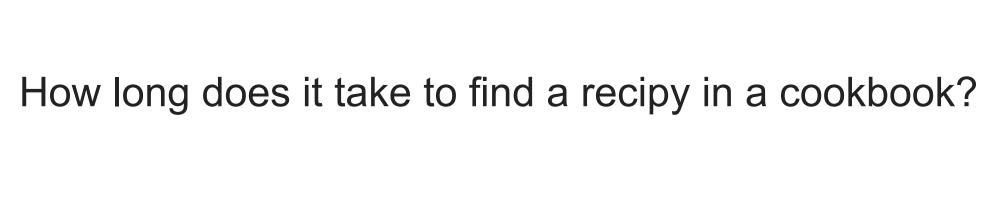
Python Programming for Data Science

Week 40, Friday

- Computational Complexity
- Exceptions



How long does it take to find a recipy in a cookbook? How can we answer a question like this?

Exercise: Finding a recipy in a cookbook

Let's say our cookbook contains 100 recipes.

How many recipes would we (on average) need to look at before finding the one we are looking for?

Exercise: Finding a recipy in a cookbook — solution

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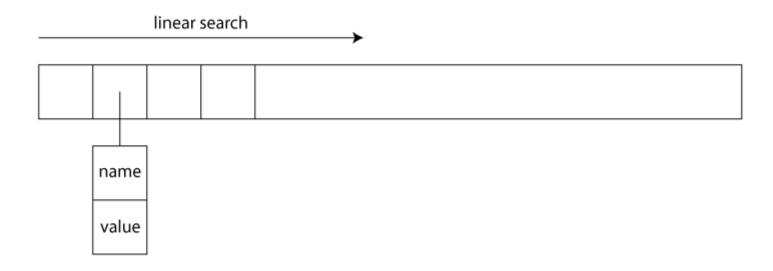
How many recipes would we (on average) need to look at before finding the one we are looking for?

Algorithm: We look at the recipes from the beginning to the end, and stop when we find it. On average, we will have to look at 100/2 recipes.

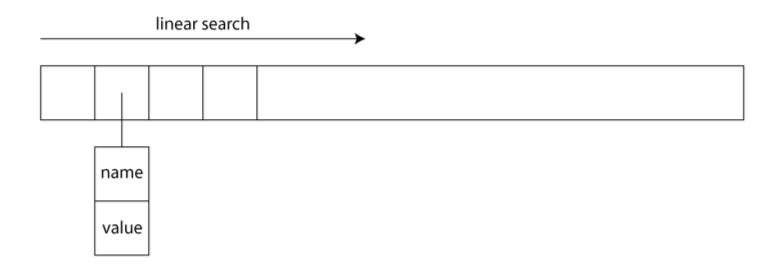
Exercise 1

Data: 25.000 genes and their DNA sequences. How do we represent this?

- 1. Could we use a list? How many genes would we need to look at to find a particular gene?
- 2. Would it help if we sorted the elements in the list?
- 3. How many genes would we need to look at to find a particular gene if we used a dictionary?



Q: How many elements will we (on average) have to look at before finding our element?



Q: How many elements will we (on average) have to look at before finding our element?

A: On average, we will have to look at 25.000/2 elements before we find the element we want

Exercise 1.2 - Does sorting help?

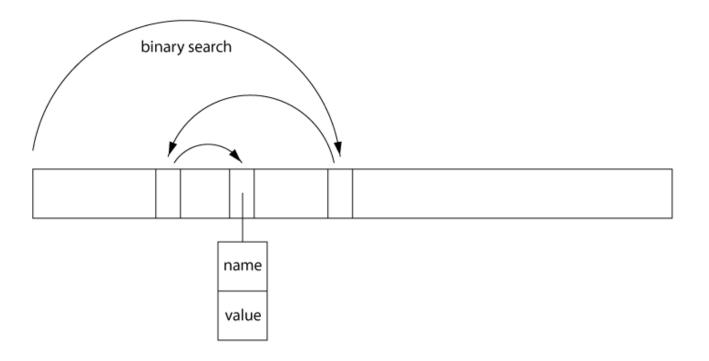
Exercise 1.2 - Does sorting help?

