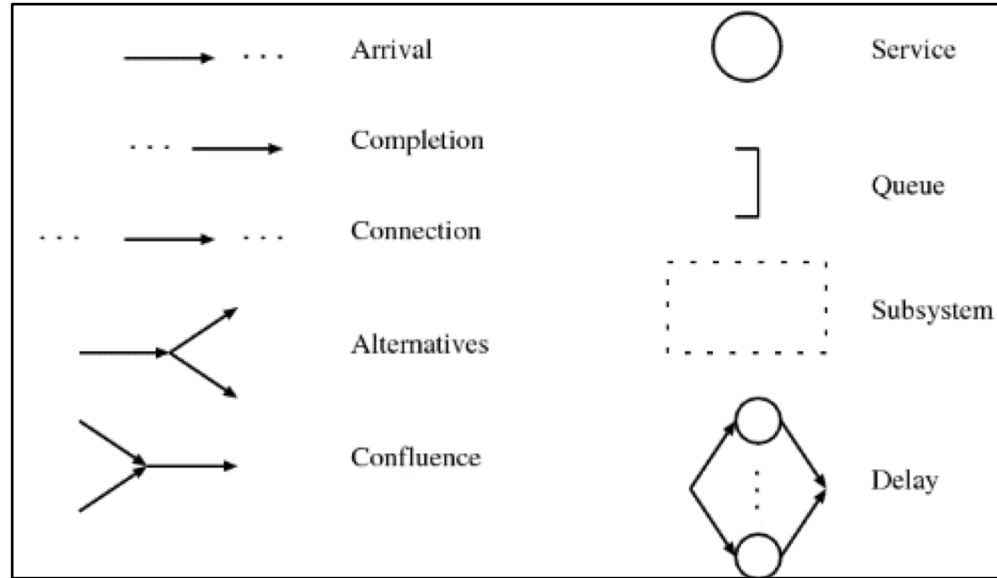
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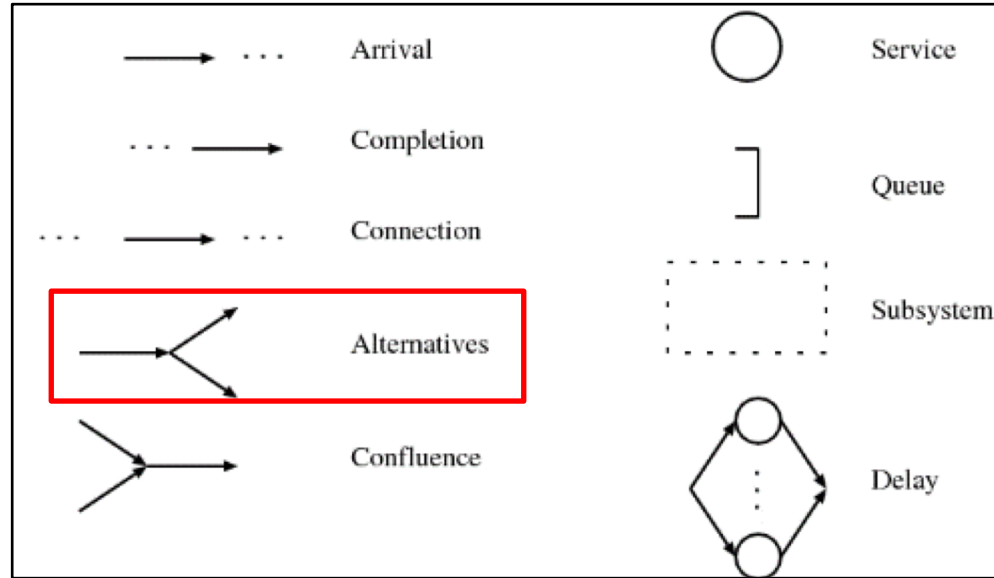
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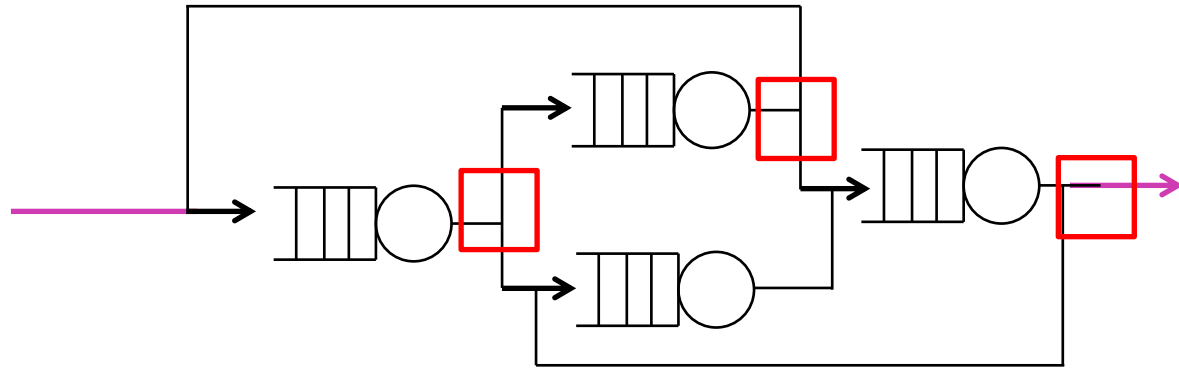
Whenever a job, after finishing service at a service center has several possible alternative routes, an appropriate selection policy must be defined.

