
Advanced Deep Learning: Representations in Practice

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coASfal

Course outline

Goal 1: Quick tour of recent developments in deep learning

Goal 2: Inspiration for thesis/research projects

Week	Lecturer	Subject	Literature	Assignment
1	Stefan	Introduction to Neural Networks.	d2l 2.1-2.5, 2.7, 11.5.1, slides	
2	Stefan	CNNs; FCNs; U-Nets. Data augmentation; invariance; regularization e.g. dropout	d2l 6, 7, 13.9-13.11, slides	Assignment 1 (May 10)
3	Anders/Phillip	May 9 (A): RNNs May 11 (P): Transformers	d2l 8 Transformers: d2l 10.5-10.7 + Vaswani et al. (2017) ^e	Assignment 2 (May 20)
4	Phillip/Anders	May 16 (P): Representation and Adversarial Learning May 18 (A): A Learning Framework + Self-supervised Learning + Contrastive Learning	Autoencoders: blog post ^e GANs: Goodfellow (2016) ^e Self-supervised learning: blog post ^e Contrastive learning: Dor et al. (2018) ^e Adversarial examples: Goodfellow et al. (2015) ^e	
5	Anders	May 23: General Properties, e.g., Scaling Laws, Lottery Tickets, Bottleneck Phenomena May 25: Applications of Representation, Adversarial and Contrastive Learning	GANs: Lample et al. (2018) ^e Autoencoders: Chandar et al. (2011) ^e Contrastive learning: Yu et al. (2018) ^e DynaBench: Talk by Douwe Kiela ^e (Facebook, now HuggingFace) Scaling laws: Kaplan et al. (2020) ^e	Assignment 3 [<i>MC on Representation Learning</i> /1p Report on Lottery Ticket extraction] (June 3)
6	Anders	May 30: Interpretability, Transparency, and Trustworthiness & Deep Learning for Scientific Discovery June 1: Interpretability (Feature Attribution), including Guest Lecture by Stephanie Brandl	DL for Scientific Discovery: Sullivan (2022) ^e Interpretability/Background: Segaard (2022) ^e	
7	Anders	June 6: <i>Off (no teaching)</i> June 8: Interpretability (Training Data Influence)	Literature: Feng and Boyd-Graber (2018) ^e ; Jiang and Senge (2021) ^e	
8	Anders	June 13-15: Best Practices	Literature: Dodge et al. (2019) ^e and Raji et al. (2021) ^e	Assignment 4 [<i>MC on Interpretability</i> ; 1p Report on Best Practices] (June 21)

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Goal 2: Inspiration for thesis/research projects

Architectures

Framework

Fairness /

Explainable AI

Methodology

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Today

- a) Feature spaces
 - b) Shoehorning text into vector spaces
 - c) How to compare vector spaces
 - d) How to align vector spaces
 - e) Applications
 - i) fMRI analysis
 - ii) Cross-lingual learning
 - iii) Multi-modal analysis
 - iv) Bias detection
-

Feature spaces

Feature spaces

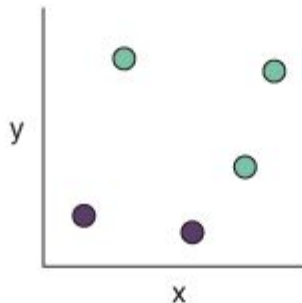
- Feature spaces are vector spaces.
 - A vector space is anything that supports addition, subtraction and scalar multiplication of vectors and has a zero vector.
 - Imagine a feature space with height, weight, and age. This is a three-dimensional vector space with vectors of the form $\langle 172, 58, 29 \rangle$.
-

Dimensionality trade-off

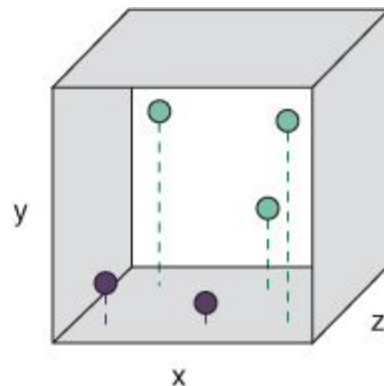
In standard machine learning, dimensionality was determined by considerations of statistical support and separability. As we saw last time, scaling laws for DNNs seem to also reflect training dynamics.



One dimension



Two dimensions



Three dimensions

Text vector spaces

Vector spaces

Old idea.

Salton, 1983

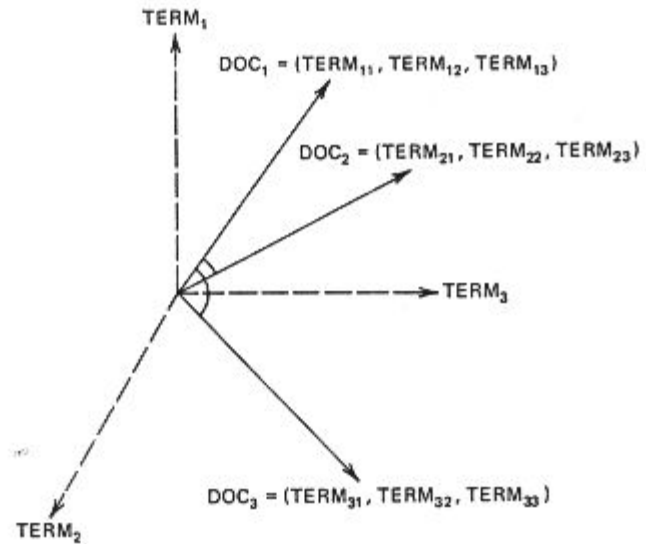
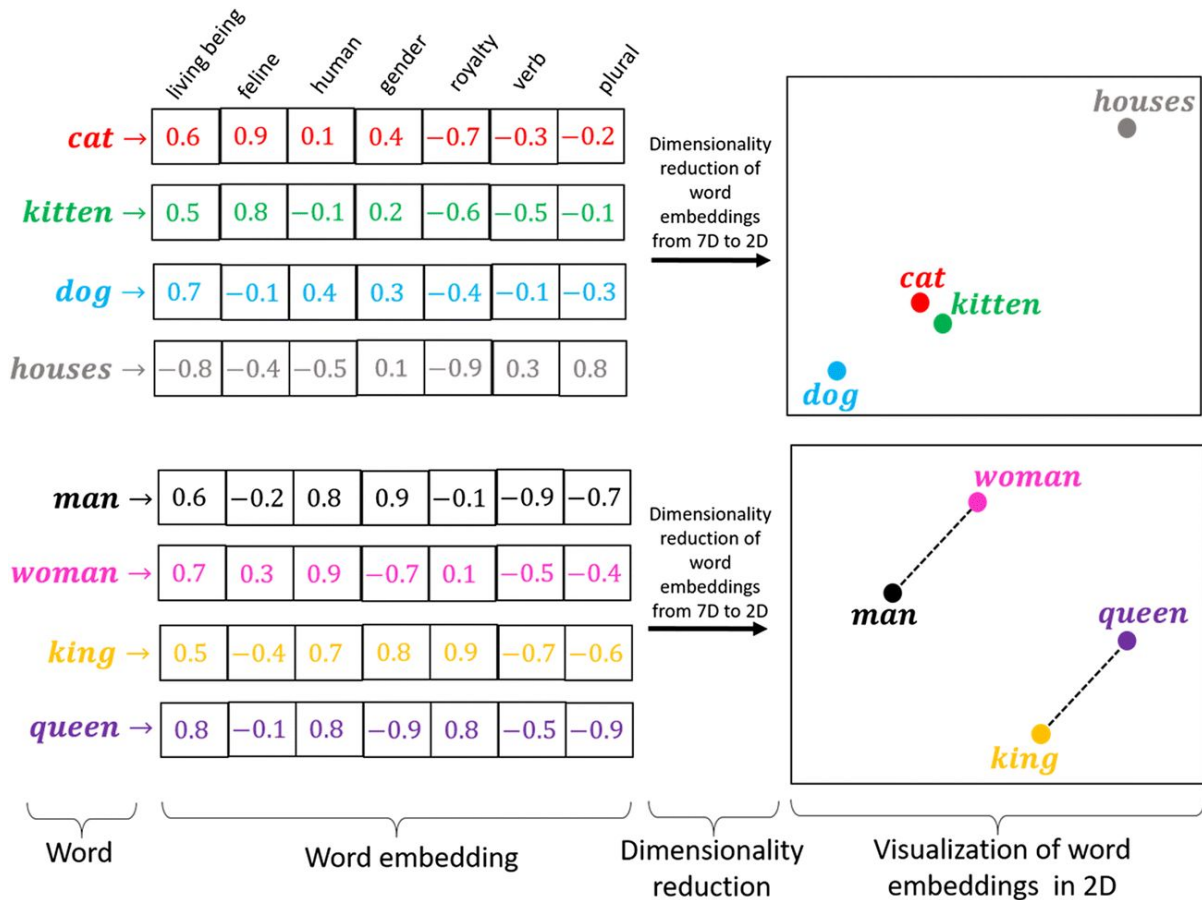


Figure 4-2 Vector representation of document space.

