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Design, model and build a USAR robot platform

Mechatronic Project 478
Final Report

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Executive summary

Title of Project
Design, model and build a USAR robot platform
Objectives
Create a model to describe the kinematics of a Load Intuitive Module (LIM). Build a prototype Urban Search and Rescue (USAR) device which uses LIMs to climb stairs. Validate the model using the prototype.
What is current practice and what are its limitations?
The current practice for USAR platform ranges widely, but the most successful platforms use tracks with paddles for locomotion. These devices are effective but very expensive, so there is a need for low cost expendable USAR robots.
What is new in this project?
This project will introduce a model to describe a less expensive stair climbing robot platform using LIMs.
If the project is successful, how will it make a difference?
The model developed in this project can be used to inform future USAR designs.
What are the risks to the project being a success? Why is it expected to be successful?
The main risk to this project is that it does not build a working prototype in time. This risk will be mitigated through careful planning and consideration of previous pitfalls.
What contributions have/will other students made/make?
In 2013, Matthew Wilson developed the LIM system as a masters project at the University of Cape Town (UCT). Further development on the system was done in final year projects at UCT by students Jordan Haskel, Murray Buchanan, and Richard Daniel Powrie in 2017, 2018, and 2019 respectively.
Which aspects of the project will carry on after completion and why?
USAR devices using LIMs as a platform can be designed, built and tested.
What arrangements have been/will be made to expedite continuation?
All calculations, designs, and code will be made available to future students.

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Chapter 1

Literature review

1.1 USAR Robots

In both natural and man-made disasters, USAR operations are critical for reducing casualties. Robots can be deployed in USAR operations to compliment human and canine rescuers. Robots have the advantage of being able to be deployed in scenarios too small or too dangerous for humans, and aerial robots such as quadcopters are extremely effective at quickly mapping terrain and providing situational awareness to teams. Other emerging applications of USAR robotics is remote fire fighting, victim interaction and extraction (Delmerico *et al.*, 2019).



Figure 1.1: A tracked USAR robot, with paddles for obstacle climbing (Delmerico *et al.*, 2019)



Figure 1.2: ANYmal, a legged USAR robot (Delmerico *et al.*, 2019)

In order to perform USAR operations, robots need some form of locomotion. For ground robots, this typically involves either tracks, wheels, or legs. (Delmerico *et al.*, 2019). Tracked robots with actuated paddles for obstacle climbing, such as the one shown in Figure 1.1, have been found to perform extremely well. This is evident by their representation in the winners of the Robocup Rescue Robot League (RRL), an event in which teams compete to produce robots for versatile USAR operations (Sheh *et al.*, 2016). Wheeled robots are generally the simplest and easiest to repair, but can get stuck more easily in uneven terrain. Legged robots provide the advantage of not needing a continuous path, and rapid developments in optical sensors and control systems are enabling them to be even more viable, one of these robots is shown in Figure. Wheel-leg hybrid systems will use legged motion for navigating difficult

terrain, and wheels when on smooth ground (Delmerico *et al.*, 2019).

1.2 Load-Intuitive Modules

A Load-Intuitive Module (LIM) refers to a wheel system proposed by Matthew Wilson, shown in Figure 1.3 (Wilson, 2013). The LIM system uses a two outer "minor wheels" placed on a central hub that can be rotated as a "major wheel". The minor wheels are geared to the central hub such that they drive the vehicle, however if they experience high resistance, for example from hitting an obstacle, the torque will cause the major wheel to rotate instead, flipping one of the minor wheels over the obstacle to automatically climb it. The system is referred to as "Load-Intuitive" because it will intuitively climb over obstacles in response to increased load on the wheels. LIMs are designed to be used in low cost USAR robots, allowing them to climb over objects without the need for many actuators.

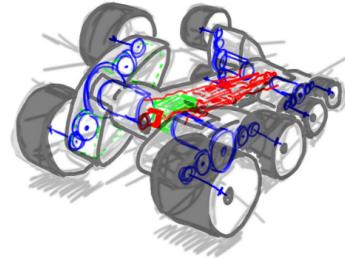


Figure 1.3: Systems layout of Wilson's LIM device (Wilson, 2013)

One advantage LIMs provide over existing locomotion methods is that they can climb obstacles higher than their profile, meaning they can enter low voids while rolling, and climb relatively tall obstacles by flipping over them. Another advantage is that LIMs require minimal actuation, one motor can be used to drive both the rolling and flipping motion, which will reduce costs when compared with other designs.

"LIMed" robot platforms (platforms using LIMs for locomotion) were built individually by four final year students at UCT (Wilson, 2013), (Haskel, 2017), (Buchanan, 2018), and (Powrie, 2019). These platforms show some success in climbing a single step, albeit inconsistently.

1.2.1 Wilson's LIM robot

Wilson designed and built the first LIM robot in 2013, shown in Figure 1.4. This robot was designed as a prototype for a low cost USAR star-climbing robot. At first Wilson considered only using LIMs for the front set of wheels, with the rear set using regular wheels. However, after performing a 2D simulation in Algodoor shown in 1.5, he concluded that using LIMs for the rear wheels was necessary as regular wheels provided little to no support to the climbing motion after the first step, presumably because the rear wheel would stop making contact with the stairs. Using LIMs for the rear wheels means they will be able to climb as well, and can always apply a forward force on the body.