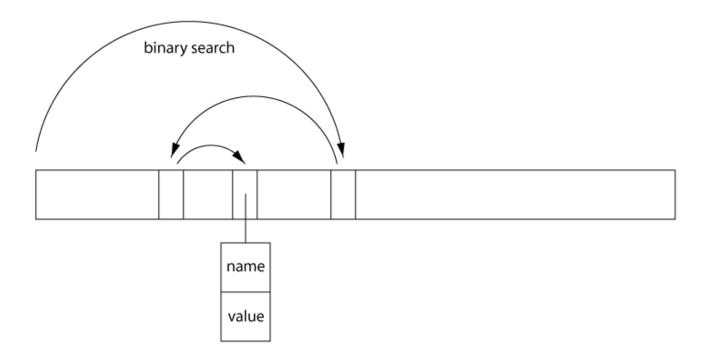
In other words: Is it easier to find a name in a phone book than a recipe in a cook book?

Exercise 1.2 - Does sorting help?

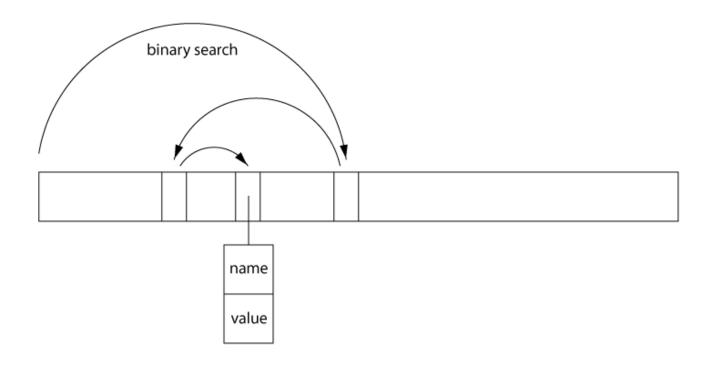
In other words: Is it easier to find a name in a phone book than a recipe in a cook book?

Yes.



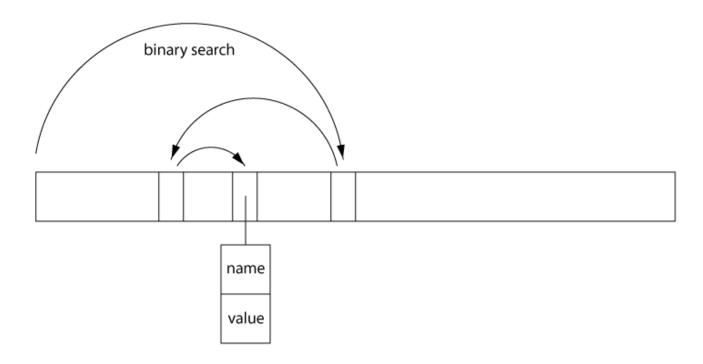


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This means we have to check roughly $log_2(25000) \approx 15$ elements before we find the element we want.

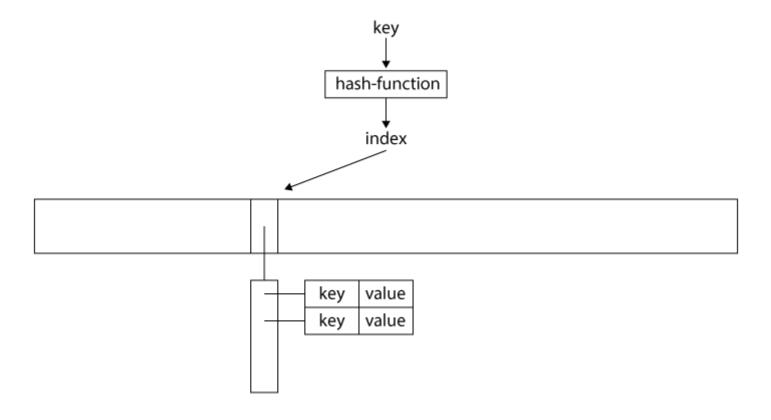


Using binary search, we exclude half of the list each time.

This means we have to check roughly $log_2(25000) \approx 15$ elements before we find the element we want.

(note: sorting also takes time: ($\sim 25000 * \log_2(25000)$).

Exercise 1.3 - solution: Dictionary



A dictionary will automatically create a function that maps key values to indices in a list. This means it can do lookups in very few operations.

Structuring data

 In data science, you are often in a situation where you need to represent a large amount of data in your program.

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Structuring data

- In data science, you are often in a situation where you need to represent a large amount of data in your program.
- We have seen several examples of situations where we read in data and store it in some data structure, for instance a list of lists or a dictionary of lists.
- The speed by which a given task can be solved is often very dependent on how you represent the data.

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We want to express the efficiency of an algorithm independent on the specific choice of cookbook, and independently of whether we run on a slow or a fast computer.

"How long" can therefore not really be measured in minutes or seconds.