Word Embeddings: Idea

Vector representations of words that enable us to reason about word similarity.



Demo screenshots

You can use word embeddings to explore associations in different corpora.

Select corpus: Danish newspapers 1900-2016 ▾

Nearest words: krig

Analogy: man is to woman as king is to ?

#	Word
1	konflikt Search in Mediestream
2	militærmagt Search in Mediestream
3	verdensfreden Search in Mediestream
4	splitelse Search in Mediestream
5	massakre Search in Mediestream

Select corpus: Grundtvig ▾

Nearest words: krig

Analogy: man is to woman as king is to ?

#	Word
1	alrik
2	rhodierne
3	underhandler
4	stilstanden
5	feide

Demo screenshots

You can use word embeddings to explore associations in different corpora.

Select corpus: Danish newspapers 1900-2016

Nearest words: krig **Go**

Analogy: man is to woman as king is to ? **Go**

#	Word
1	konflikt Search in Mediestream
2	militærmagt Search in Mediestream
3	verdensfreden Search in Mediestream

Models

Select one of the available models

English GoogleNews Negative300

Nearest words

Given a word, this demo shows a list of other words that are similar to it, i.e. nearby in the vector space.

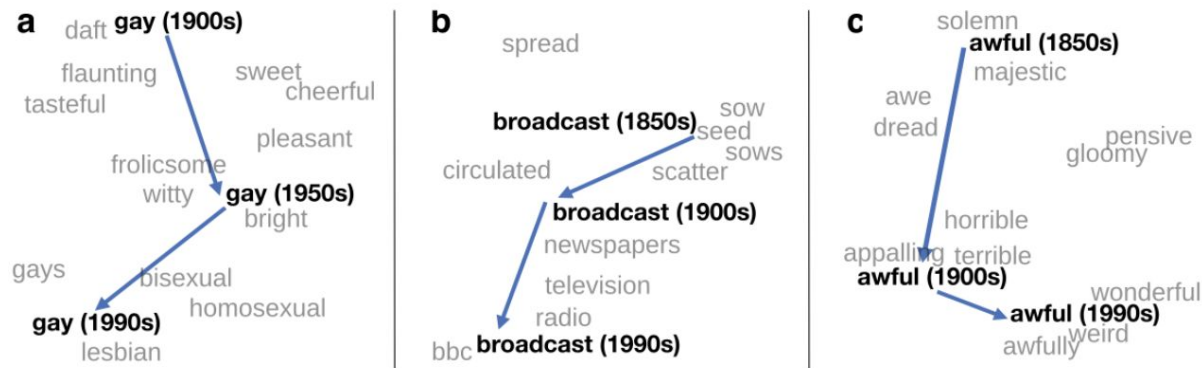
war **Show nearest** **Case sensitive:** ☒ **Top N:** 10

wars
War
invasion
Persian_Gulf_War
Vietnam_War
Iraq
occupation
conflict
hostilities
Cold_War

3	underhandlinger
4	stilstanden
5	feide

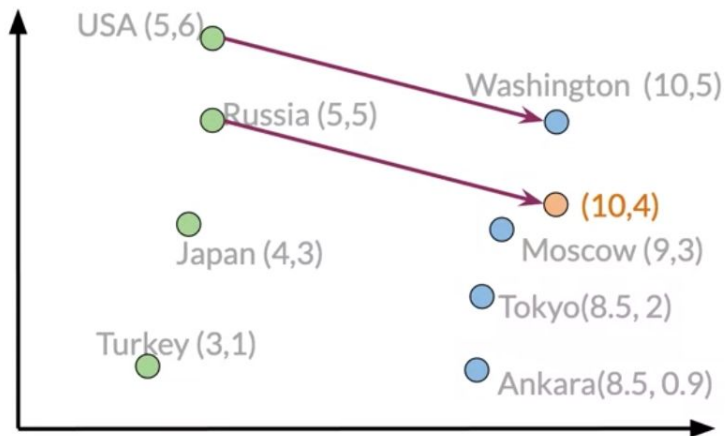
Temporal drift

We can also use word embeddings to monitor changes in word associations over time.



From analogies to isomorphism

If two spaces respect the same analogies, covering all words, they're isomorphic.

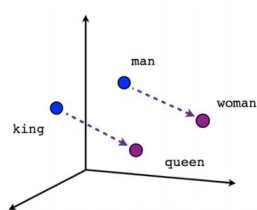


$$\text{Washington} - \text{USA} = \begin{bmatrix} 5 & -1 \end{bmatrix}$$

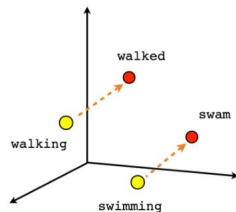
$$\text{Russia} + \begin{bmatrix} 5 & -1 \end{bmatrix} = \begin{bmatrix} 10 & 4 \end{bmatrix}$$

How to evaluate embeddings?

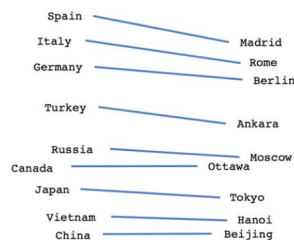
- Word associations
- Word analogies
- Alignment with lexical databases
- Downstream applications