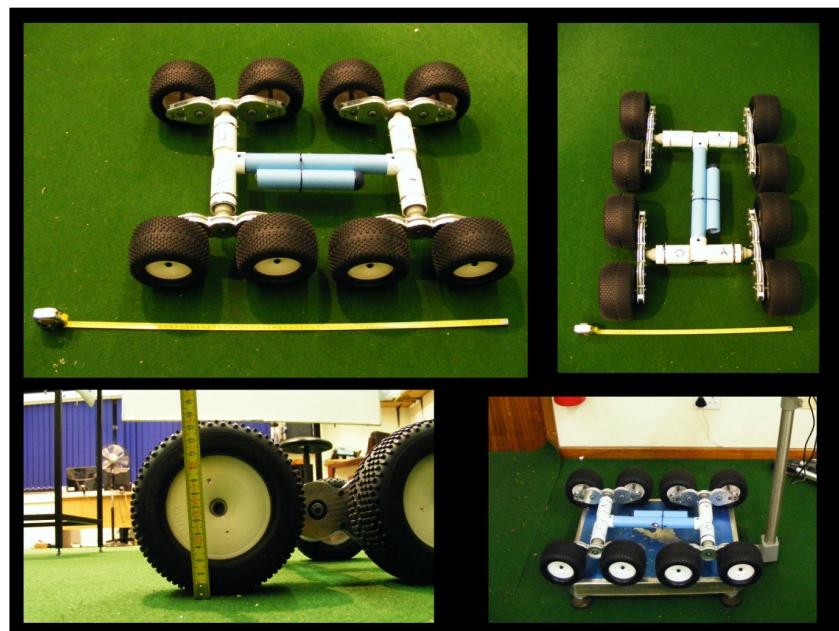


Figure 1.4: Wilson's Robot (Wilson, 2013)

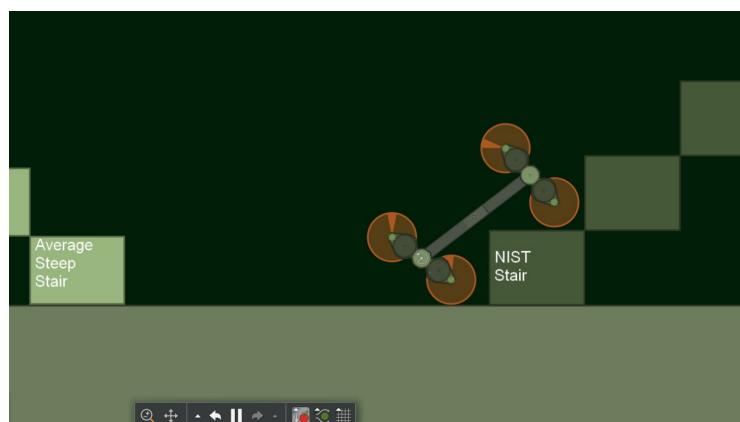


Figure 1.5: Wilson's Algodoor simulation of stair climbing (Wilson, 2013)

Wilson's robot had some limitations that prevented him from performing extensive tests. Chiefly, it was unable to climb stairs as the motors would stall upon encountering an obstacle. To validate the LIM concept in spite of this issue, Wilson split the robot in half and tested stair climbing using only the front LIMs and the chassis dragging behind as a tail. This "tail-dragging half assembly" was able to climb a single step as shown in Figure 1.6. Wilson's project ran out of time before he was able to solve the climbing motion of the complete robot, however he was able to confirm that the LIM system can climb at least a single stair in the half assembly configuration (Wilson, 2013).

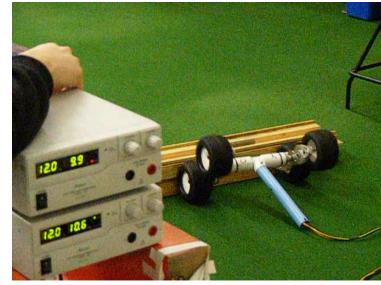


Figure 1.6: Wilson's half assembly climbing a stair (Wilson, 2013)

1.2.2 Haskel's Theseus

Haskel designed and built a LIMed robot to further test the concept, which he named "Theseus", shown in Figure 1.7. Unlike Wilson, Haskel assumes that using LIMs for rear wheels is not necessary for the stair climbing motion, and instead chooses to use a dragging tail to provide counter torque, similar to the tail-dragging half assembly used by Wilson. Theseus is much smaller and lighter than Wilson's robot.



Figure 1.7: Haskel's Theseus (Haskel, 2017)

Haskel tested different concepts for the tire tread, dragging tail, and gear ratios. However, none of his configurations could consistently climb a step. In the majority of step-climbing attempts, Theseus' LIMs would flip over to mount the step, but it would not be able to pull itself up. This can be attributed to a lack of grip or a lack of torque. Haskel intended to do further work on the project,

however he ran out of time due to component shortages and protests at UCT (Haskel, 2017).

1.2.3 Buchanan's Ascender

Buchanan designed and built "Ascender", a robot platform using LIMs for locomotion, shown in Figure 1.8. Buchanan iterated on the design several times in order to reduce mass and increase torque. The intention was build a drivetrain that could be combined with the electronics of Haskel's Theseus to produce a successful stair climbing robot. As such, the Ascender does not include any electronic control systems, and is instead controlled externally by power supplies connected to the motors.

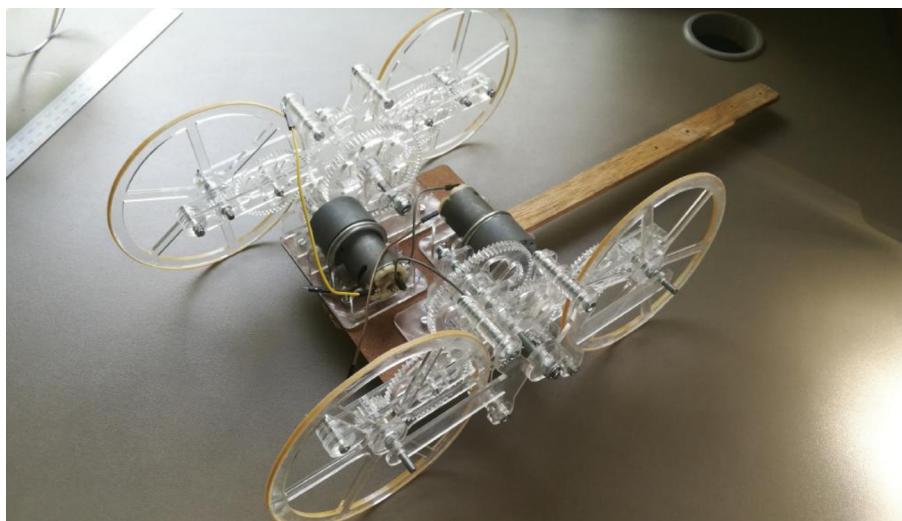


Figure 1.8: Buchanan's Ascender (Buchanan, 2018)