The policy that describes how the next destination is selected is called routing.

We can change **class** of customer during routing

# Queueing network

- Arrival
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- **Routing**

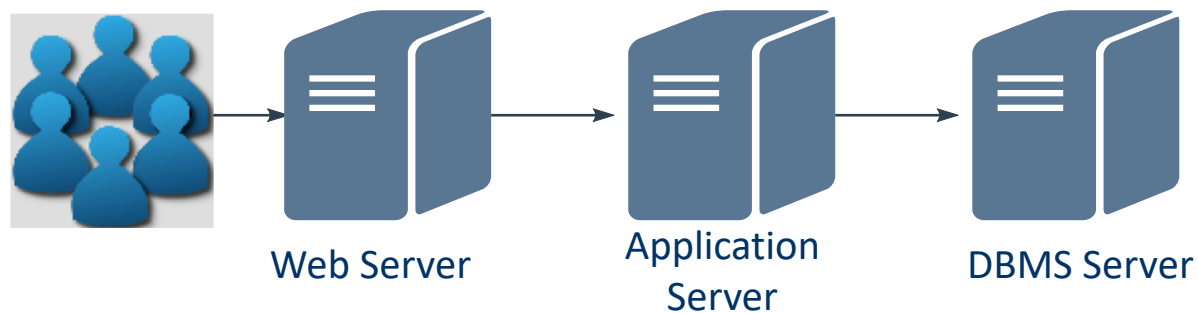


Main algorithms for alternatives:

- **Probabilistic:** each path has assigned a probability of being chosen by the job that left the service center.
- **Round robin:** the destination chosen by the job rotates among all the possible exits.
- **Join the shortest queue:** jobs can query the queue length of the possible destinations, and choose to move to the one with the lowest number of jobs waiting to be served.

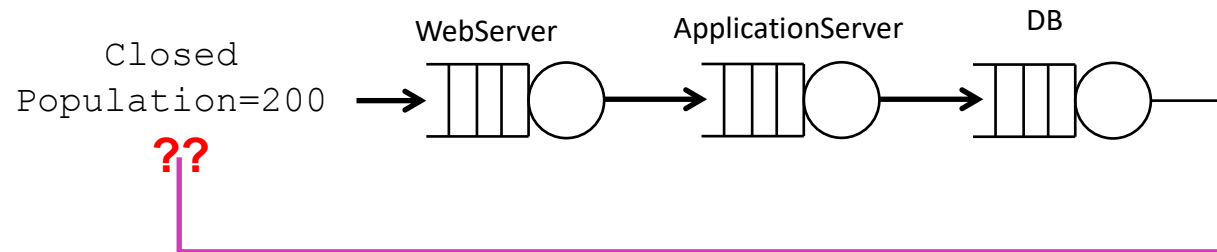
# Example

- The document repository system at our company has the following characteristics:
  - Users connect via web to a web server. There are 200 users.
  - The web server receives users requests and communicates to the application server of the system.
  - The application server processes the document to extract data of structured fields and connects to the Data Base server to store the document