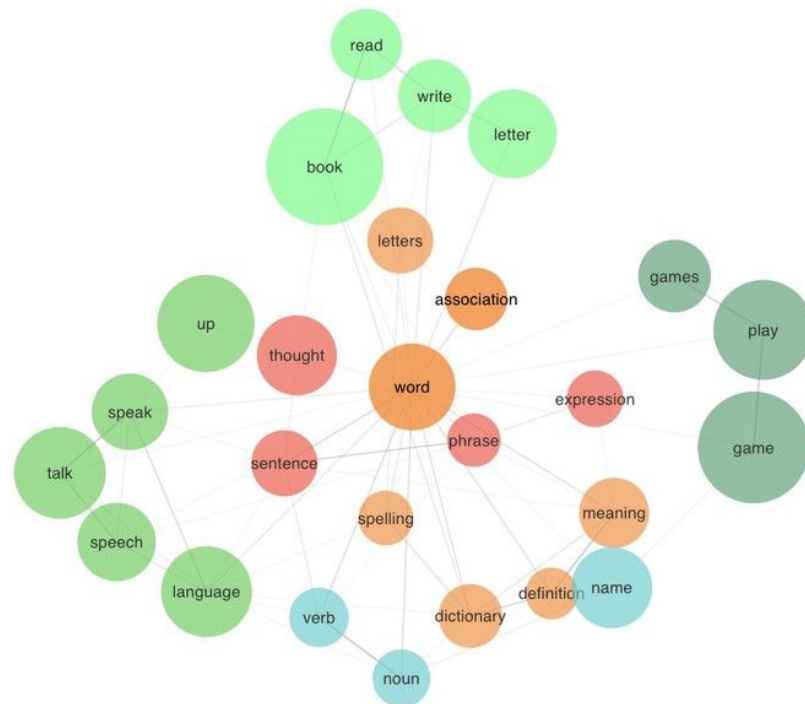
Male-Female



Verb tense

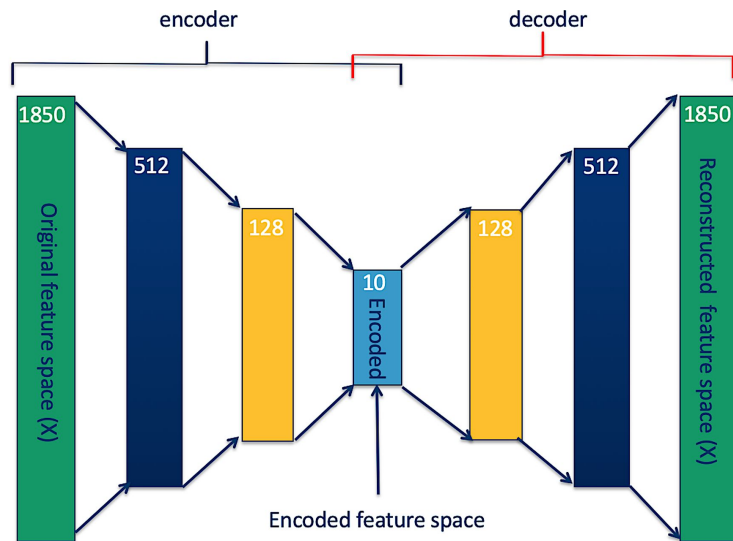
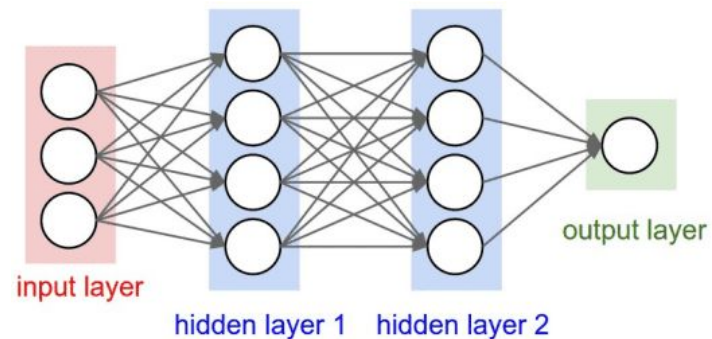


Country-Capital

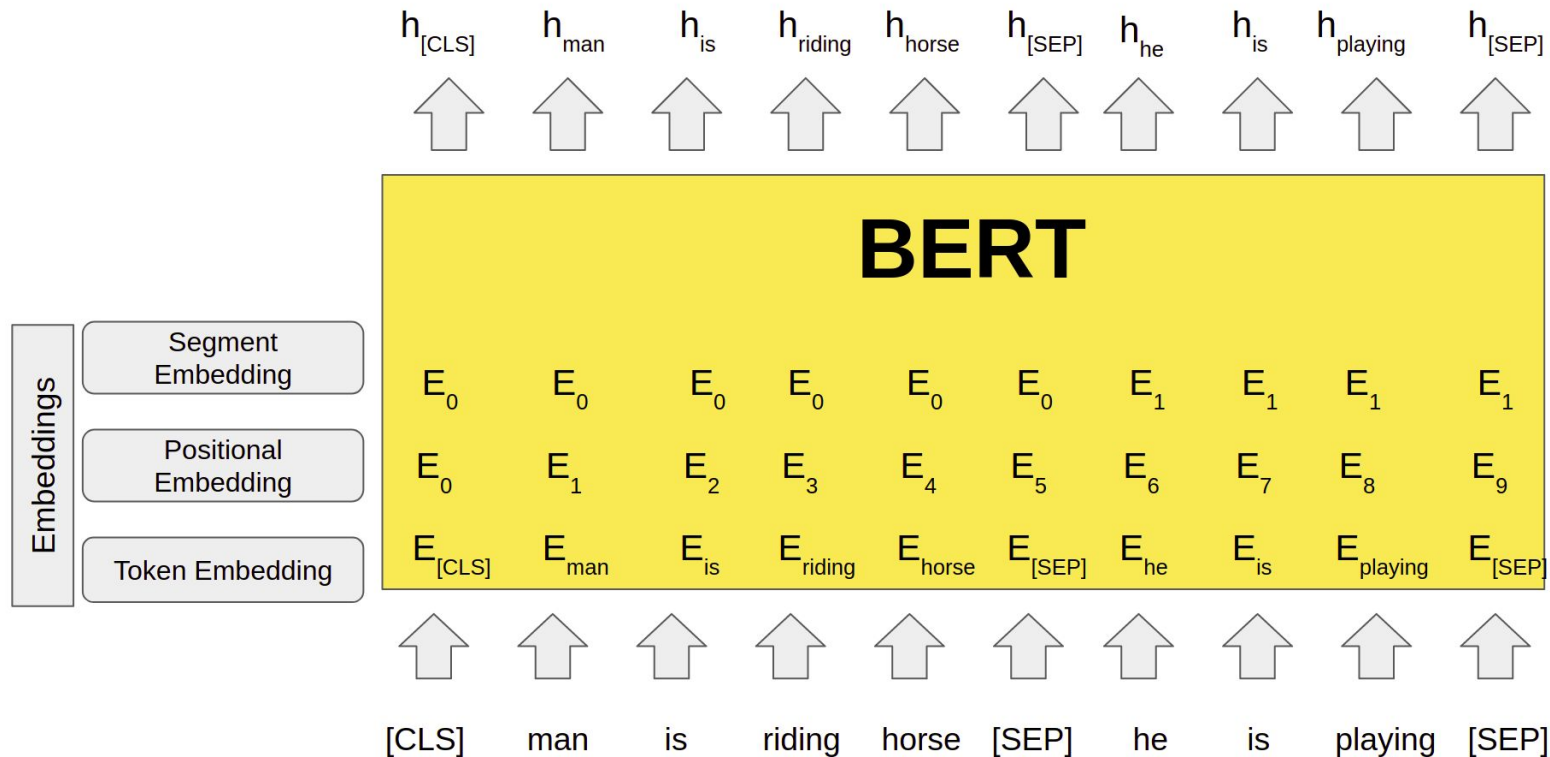


Deep networks as representation learners

Pretrained language models – such as BERT and GPT – are also text vectorizers. DNNs are generally representation learners and can be used as such (frozen); see e.g. Bert-as-a-service.



Challenges evaluating LM embeddings



Strategies

- Token embeddings
 - Output token embeddings
 - Sentence or output token embeddings in simple contexts, e.g., 'This is a ____'
 - Averaging over simple contexts
 - Averaging over randomly sampled contexts
-

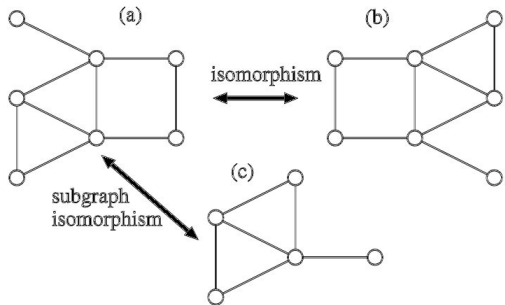
How to compare

Representational similarity

- Isometry

Challenge:

Vector spaces of different models or modalities are of course never *completely* isometric, but isomorphic?



Isomorphisms of Vector Spaces

Definition: An *isomorphism* (of V with W) is a *bijective* linear map $T : V \rightarrow W$.

Two vector spaces V and W are *isomorphic* if there exists an isomorphism $T : V \rightarrow W$. If this is the case, then we write $V \simeq W$.

Theorem 25: Let $T : V \rightarrow W$ be any map. Then T is *bijective* if and only if it has an inverse.

Theorem 26: Let $T : V \rightarrow W$ be a linear map and suppose that $\dim(V) = \dim(W) < \infty$. The following statements are equivalent.

- T is an isomorphism.
- T is invertible (i.e., T has an inverse).
- T is injective.
- T is surjective.