Buchanan's testing showed that the Ascender was able to climb a single step of 120 mm in 6 out of 10 attempts, and a step of 140mm in 2 out of 10 attempts. Buchanan noted a flaw in the design; after the LIMs flip over as part of the climbing motion, the body of the robot would lodge itself onto the the edge of the step and the wheels would spin freely, a phenomenon referred to as beaching. The LIMs would then spin until the top wheel makes contact with the top of the step, from there it would either grip and pull the robot up the step as intended, or it would dislodge the body and the robot would fall off the step. A successful climb is shown in Figure 1.9. Buchanan also reported that the Ascender was fragile to the point that it broke during the testing. Buchanan did not test the Ascender's ability to climb a staircase, but he concluded that it would be able to as a staircase is simply repeated single steps. (Buchanan, 2018)

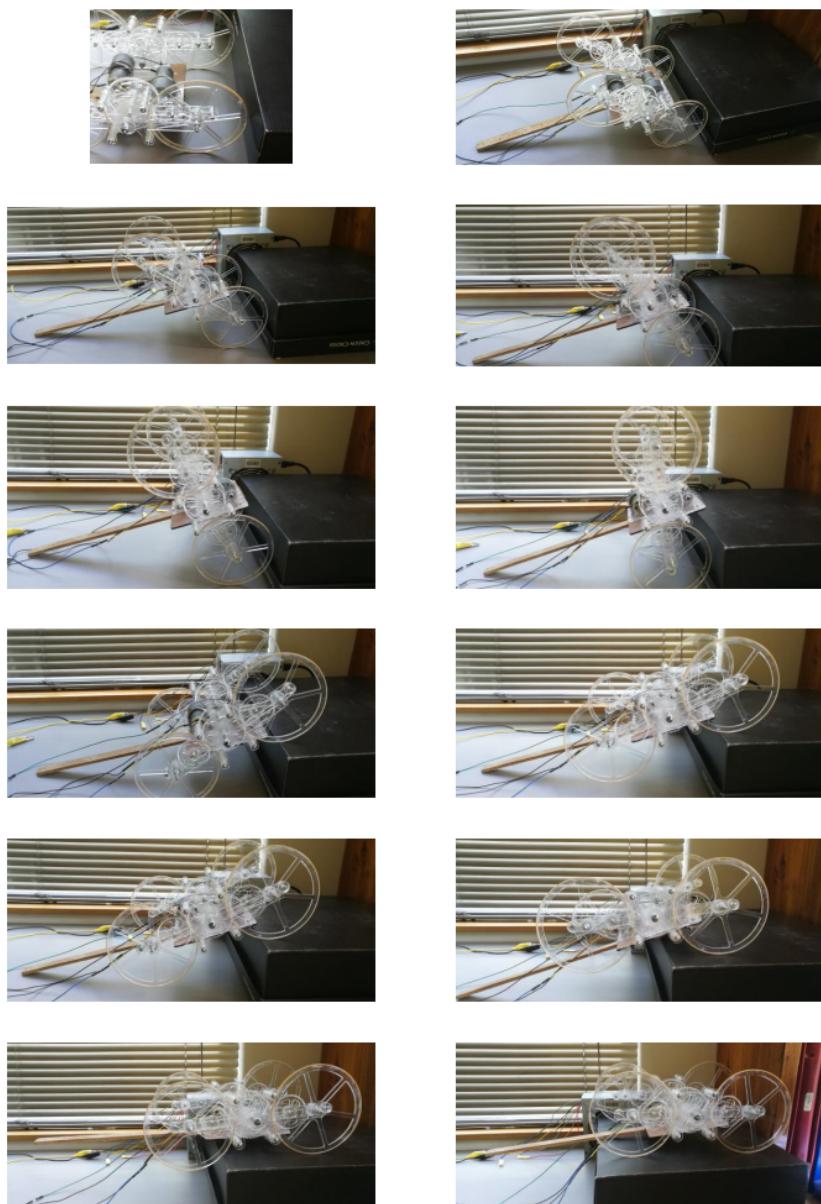


Figure 1.9: Buchanan's Ascender climbing a step (Buchanan, 2018)

1.2.4 Powrie's Di-Wheel robot

Powrie developed a robot using LIMs, however in his report he referred to LIMs as Di-Wheels. His reason for renaming them is that the behaviour of the LIMs does not only respond to external loads on the wheels, it also depends on the torque applied by the motors. He chose the name "Di-Wheel" in reference to a similar design by the name of "Tri-Wheel", which used three minor wheels instead of two, developed by Smith *et al.* (2015). Powrie's Di-Wheel robot is larger and more robust than Buchanan's Ascender, while being lighter than Wilson's LIMed robot. It is shown in Figure 1.10.