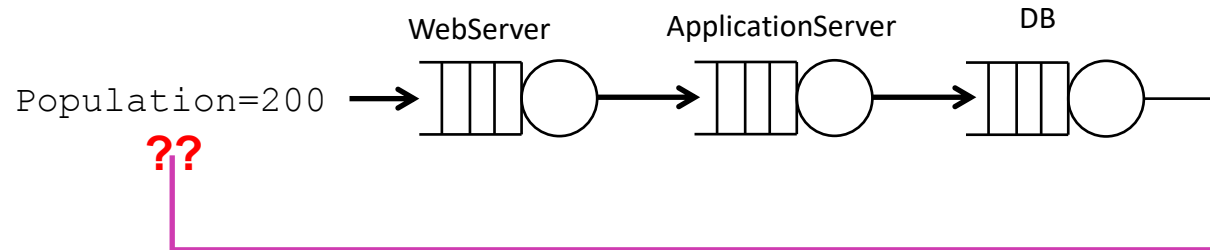
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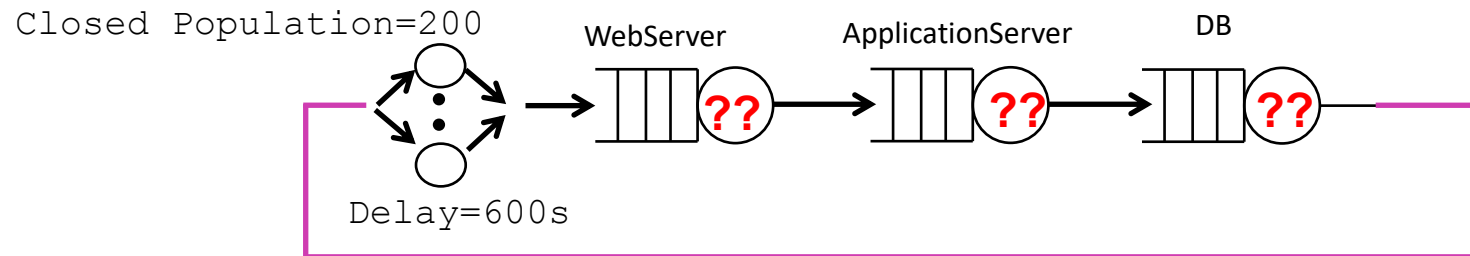
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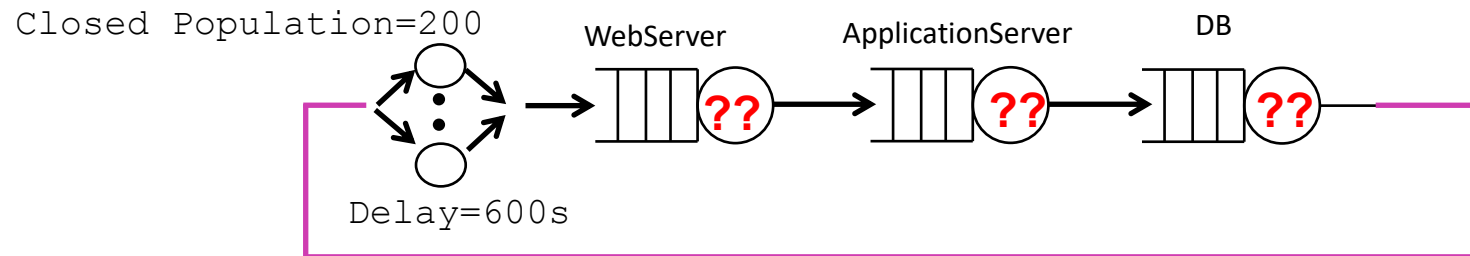
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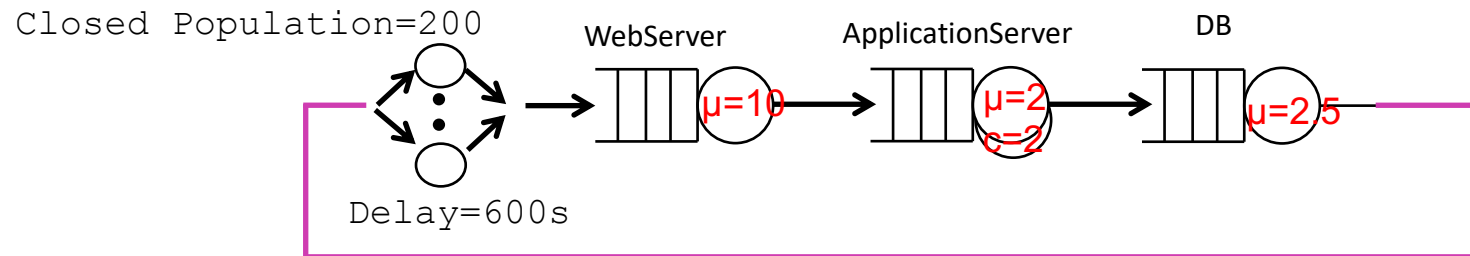
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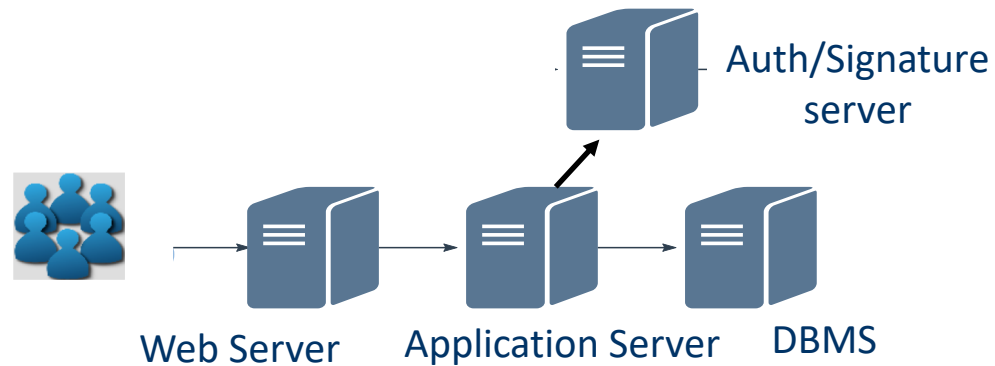
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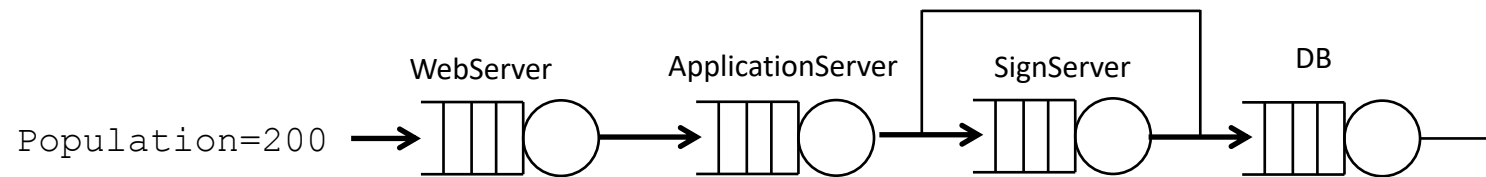
## Example (system upgrade)