Instead, we can express it in terms of the *input size*, n — in our case the number of recipes in the cookbook.

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- a conservative (worst case) estimate of the number of steps necessary to complete the algorithm
- expressed in terms of the size of the input n
- formally described using the big-O notation (e.g. O(n))

Mathematical notation that describes the asymptotic behaviour of a function.

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Think of the time complexity of a program as a function f(n) of the input size n.

- As the input size grows, the execution time typically grows
- We don't know exactly how it grows
- The O formalism is designed to give an upper bound.

Big-O notation - for the mathematically inclined

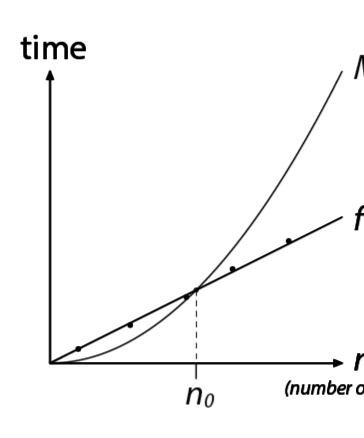
We say that

$$f(n) \in O(g(n))$$

if there exists values n_0 and M, such that

$$|f(n)| < M \cdot |g(n)|$$

for all $n>n_0$



Big-O notation - Examples

$$n^{2} + n + 3 \qquad \in O(n^{2})$$

$$3n^{8} + 4n + 7n^{10} \in$$

$$3n + 10 \qquad \in$$

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 $n + 1000000 \in O(n)$

Complexity - Exercise 2

1. What is the complexity of:

```
print(l) # l is a list of length n
```

2. What is the time complexity of the following code?

3. What is the time complexity of the following code? And what does it do?

Complexity - Exercise 2 - Solution (1)

```
1 = [4,6,2,5,7,8,9] print(1)
```

Complexity - Exercise 2 - Solution (1)

```
l = [4,6,2,5,7,8,9]
print(l)
```

Even though it is just a single command, print will have to look at all elements in the list in order to print them. The complexity is therefore O(n).

Complexity - Exercise 2 - Solution (2)

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Complexity: $O(n^2 + n) = O(n^2)$

Complexity - Exercise 2 - Solution (3)

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Complexity: $O(n(n + 1)/2 + n) = O(n^2)$

Complexity - Exercise 2 - Solution (3)

Complexity: $O(n(n + 1)/2 + n) = O(n^2)$

This algorithm is called bubble sort. It sorts the lists.

The built in sort method in python lists is faster. It has complexity $O(n \cdot \log(n))$

Complexity - Exercise 3

- 1. What is the complexity of looking up an element in a list using []?
- 2. What is the complexity of removing an element in a Python list (using pop())?
- 3. What is the complexity of the strip() method in the string class?
- 4. What is the complexity of your handin4_test.py?

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We have already seen exceptions in action many times. Every time you have written a program that crashed this has been due to an exception.

Exceptions - example

```
a = ?

output

File "/home/lpp/lpp2016/exceptions.py", line 1
   a = ?
   ^
SyntaxError: invalid syntax
```

Exceptions - example

The program crashes because we assign? to the variable a.

This does not make sense, so Python complains.

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This does not make sense, so Python complains.

Python automatically raises built-in exception when it discovers an error, and terminates the program (default behavior).

Exceptions - more examples

```
d = {'Mon':'Monday', 'Tue':'Tuesday'}
print(d[Wed])

Traceback (most recent call last):
   File "/home/lpp/lpp2016/exceptions.py", line 2, in
     print(d[Wed])
NameError: name 'Wed' is not defined
output
```

Q: What's wrong here? What is Python trying to tell us?

Exceptions - more examples

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      print(d[Wed])
NameError: name 'Wed' is not defined
output
```

Q: What's wrong here? What is Python trying to tell us?

A: Python thinks Wed is a variable, which is not defined

Exceptions - more examples (1)

```
print(d['Wed']) # Specify Wed as a string

Traceback (most recent call last):
   File "/home/lpp/lpp2016/exceptions.py", line 2, in
        print(d['Wed'])
   KeyError: 'Wed'
```

Exceptions - more examples (1)

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KeyError: 'Wed'
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Q: What's wrong this time? What is Python trying to tell us?

A: The key 'Wed' is not present in our dictionary.

Catching exceptions

Rather than letting the program crash, you can define how to respond to an exception

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This is done using *try-catch* statements