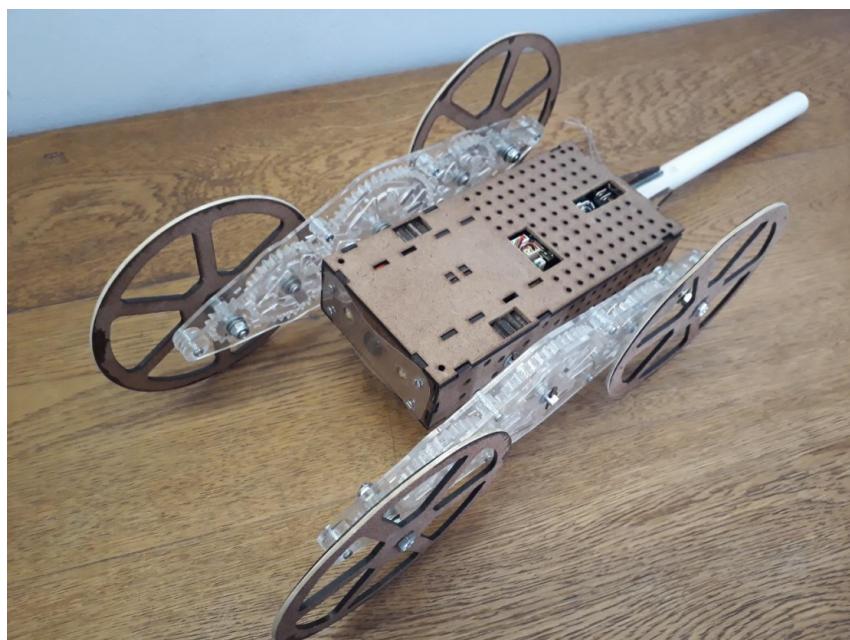


Figure 1.10: Powrie's Di-Wheel Robot (Powrie, 2019)

The Di-Wheel robot was successful in climbing a single step of 220 mm, shown in Figure 1.12. Further testing was not performed as noise from the robot's motors would interfere with the control system, preventing untethered driving. Powrie ran out of time before he was able to solve this issue. Powrie also found that when both motors are powered on, one of the LIMs would flip first, putting all the weight on the other LIM so preventing it from flipping. The result is that the robot would fall on its side, as seen in Figure 1.11 (Powrie, 2019).

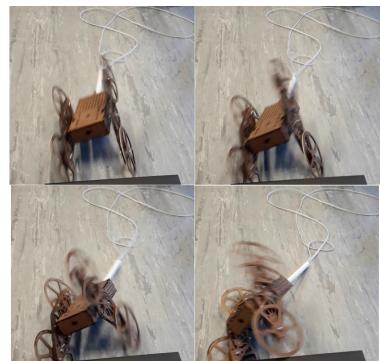


Figure 1.11: The Di-Wheel robot falling due to unsynchronised LIMs (Powrie, 2019)

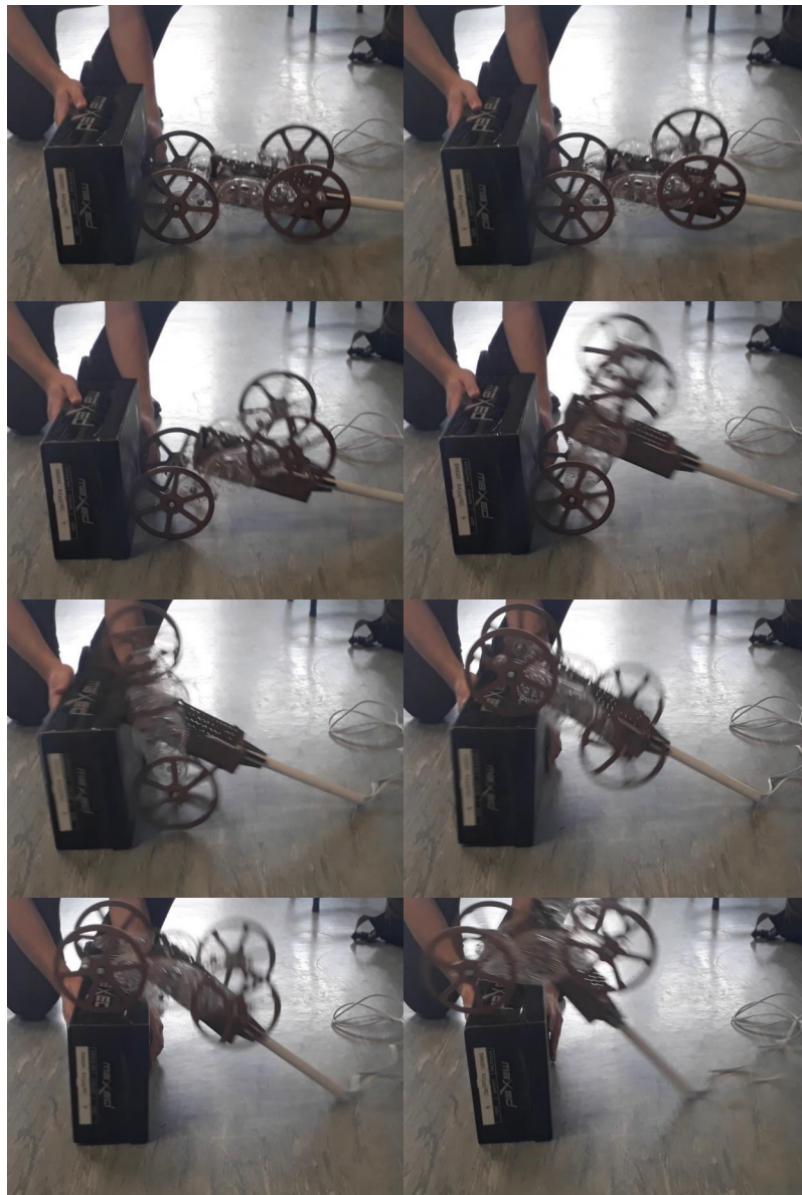


Figure 1.12: Powrie's Di-Wheel robot climbing a step (Powrie, 2019)

1.2.5 Gearing

The gear ratios of the LIMs will affect its motion significantly. The rotational speed of the central gear will be translated into both the speed of the LIM frame and the speed of the wheels:

$$\dot{\theta}_{central} = \dot{\theta}_{frame} + \frac{N_A}{N_C} \dot{\theta}_{wheel} \quad (1)$$

where $\dot{\theta}_{central}$ is the angular speed of the central gear, $\dot{\theta}_{frame}$ is the angular speed of the LIM frame, $\dot{\theta}_{wheel}$ is the angular speed of the outer wheels relative to the frame, N_A is the number of teeth on the outer gears, and N_C is the number of teeth on the central gear.