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  - Users connect via web to a web **server** and can **request to sign the document**. There are 200 users
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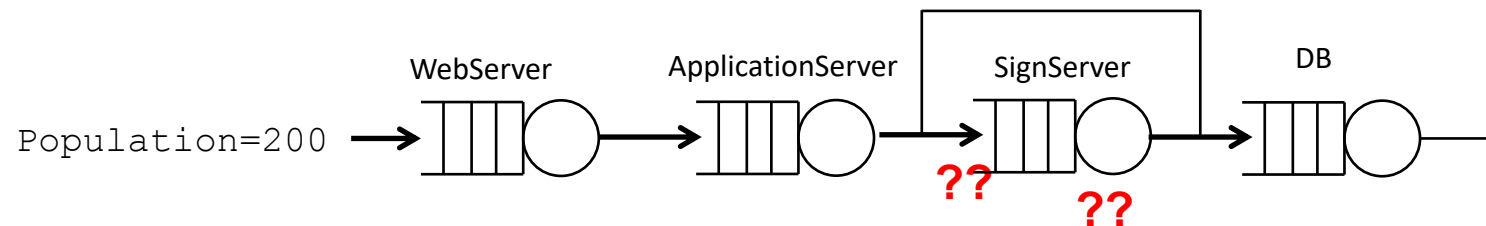
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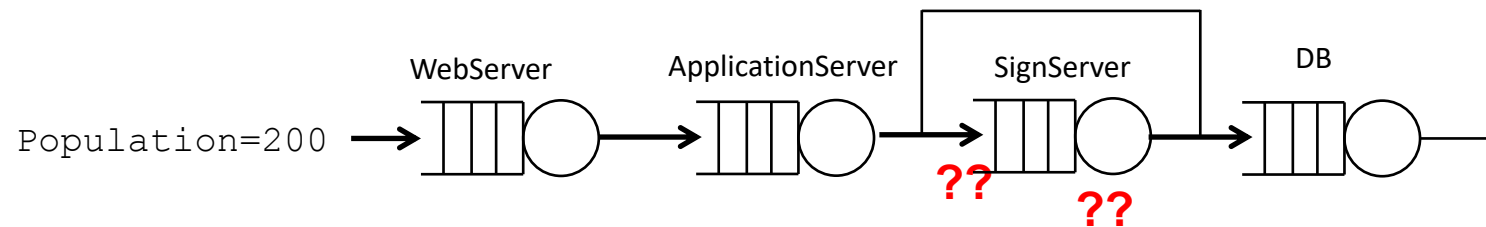
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