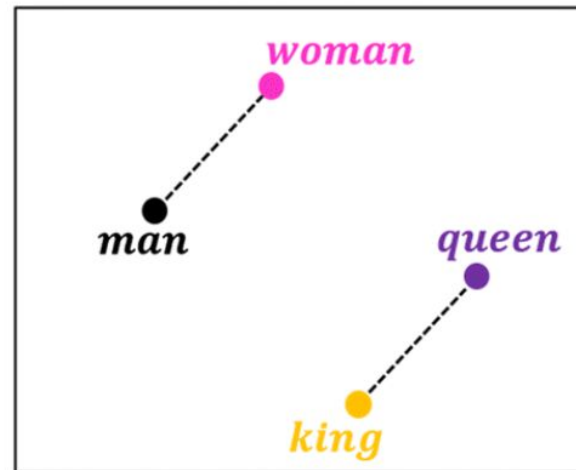
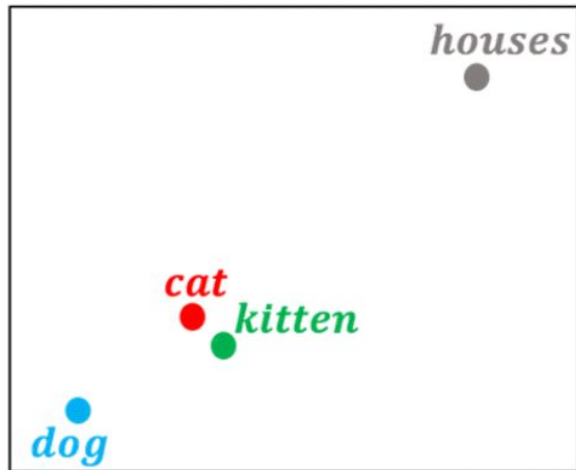
Remark: This theorem generalizes the *Fundamental Theorem of Invertible Matrices*. Indeed, if we take

$$V = W = \mathbb{R}^n \quad \text{and} \quad T = T_A,$$

where A is an $n \times n$ matrix, then we obtain the Fundamental Theorem.

Nearest neighbor graphs/analogy

- Two embedding spaces are nearest neighbor graph isomorphic if they satisfy the same nearest neighbor relationships.
- Two embedding spaces are graph isomorphic if they satisfy the same analogies.



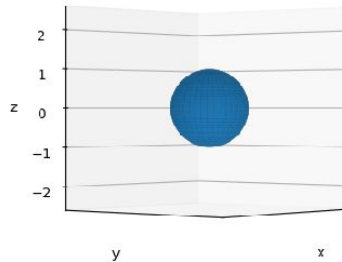
Epsilon isometry

Given a positive real number ε , an **ε -isometry** or **almost isometry** (also called a **Hausdorff approximation**) is a map $f: X \rightarrow Y$ such that

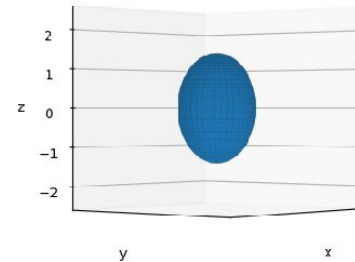
$$|d_Y(f(x), f(x')) - d_X(x, x')| < \varepsilon$$
$$d_Y(y, f(x)) < \varepsilon$$

That is, an ε -isometry preserves distances to within ε and leaves no element of the co-domain further than ε away from the image of an element of the domain.

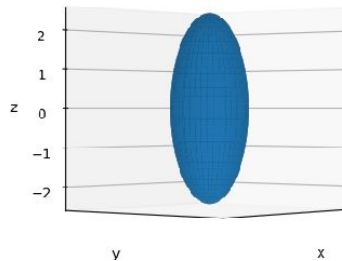
epsilon = 0.0



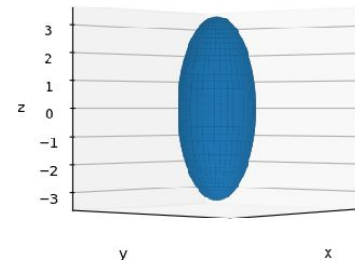
epsilon = 1.0



epsilon = 5.0

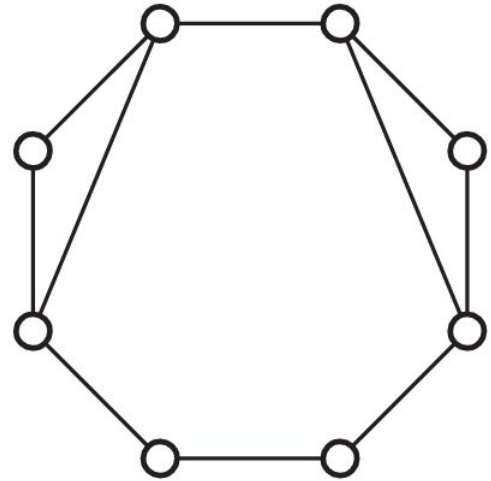
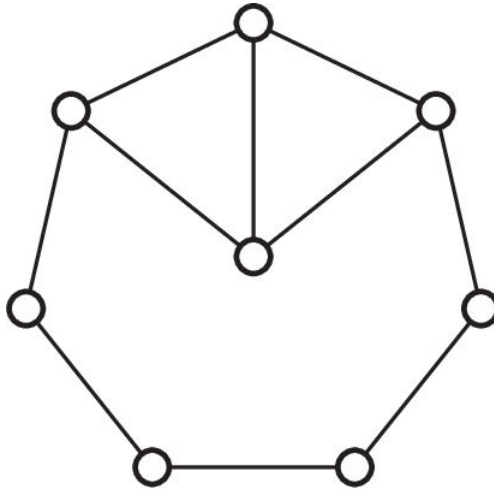


epsilon = 10.0



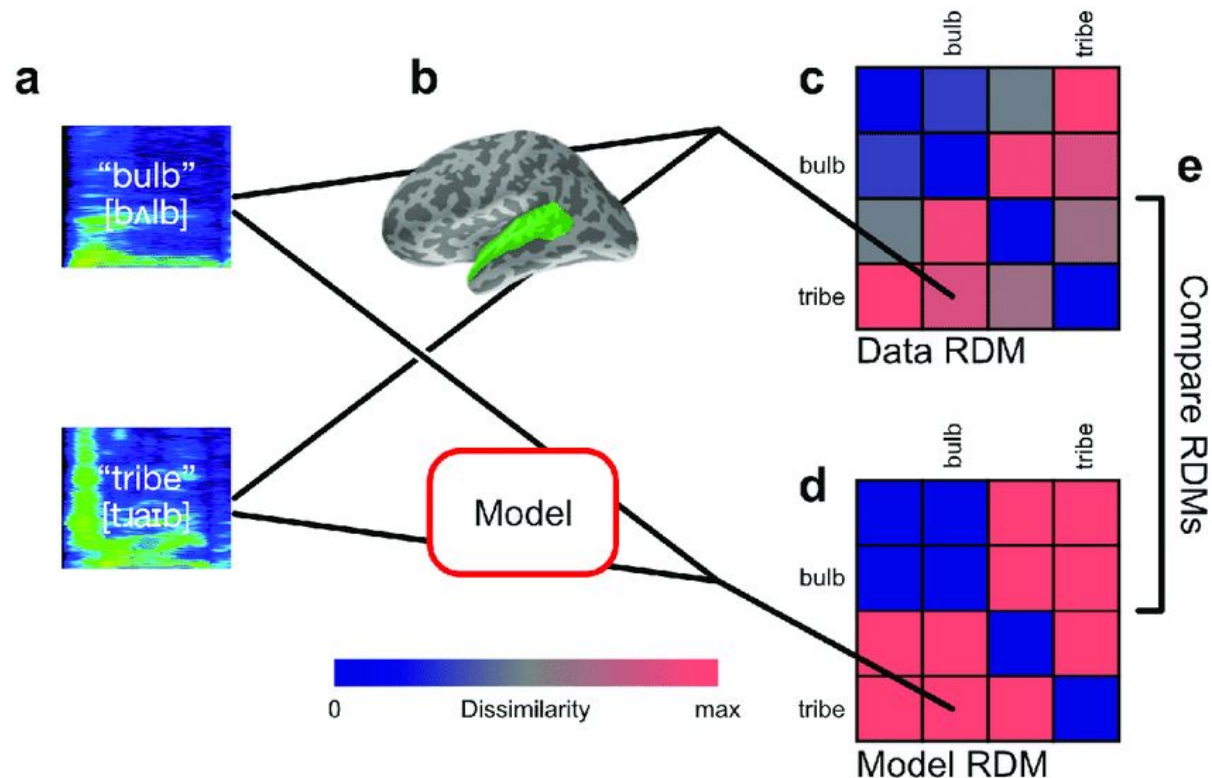
Isospectrality

Two graphs are called cospectral or isospectral if the adjacency matrices of the graphs are isospectral, that is, **if the adjacency matrices have equal multisets of eigenvalues.**



RSA

- Consider all pairs in a dataset, b and t .
- Obtain representations in two models, e.g., $\mathbf{v} = \text{vector}(b)$ and $\mathbf{w} = \text{vector}(t)$.
- Construct the representational dissimilarity matrix (RDM) for each model, in which $\text{distance}(\mathbf{v}, \mathbf{w})$ is a cell value.
- Compute the correlation (e.g., Spearman's rho) across the cell values of the two RDMs.