When both the wheels and the LIM frame aren't constrained, the system is under-actuated and its motion is non-trivial. However, when the LIM frame isn't flipping (i.e. normal driving on a flat plane), $\dot{\theta}_{frame} = 0$, therefore:

$$\dot{\theta}_{wheel} = \frac{N_C}{N_A} \dot{\theta}_{central} \quad (2)$$

When the wheels have encountered an obstacle, such as a step, friction will prevent them from turning, $\dot{\theta}_{wheel} + \dot{\theta}_{frame} = 0$. In this case:

$$\dot{\theta}_{frame} = \frac{\dot{\theta}_{central}}{(1 - \frac{N_A}{N_C})} \quad (3)$$

This means that during flipping motion, if $\frac{N_A}{N_C} > 1$, then the LIM frame will flip in the opposite direction to the rotation of the central gear, so the front wheel will roll up the side of the obstacle (Wilson, 2013). This is ineffective for climbing steps as the LIM will never mount the step, but rather continue rotating backwards until it returns to the starting position (Haskel, 2017).

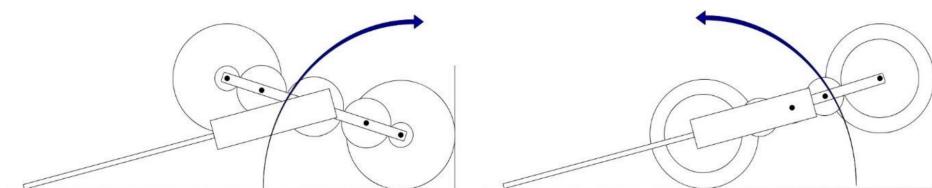


Figure 1.13: Two different climbing motions using different gear ratios (Powrie, 2019)

If $\frac{NA}{NC} < 1$, then the LIM frame will rotate forward, the rear wheel will flip over and mount the obstacle. This allows the LIM to climb stairs as intended. The two cases are shown in Figure 1.13, with the left showing the case when $\frac{NA}{NC} < 1$, and the right showing the case when $\frac{NA}{NC} > 1$.

1.2.6 Control requirements

LIMs are considered "Load intuitive" because of their ability to adapt to terrain mechanically. Open-loop control is ideal in this case, as an operator need only turn the motor on and the LIM will drive forward if it can, or attempt to climb an obstacle if it is obstructed (Wilson, 2013). However, Powrie found that his robot was not suited to open loop control. When full voltage is provided to the motor, the LIMs would flip even if when is on a flat plane. Powrie's calculations suggest that whether the LIM flips or not is largely dependent on the torque applied to it, a low torque results rolling, and a high torque results in flipping. His report suggests that LIMs only responds to terrain intuitively for a "medium torque" (Powrie, 2019). In this case a medium torque would be defined as a torque that results in rolling when the LIM is unobstructed, and flipping only when it is obstructed. This indicates that it may be necessary to have a control system that manages the torque provided to the LIMs to ensure that they do not flip on flat terrain if the motors are sufficiently powerful.

Powrie also found that when climbing a step, one LIM could flip first, putting weight on the other and preventing it from flipping, as seen previously in Figure 1.11 (Powrie, 2019). This suggest that a control system is needed to roughly synchronise the LIMs, if one is ahead of the other, more torque should be provided to the trailing LIM to correct its motion.

Chapter 2

2D simulation

In order to create an accurate model of the LIM system, it is important to understand how it functions. Previous reports have given some insight into this, but none of them have demonstrated a LIM robot that can climb consecutive steps. Wilson performed a simple simulation of a LIM robot in Algodoor, and concluded that the robot would need LIMs for the rear wheels in order to support consecutive stair climbing (Wilson, 2013), however all of the subsequent projects simply used a dragging tail instead of rear wheels. There is a need to resolve this inconsistency in past work, and to gain insight into the function of the LIM system. To do this, another 2D simulation using Algodoor is performed.

2.1 Limitations

Algodoor is a two dimensional physics sandbox (Gregorcic and Bodin, 2017). Initial testing with the software showed that limitations on the physics engine prevent accurate simulation of gears with teeth at a centimetre scale. This means it is impossible to accurately simulate a LIM device at the scale that they would be used in reality. The simulation can be scaled up to avoid this issue. However, this prevents an accurate simulation of the kinematics of the system.

Additionally, it was found that Algodoor does not allow for the accurate simulation of an electric motor. In a typical electric motor, the available torque will decrease as the speed increases. This nuance is not present in Algodoor, so it cannot be used to provide an accurate simulation of the motor requirements. Despite these limitations. Algodoor is still useful as a tool to roughly test the motion of LIMs, and to determine how it would interact with steps. The advantage of Algodoor over other simulation methods is its ease of use, it only takes a few minutes to build a LIMed robot in Algodoor.

2.2 Configuration

To improve the accuracy of the Algodoor physics engine, the simulation frequency is set to 1200 and all objects are scaled up 100 times. A basic LIM system with

a dragging tail is set up, using gear and wheel dimensions from Powrie (2019), shown in Figure 2.1.