```
d = {'Mon':'Monday', 'Tue':'Tuesday'}
try:
    d['Wed']  # you can have as many lines as you want in here
except:
    # print keys to screen when error occurs.
    print("Key not found in dictionary. Available keys:", d.keys())
```

```
Key not found in dictionary. Available keys: ['Mon', 'Tue']
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except:
    # print keys to screen when error occurs.
    print("Key not found in dictionary. Available keys:", d.keys())
Key not found in dictionary. Available keys: ['Mon', 'Tue']
```

Now that the exception has been caught, it will no longer crash your program.

Catching specific exceptions

Rather than catching *any* type of exception, you can specify that you only want to catch exceptions of a certain type.

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```
d = {'Mon':'Monday', 'Tue':'Tuesday'}
try:
    d['Wed']
except KeyError: # <- Only catch KeyError exceptions
    # print keys to screen when error occurs.
    print("Key not found in dictionary. Available keys: ", d.keys())</pre>
```

```
Key not found in dictionary. Available keys: ['Mon', 'Tue']
```

Catching specific exceptions (continued)

If we catch the wrong exception type, we will get the original behavior:

Catching specific exceptions (continued)

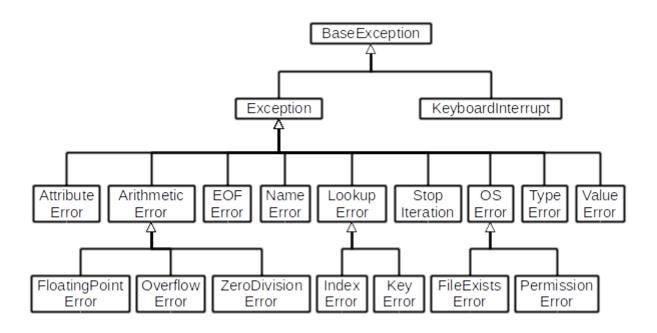
If we catch the wrong exception type, we will get the original behavior:

```
d = {'Mon':'Monday', 'Tue':'Tuesday'}
try:
    d['Wed']
except NameError: # <- Only catch NameError exceptions
    # print keys to screen when error occurs.
    print("Key not found in dictionary. Available keys: ", d.keys())</pre>
```

```
Traceback (most recent call last):
   File "/home/lpp/Documents/lpp2015/errors.py", line 2, in <module>
        d['Wed']
KeyError: 'Wed'  # <- NOTE: our bug produces a KeyError</pre>
```

Exceptions – Class hierarchy

Pythons built-in exceptions are structured in a class hierarchy.



Catching specific exceptions (continued 2)

The class hierarchy makes it possible to be more flexible in specifying which exceptions to catch

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The exception type that you specify and all derived classes from this class will be caught

```
d = {'Mon':'Monday', 'Tue':'Tuesday'}
try:
    d['Wed']
except Exception: # Exception covers both NameError and KeyError
    print("Key not found in dictionary. Available keys: ", d.keys())
```

Catching exceptions – accessing details

You can access the exception object itself to gain extra information regarding the error.

This this done using the as keyword

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This this done using the as keyword

```
d = {'Mon':'Monday', 'Tue':'Tuesday'}
try:
    d['Wed']
except Exception as error: # Save error object
    # error contains information about key that failed
    print("Information about error: " + str(error))
```

```
Information about error: 'Wed'
```

Exercise

Write the most specific try/except statement for each of the following situations:

1.

```
print(I_love_python)
```

2.

```
l=[1,2,3,4]
print(l[4])
```

3.

```
print(1/0)
```

1.

```
print(I_love_python)

Traceback (most recent call last):
   File "/home/lpp/lpp2016/exceptions.py", line 1, in
      print(I_love_python)
NameError: name 'I_love_python' is not defined
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1.

```
print(I_love_python)

Traceback (most recent call last):
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```

We note that our mistake raises a NameError. Solution:

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NameError: name 'I_love_python' is not defined
```

We note that our mistake raises a NameError. Solution:

```
try:
    print(I_love_python)
except NameError as error:
    print("Something is wrong here: %s" % error)
```

2.

```
l=[1,2,3,4]
print(1[4])

Traceback (most recent call last):
   File "/home/lpp/lpp2016/exceptions.py", line 2, in
      print(1[4])
IndexError: list index out of range
```

2.

```
l=[1,2,3,4]
print(l[4])

Traceback (most recent call last):
   File "/home/lpp/lpp2016/exceptions.py", line 2, in
      print(l[4])
IndexError: list index out of range
```

We note that our mistake raises an IndexError. Solution:

2.