How to align

Exercise

Do you have any techniques in your toolbox for aligning vector spaces?

Hint: You can think of vector spaces as datasets, matrices, graphs, or metric spaces, as you see fit.

Two ways

Supervised

- Multinomial regression
- Autoencoding
- Procrustes alignment
- CCA

Unsupervised

- Vanilla GANs
 - Wasserstein GANs
 - Other variations of GANs
 - Point-set registration (ICP)
-

Supervised

Supervision

Supervision takes the form of a seed of paired vectors:

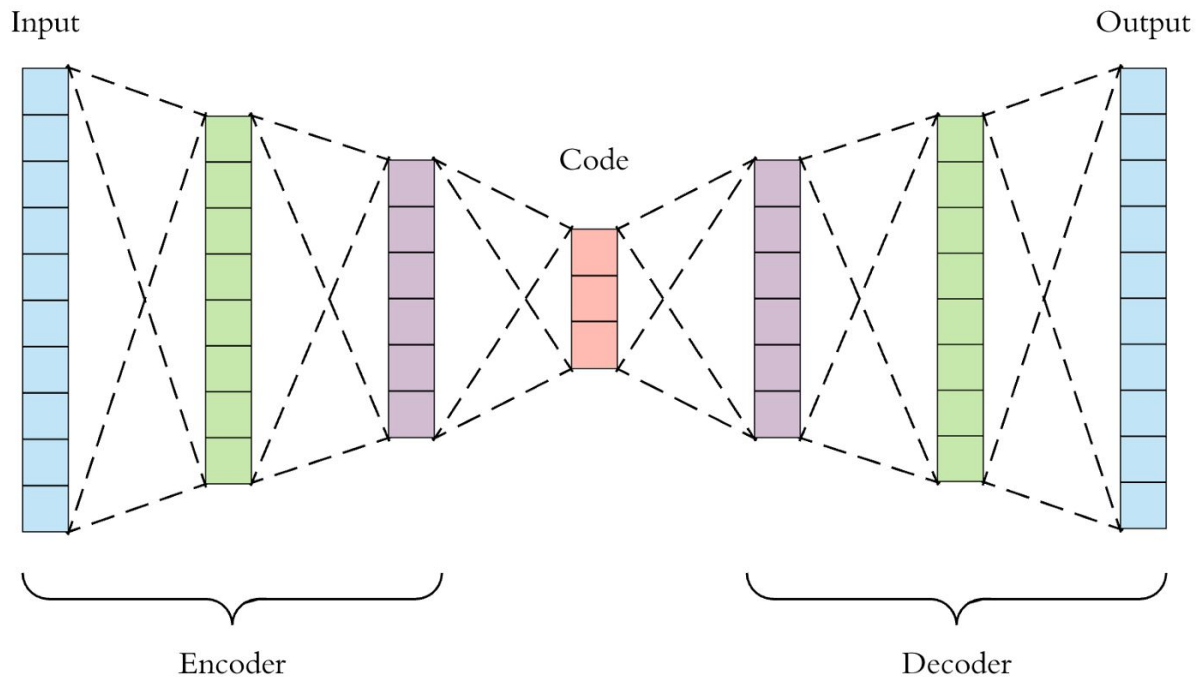
$$\mathbf{v}_S \sim \mathbf{v}_T$$

A simple regression model

For each vector \mathbf{v}_S in vector space \mathbf{S} , predict $\mathbf{v}_T[0]$ for the corresponding vector \mathbf{v}_T in vector space \mathbf{T} . For d -dimensional spaces, this amounts to training d (linear) regression models.

Autoencoder

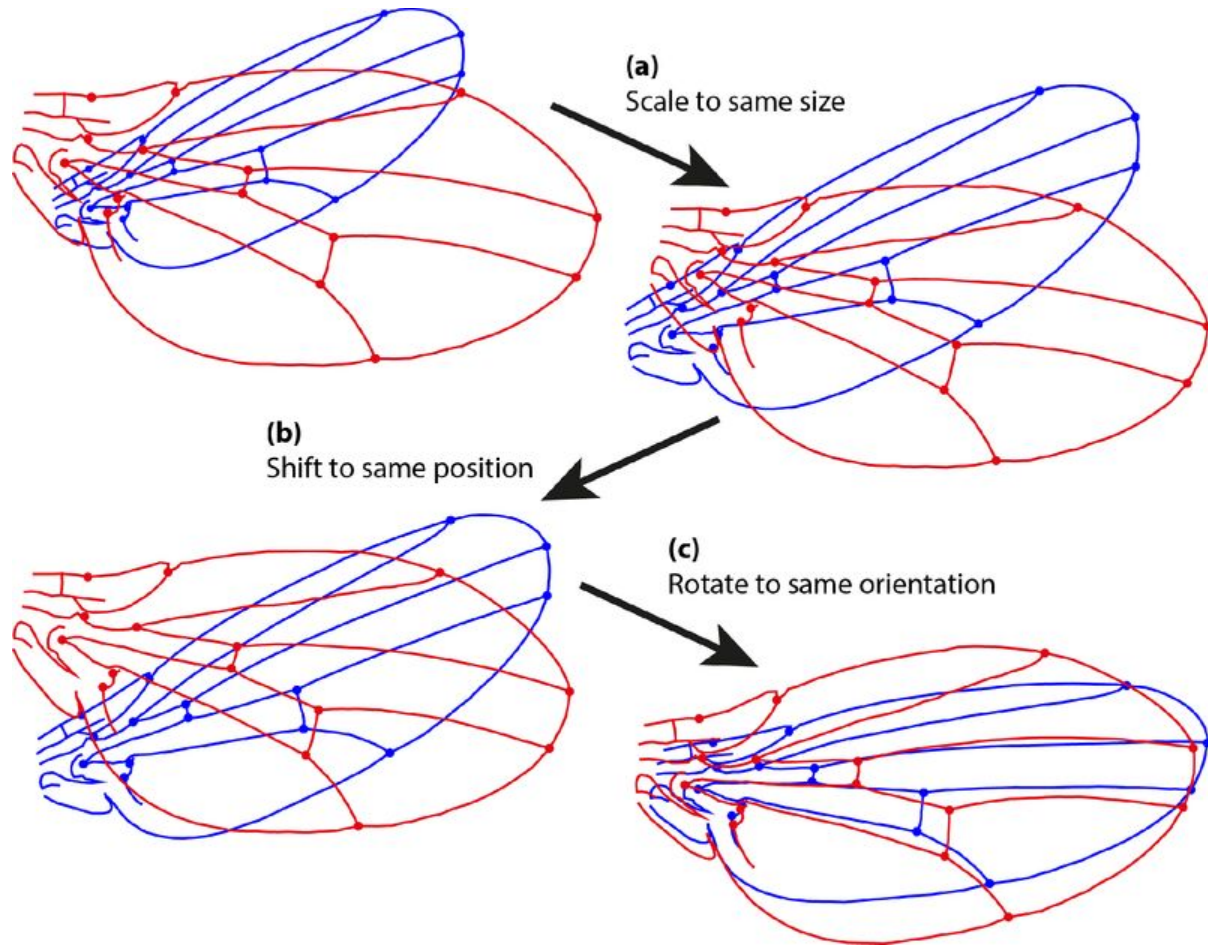
We can also use an autoencoder for the same purpose. For each seed vector pair, simply reconstruct one from the other. This learns a mapping from **S** into **T**.



Procrustes alignment

For two identically sized matrices \mathbf{M}_S and \mathbf{M}_T , we apply a transform to the other to minimize the sum of distances between the representations of our seed pairs.

Methods differ depending on what you take the transformation matrices to be, e.g., orthogonal, rotation, symmetric or permutation matrices.