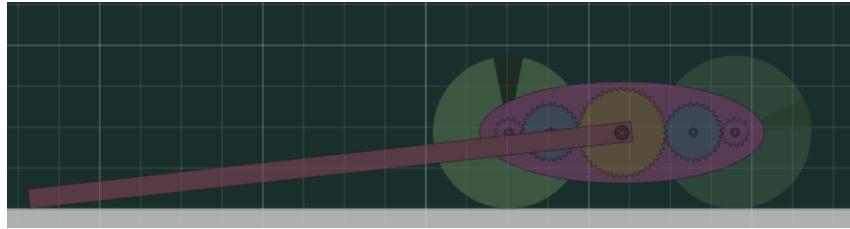


Figure 2.1: Initial Algodox LIM system

2.3 Observations

2.3.1 Rear wheels

Simulations suggest that rear wheels are not necessary for successful consecutive stair climbing. If the motor torque is sufficient, the LIM will be able to climb steps with only a dragging tail for counter torque. It should be noted that adding a motorised rear wheel, with or without LIMs, does provide a supporting force to the front LIMs during flipping motion, so if the frontal motor cannot provide sufficient torque, rear wheels should be considered in the design.

2.3.2 Mounting obstacles

There are three ways in which a LIM can mount an obstacle after flipping up to it. The first is that the wheel collides directly with the obstacle, shown in Figure 2.2. This happens when the obstacle is taller than a certain threshold based on the geometry of the LIM, and can result in the wheel bouncing off of the obstacle and failing to pull itself up. In this case a controller may be used to limit the speed of the flipping motion to ensure that the wheel is not going fast enough to bounce off the obstacle when it collides.

The second way is that the LIM frame collides with the obstacle and mounts it, then the LIM continues to rotate until the wheel makes contact with the surface of the obstacle to pull the robot forward. This case is shown in Figure 2.3. Note that the LIM frame can slip on the edge of the obstacle, which may result in failure to climb.

The third way is that the body of the robot, presented here as an extension of the tail, will mount the obstacle. This is shown in Figure 2.4. When the body has beached onto the obstacle, seen in Figure 2.4.2, there is nothing resisting the motion of either the wheels or the LIM, so they can accelerate quite quickly. If

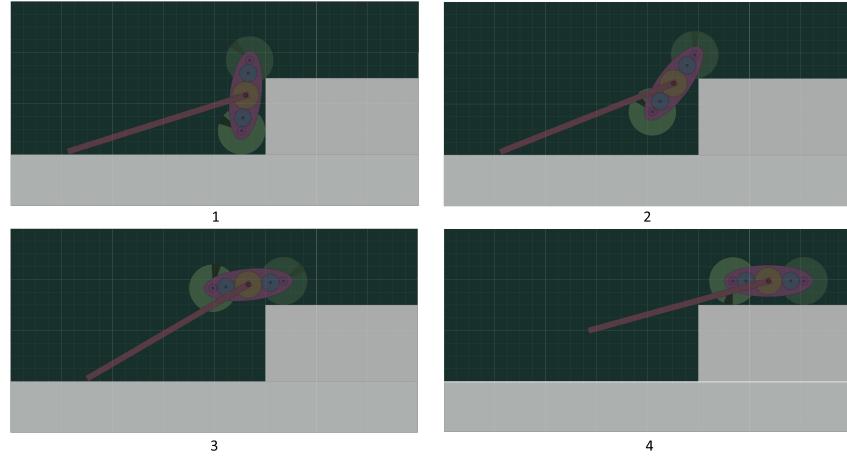


Figure 2.2: LIM climbing with wheel contact

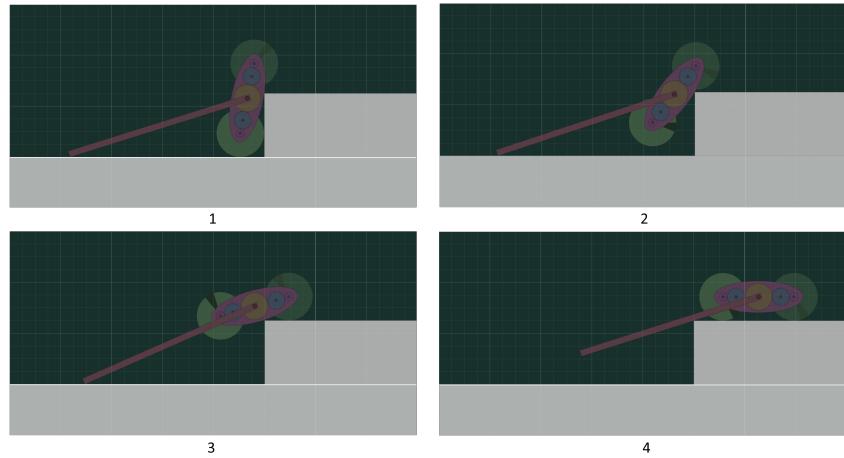


Figure 2.3: LIM climbing with LIM frame contact, note how the contact point slips between 1 and 2

they move too fast, the wheel can bounce off the obstacle when it makes contact, dislodging the body so that it falls back down to the initial position. Buchanan (2018) found that his Ascender followed this motion, which caused it to fail many of its climbing tests. He mentions that this can be avoided by moving the LIM axle to the end of the body, so that the body does not protrude beyond the LIM frame during climbing motion.

Each of these climbing methods has its flaws, however the case where the LIM frame collides with the obstacle is preferred as it reduces the chance that the wheel will bounce off the obstacle. To address slipping, grousers can be added to the robot's body (Robillard, 2019). The updated model with grousers can be seen in Figure 2.5.