```
l=[1,2,3,4]
print(l[4])

Traceback (most recent call last):
   File "/home/lpp/lpp2016/exceptions.py", line 2, in
        print(l[4])
IndexError: list index out of range
```

We note that our mistake raises an IndexError. Solution:

```
l=[1,2,3,4]
try:
    print(l[4])
except IndexError as error:
    print("Something is wrong here: %s" % error)
```

3.

```
print(1/0)

Traceback (most recent call last):
   File "/home/lpp/lpp2016/exceptions.py", line 1, in
        print(1/0)
ZeroDivisionError: integer division or modulo by zero
```

3.

```
print(1/0)

Traceback (most recent call last):
   File "/home/lpp/lpp2016/exceptions.py", line 1, in
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ZeroDivisionError: integer division or modulo by zero
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We note that our mistake raises a ZeroDivisionError. Solution:

3.

```
print(1/0)

Traceback (most recent call last):
   File "/home/lpp/lpp2016/exceptions.py", line 1, in
        print(1/0)
ZeroDivisionError: integer division or modulo by zero
```

We note that our mistake raises a ZeroDivisionError. Solution:

```
try:
    print(1/0)
except ZeroDivisionError as error:
    print("Something is wrong here: %s" % error)
```

Raising exceptions

You can also raise the built-in exceptions yourself:

```
raise KeyError

Traceback (most recent call last):
   File "/home/lpp/lpp2016/exceptions.py", line 1, in
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KeyError
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```

The raise statement can be used at any place in your code to interrupt the program

Exceptions – the assert statement

It is common to insert sanity checks in a program, testing that a particular condition is always true

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assert condition # raises an AssertionError if condition is not True
```

Example:

```
x = 2
assert x>0 and x<10
assert x<0 and x>10
```

Exercise

Write a function that takes a single number as argument

- 1. The function should check that this number is an even number (0,2,4,6,...) and raise an exception otherwise.
- 2. Call the function with an uneven number:
 - Without catching the exception
 - Catching the exception and printing a warning.

```
def my_function(value):
    '''Function without any functionality. But assumes that value is even.
    assert value%2 == 0  # Raise exception if value is not even

# Call with uneven number
my_function(1)
```

```
Traceback (most recent call last):
    File "/home/lpp/Documents/lpp2016/errors.py", line 22, in <module>
        my_function(1)
    File "/home/lpp/Documents/lpp2016/errors.py", line 13, in my_function
        assert value%2 == 0
AssertionError
```

```
# Call with uneven number - catch AssertionError
try:
    my_function(1)
except AssertionError:
    print("Assertion failed in function")
```

Assertion failed in function

output

Defining your own exceptions

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This is done by creating a class that inherits from Exception

```
class MyException(Exception):  # Defining a very simple exception class
    pass

raise MyException  # Raising an exception of this type
```

```
Traceback (most recent call last):
   File "/home/lpp/Documents/lpp2014/errors.py", line 8, in <module>
     raise MyException
   __main__.MyException
```

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     raise MyException
   __main__.MyException
```

For more information, see the python docs.

try...except...finally

Consider this code

```
try:
    data_file = open("/usr/share/dict/british-english")

words = {}
    for i, line in enumerate(data_file):
        words[line.strip()] = i

print(words['bokeh'])

data_file.close()
except KeyError as error:
    print("Word %s not found" % str(error))
```

Q: What's wrong here?

try...except...finally

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```

Q: What's wrong here? A: We don't close the file when an exception occurs

try...except...finally(2)

You can fix the previous example by adding a finally clause to your try-except statement

```
try:
    data_file = open("/usr/share/dict/british-english")

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except KeyError as error:
    print("Word %s not found" % str(error))

finally:
    data_file.close()
```

This code will be executed no matter whether an exception was raised or not

The with statement

This pattern is very common

```
thing = initialize_thing()  # (e.g. open a file)
try:
    # do something with thing
finally:
    finalize_thing()  # (e.g. close a file)
```

The with statement

This pattern is very common

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For this reason, the following shortcut was introduced

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with initialize_thing() as thing:
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with initialize_thing() as thing:
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Example from before:

```
with open("/usr/share/dict/british-english") as data_file:
   words = {}
   for i, line in enumerate(data_file):
      words[line.strip()] = i
    print(words['bokeh'])
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The with statement (2)

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Note how the file is now automatically closed when the file exists the with statement

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Note how the file is now automatically closed when the file exists the with statement

This only works for classes that have implemented the following two methods:

- __enter__: Initializes object
- __exit__: Finalizes object

The file class is one such example