CCA

Estimate a and b to minimize

$$\rho = \text{corr}(a^T X, b^T Y)$$

Note: CCA is symmetric. There's also a symmetric version in which you do two-sided Procrustes into the averaged space of \mathbf{S} (X) and \mathbf{T} (Y).

$$\left. \begin{array}{c} b_1 X_1 \\ + \\ b_2 X_2 \\ + \\ b_3 X_3 \\ + \\ b_4 X_4 \\ + \\ \vdots \\ + \\ b_p X_p \end{array} \right\} \begin{array}{l} \text{What linear} \\ \text{combinations} \\ \text{of the } X \\ \text{variables (u)} \\ \text{and the } Y \\ \text{variables (t)} \\ \text{will maximize} \\ \text{their} \\ \text{correlation?} \end{array} \left\{ \begin{array}{c} a_1 Y_1 \\ + \\ a_2 Y_2 \\ + \\ a_3 Y_3 \\ + \\ a_4 Y_4 \\ + \\ \vdots \\ + \\ a_q Y_q \end{array} \right.$$

$= \mathbf{u}$ $= \mathbf{t}$

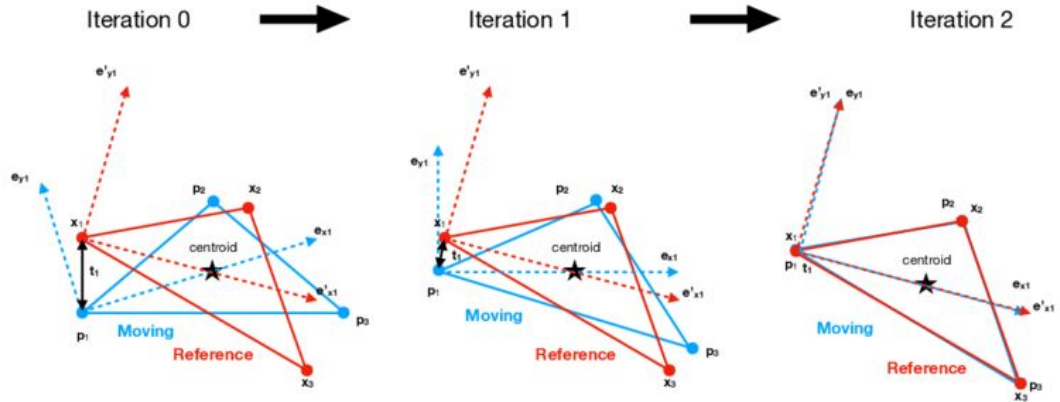
Unsupervised

Iterative Closest Point

For each point, match the closest point in the reference point cloud.

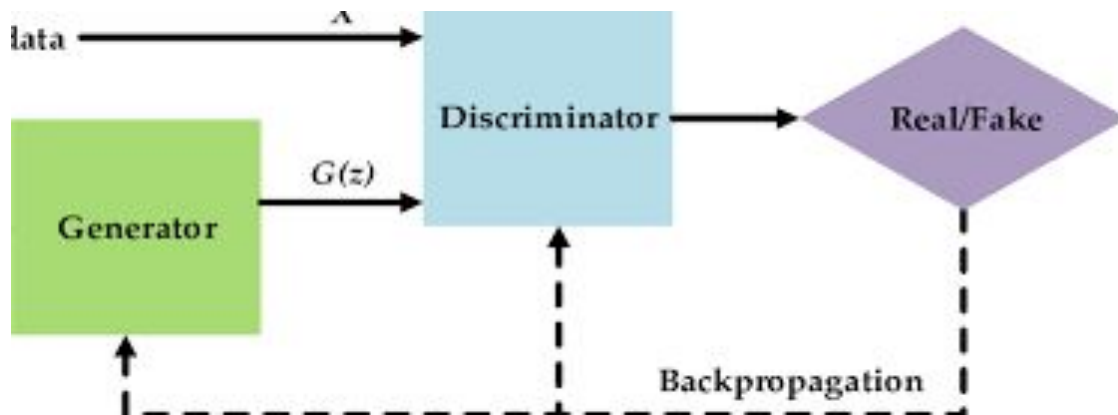
Estimate the rotation and translation matrix minimizing the pairwise distance.

Iterate (re-associate the points, etc).



Generative Adversarial Networks

Make vectors from S fake, vectors from T real. The Generator is now a linear projection.



Applications

fMRI analysis

The fMRI toolbox

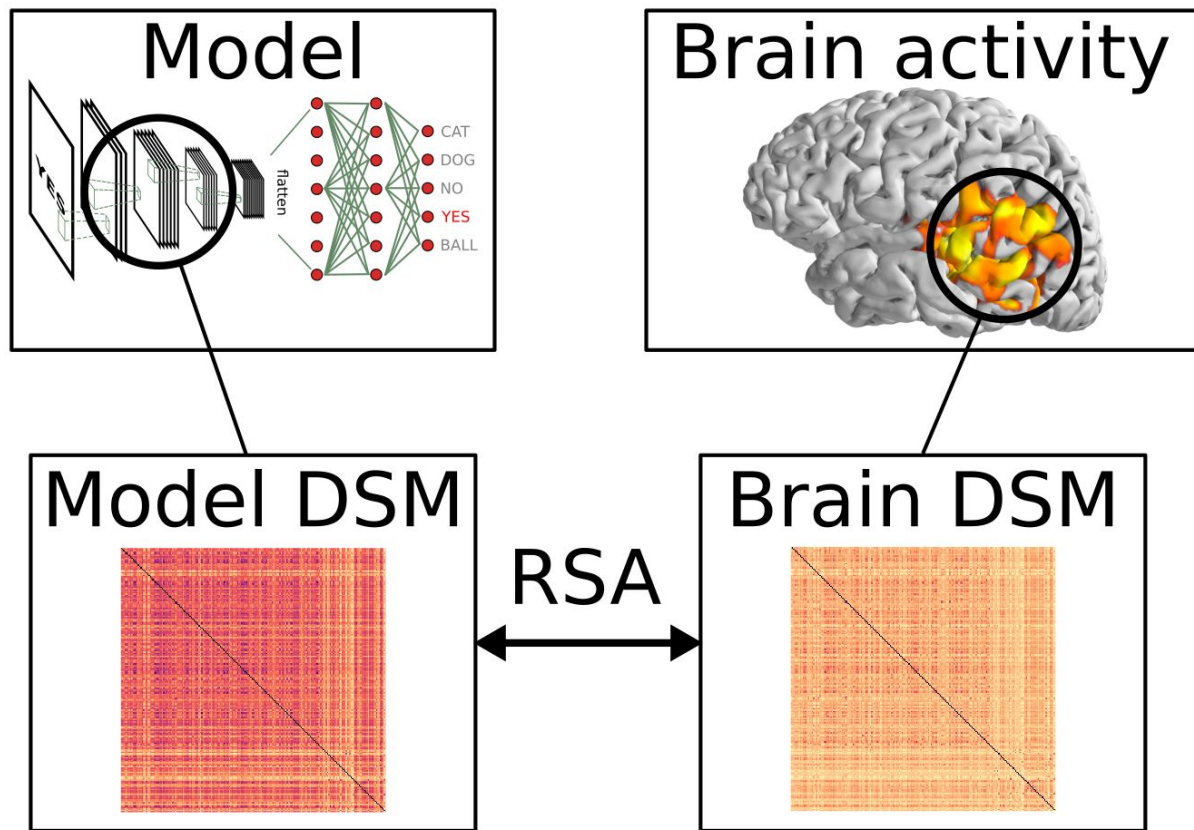
Isometry

- RSA to evaluate cognitive models

Alignment

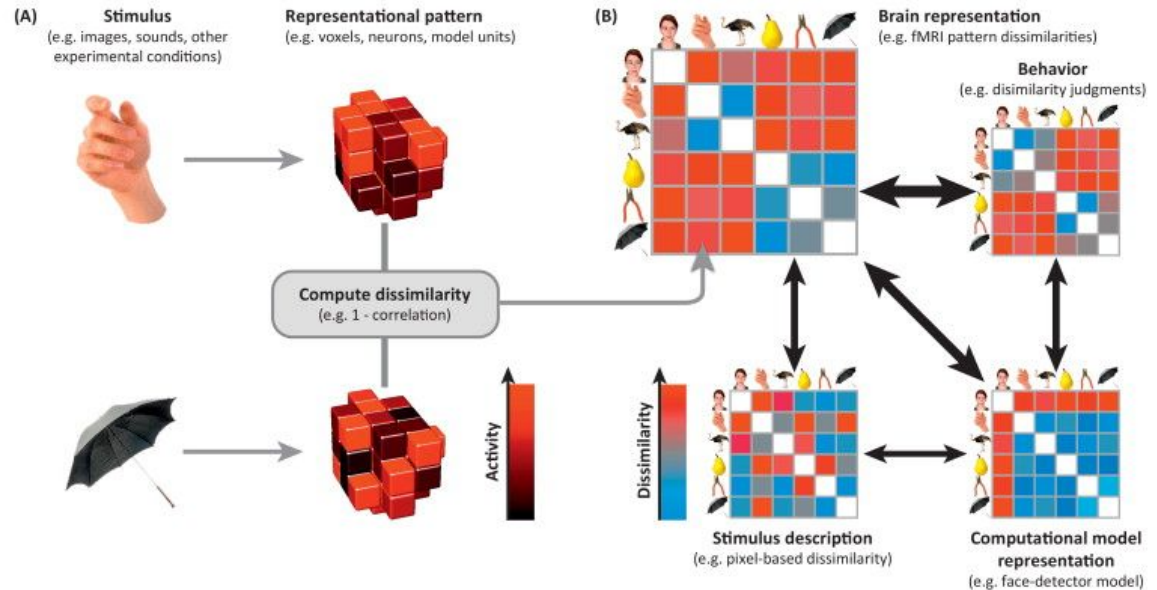
- Procrustes to align data from multiple subjects
 - CCA to align data from multiple subjects
-