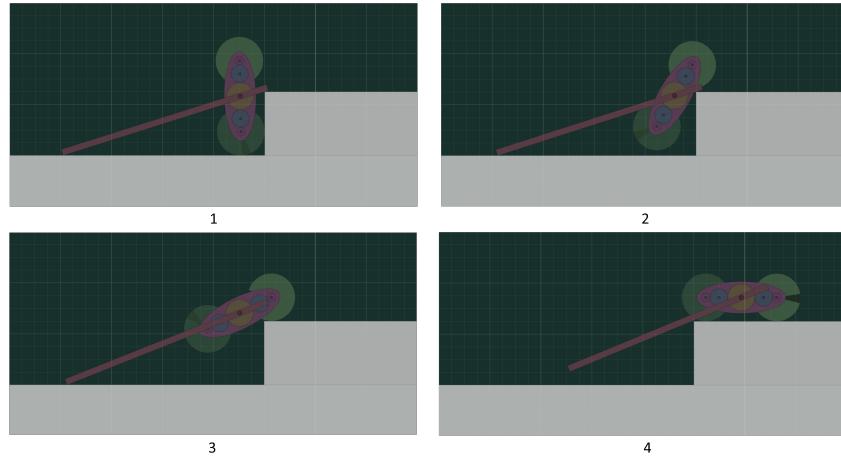


Figure 2.4: LIM climbing with robot body contact

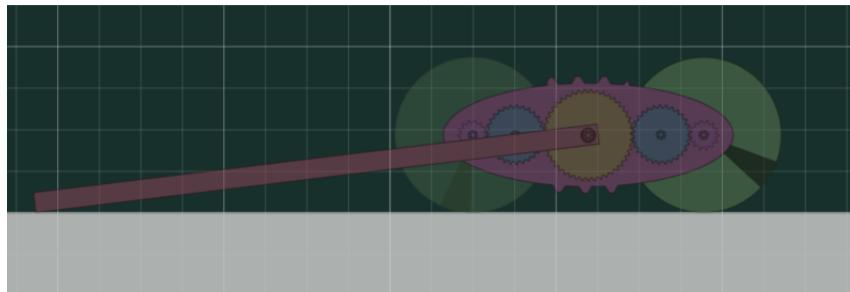


Figure 2.5: Algodoor LIM system with grousers on frame

2.3.3 Rolling and flipping

It was observed in simulation that the LIM would either roll or flip depending on the torque applied to it. There appeared to be a very small range of "medium torque" at which the LIM was truly load intuitive, if the motor torque was too weak it would never be able to flip over the obstacle and if it was too strong it would always flip and never roll, which hinders movement on flat terrain. However, this may simply be a result of inaccuracies of the simulation, as scaling and poor motor physics could significantly affect this motion.

In reality, as an electric motor increases in speed, the torque available will decrease proportionally. This means that once the LIM is rolling at speed, it will no longer have enough torque to flip itself unless it is stopped by an obstacle. This suggests that too much torque will only cause unintended flipping when the LIM is at rest on a flat plane.

Another observation made was that if the LIM rolls at speed into the obstacle, it will have to absorb all the energy of the impact. None of the translational kinetic energy of the robot is transformed into rotational kinetic energy of the LIM for flipping. This results in quite an inefficient system. One option to mitigate

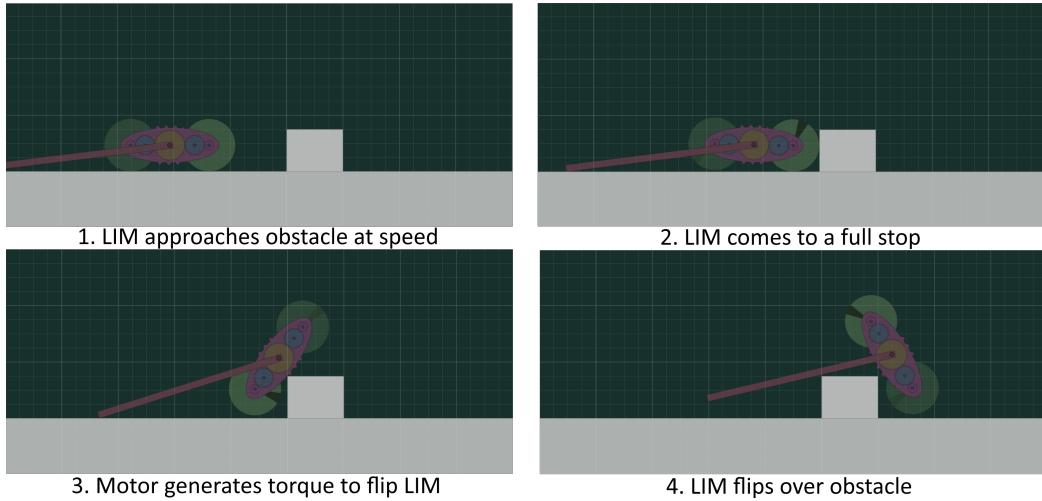


Figure 2.6: Algodoor LIM system approaching obstacle horizontally

this would be to implement a control system that solves the inverted pendulum problem in order to stand the LIMs upright on one wheel during normal operation. When the lower wheel encounters an obstacle while rolling, the LIM will readily flip over it without having to stop. The LIM could then switch to horizontal rolling when the robot needs a lower profile to enter a void. This solution would only be effective if a robust control system can be developed. These approaches are shown in Figures 2.6 and 2.7.