CV and NLP models are used to decode brain images, but to probe the potential for such decoding, we want to quantify the structural similarity of model and brain vector spaces.

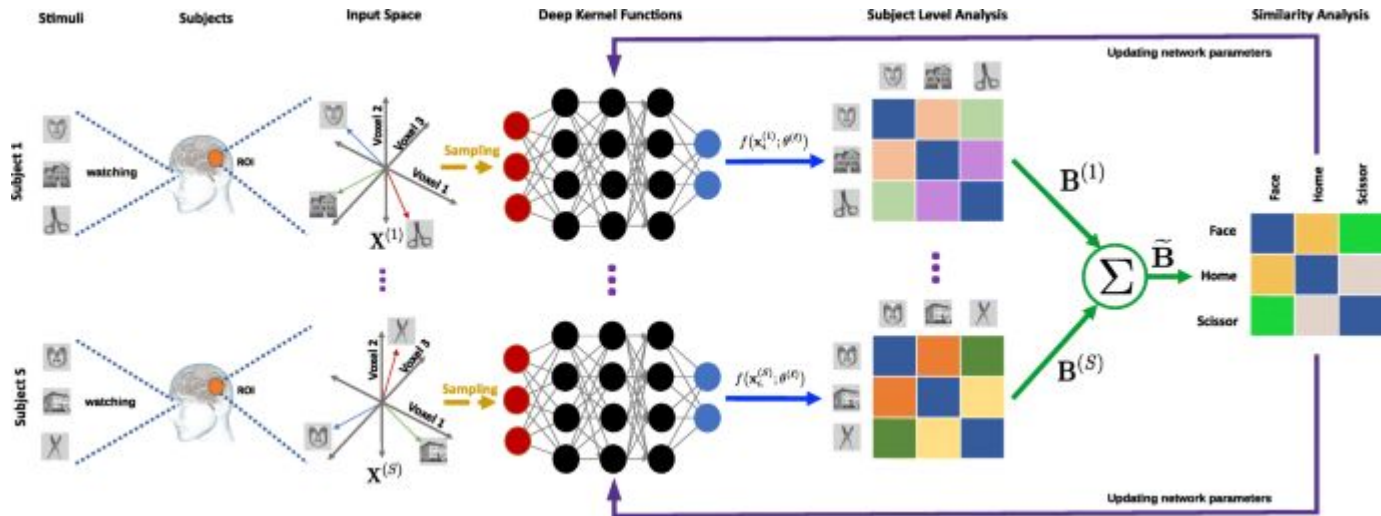


RSA workflow

- Consider voxel representations of say a hand and an umbrella.
- Compute $distance(\mathbf{v}=\text{vector}(h), \mathbf{w}=\text{vector}(u))$.
- Construct the representational dissimilarity matrix (RDM) for each model, in which $distance(\mathbf{v}, \mathbf{w})$ is a cell value.
- Construct your baseline RDM, e.g., images, model representations, other subjects.
- Compute the correlation (e.g., Spearman's rho) across the cell values of the two RDMs.



Deep RSA Learning



Cross-lingual

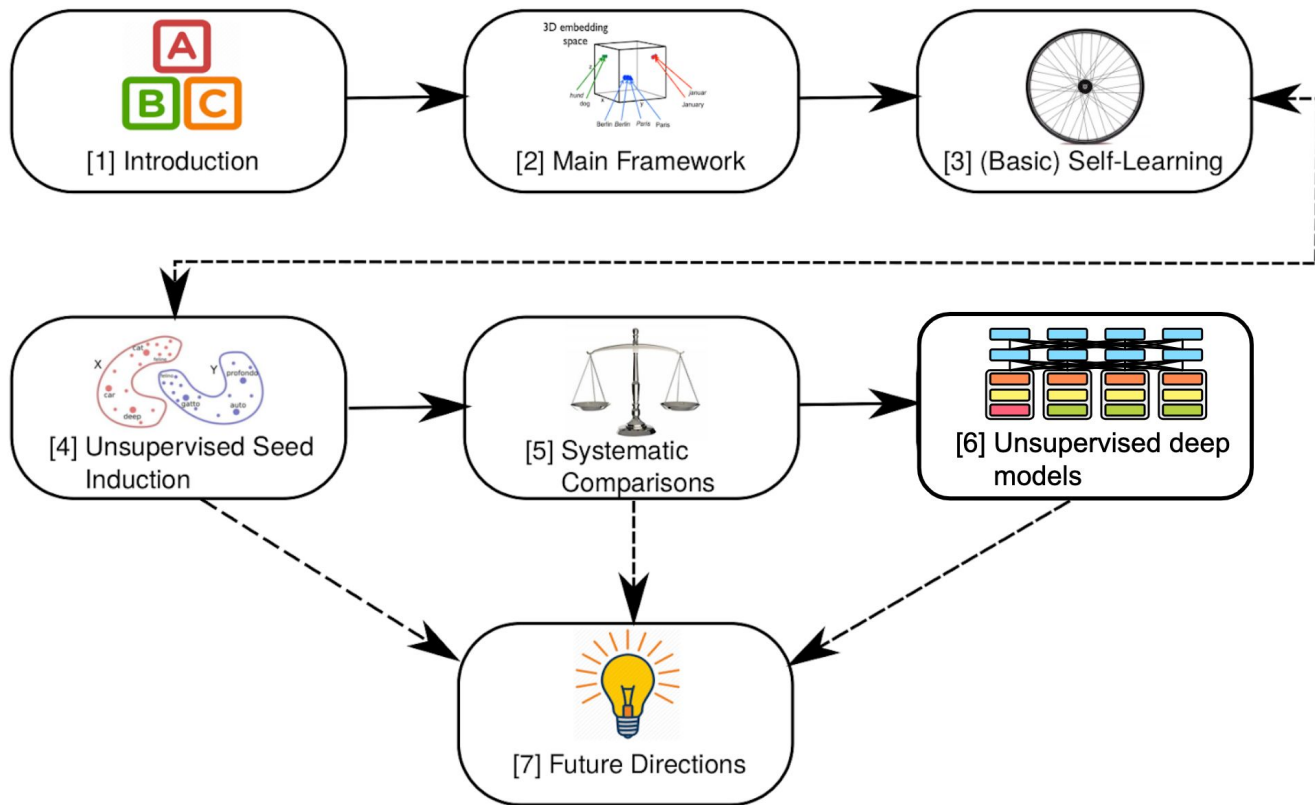
Two ways

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Unsupervised

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 - Wasserstein GANs
 - Other variations of GANs
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-



See our tutorial [here](#)

Multi-modal

Aligning text and image

If we align ResNet and GPT-J, for example, we get a $P@1=0.4$ with modest levels of supervision.

Applications

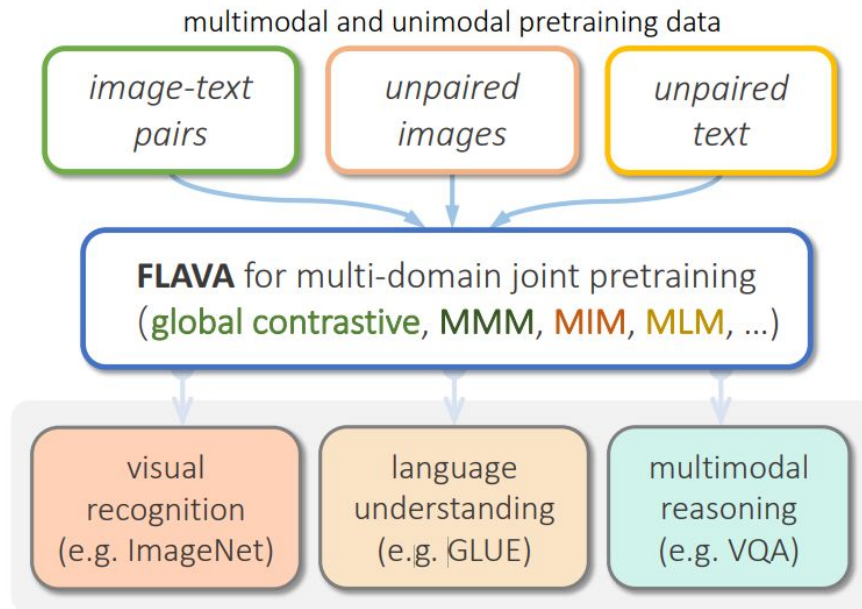
- Grounding
- Image captioning
- Visual question answering



How many slices of pizza are there?
Is this a vegetarian pizza?

FLAVA

FLAVA is a vision and language transformer by Facebook, presented at [CVPR 2022](#). FLAVA is jointly pretrained for vision, text and their alignment.



FLAVA

It does really well on both image, text, and multimodal tasks.

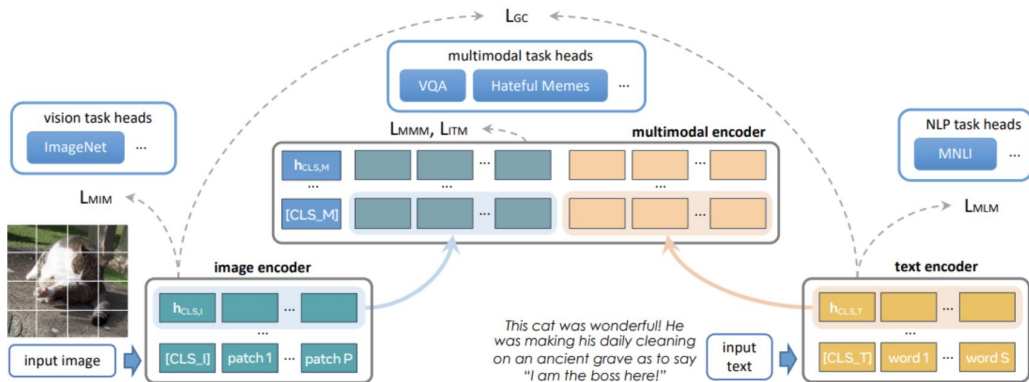
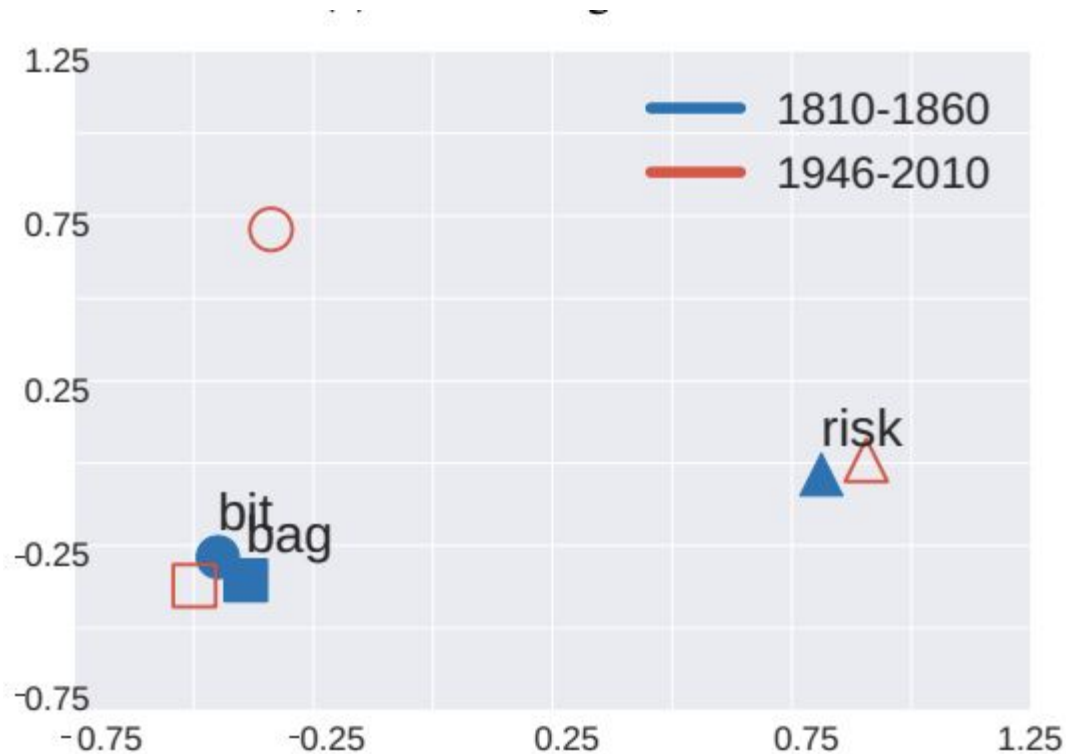


Figure 2. **An overview of our FLAVA model**, with an image encoder transformer to capture unimodal image representations, a text encoder transformer to process unimodal text information, and a multimodal encoder transformer that takes as input the encoded unimodal image and text and integrates their representations for multimodal reasoning. **During pretraining**, masked image modeling (MIM) and mask language modeling (MLM) losses are applied onto the image and text encoders over a single image or a text piece, respectively, while contrastive, masked multimodal modeling (MMM), and image-text matching (ITM) loss are used over paired image-text data. **For downstream tasks**, classification heads are applied on the outputs from the image, text, and multimodal encoders respectively for visual recognition, language understanding, and multimodal reasoning tasks.

Bias detection

Shift detection

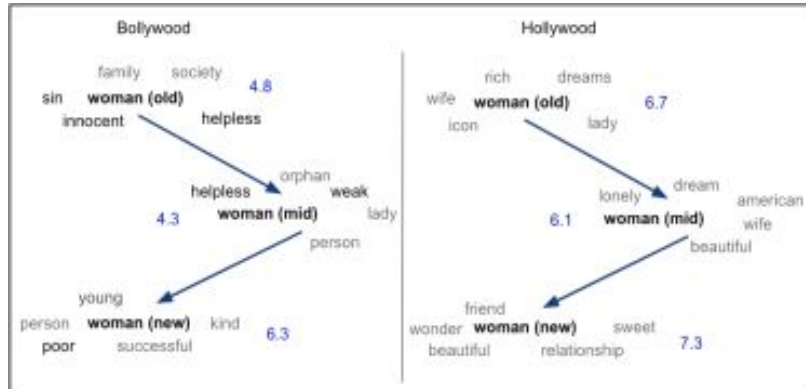
We can detect when some words have shifted meaning.



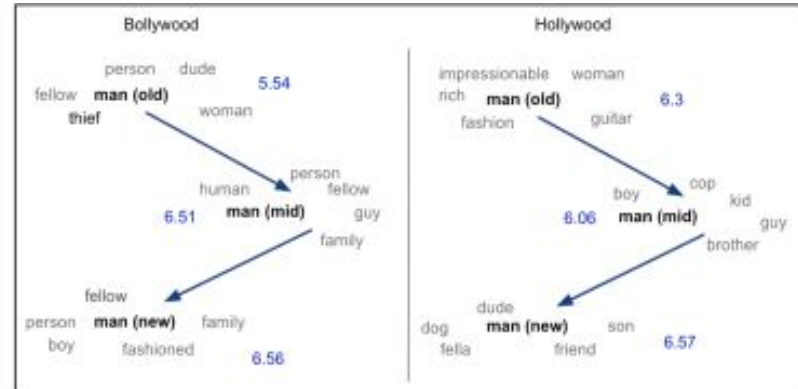
Exercise

How can you use what we have talked about today to detect bias?

Hint: In many ways.



A Woman over the years



B Man over the years

Shift detection in mentions of men and women in Bollywood/Hollywood