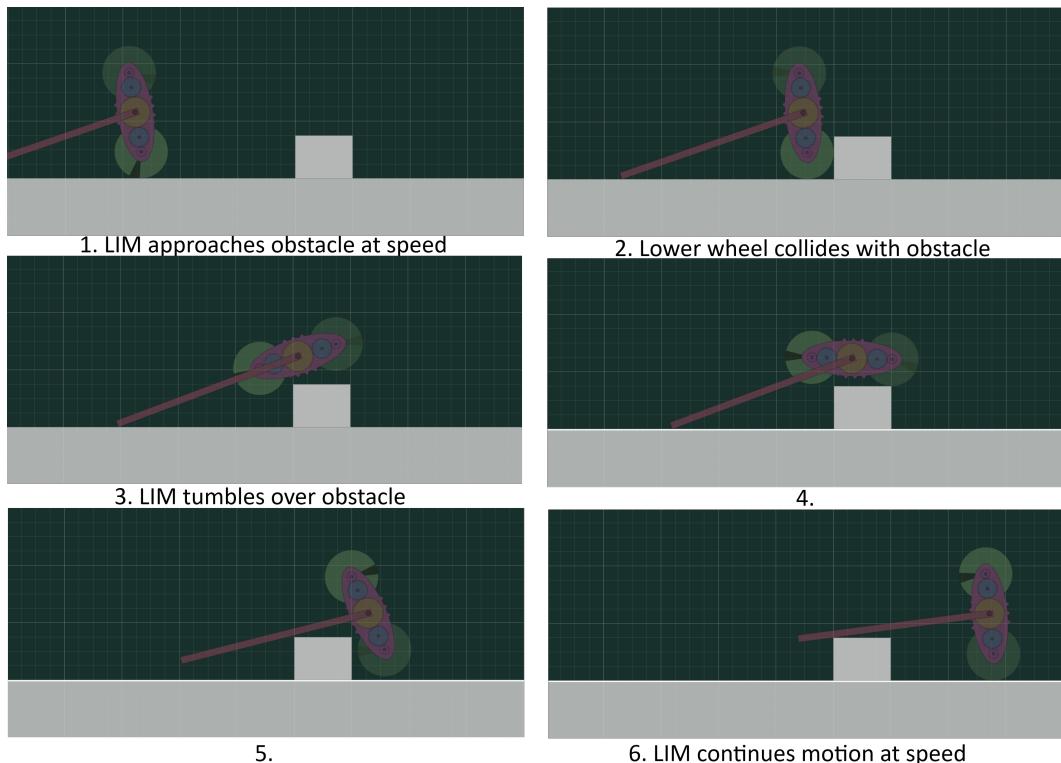


Figure 2.7: Algodoo LIM system approaching obstacle vertically

Chapter 3

Maths Model

3.1 Overview and objectives

This project develops a system of equations to analytically model the climbing motion of the device, which will be referred to as the, "Maths Model" henceforth. The intention behind this model is to allow designers to input parameters such as gear ratio, mass, wheel size, tail length, and motor torque, then determine whether the specified device will be able to climb steps. The equations can also be reversed to solve for specific parameters, such as the motor torque required to lift a device with certain properties. The maths model is developed using the MATLAB symbolic toolbox.

3.2 Definition of motions

As a LIMed device climbs, the tail and wheels come into contact with different surfaces on the stairs and ground, which changes how the device moves. The overall climbing motion is broken down into sequential stages which are modelled individually. These stages are defined as follows:

Stage 0: Rolling

When the LIMed device does is on a flat plane with no obstacle, it simply rolls forward. If the motor torque is high enough, the LIMs will flip even without an obstacle. However, DC motors lose torque as they gain speed, so the rolling motion prevents the motors from producing enough torque to flip the LIMs.

Stage 1: Lifting

When the front wheel of the LIM comes into contact with the first step, it is blocked by a step and fixed in place. The tail pushes against the ground and the

LIM starts rotating up the step. This motion ends when the LIM is vertical.

Stage 2: Flipping

Once the LIM is vertical, the bottom wheel starts to roll backwards as the top wheel falls forward onto the step. The distance that the bottom wheel rolls depends on the speed of the LIM and the height of the step. If the frame of the LIM hits the edge of the step, the device may slip backwards until the top wheel makes contact with the step. This motion ends when the top wheel is on the step.

Stage 3: Climbing

The front wheel rests on the step while the back wheel is on the ground. The tail pushes against the ground and the back wheel lifts while the front wheel simultaneously rolls forward on the step. This motion ends when the front wheel reaches the next step.

Stages 1 to 3 will repeat until the tail leaves the ground. After this point the tail will push against the edge of the previous steps.

Stage 4: Lifting from step

Similar to Stage 1, but the tail pushes against the edge of a the previous step, which now applies a force pulling the device backwards. Assuming friction on the wheel is sufficient, the LIM starts rotating up the step. This motion ends when the LIM is vertical.

Stage 5: Flipping from step

Similar to Stage 2, but the tail pushes against the edge of a the previous step, which now applies a force pulling the device backwards. This motion ends when the top wheel is on the step.

Stage 6: Climbing from step

Similar to Stage 3, but the tail pushes against the edge of a the previous step, which now applies a force pulling the device backwards. The back wheel lifts while the front wheel rolls forward on the step. This motion ends when the front wheel reaches the next step; however, due to the tail force pulling the device backwards, the back wheel will continue to lift past the horizontal while front

wheel rolls forward.

3.3 Core equations and assumptions

The maths model consists of a system of equations that are solved simultaneously. These equations are derived from the free body diagrams of each component, and only consider movement in two dimensions. The components in question are the LIM frame, the sun gear, the idler gears, and the planet gears including the shaft and the wheels, and the body of the device. These components make contact with the surroundings and the other components, which exert equal and opposite forces on each other. As the maths model only considers movement in two dimensions, the LIMs are assumed to move synchronously. To simplify the equations, only one LIM is modelled, and its mass and moment of inertia is doubled.

The free body diagrams for each component are shown in figure ???.

Each component is assigned a number, where the LIM frame is 1, the sun gear is 2, the idler gears are 3 and 4, the planet gears are 5 and 6, and the body of the device, including the tail, is 7. For example, the the sum of forces equations for the sun gear are,

$$m_2 \vec{a}_2 == \vec{w}_2 - \vec{f}_2 + \vec{g}\vec{f}_3 + \vec{g}\vec{f}_4 \quad (3.1)$$

Where m_x refers to the mass of component x , \vec{a}_x is the acceleration vector of component x , \vec{w}_x is the weight vector of component x , \vec{f}_x is the force vector that component x applies to component 1, and $\vec{g}\vec{f}_3$ and $\vec{g}\vec{f}_4$ are the force vectors that components 3 and 4 respectively apply to component 2 through the gears. This can be expanded to,

$$m_2 \begin{bmatrix} a_{21} \\ a_{22} \\ a_{23} \end{bmatrix} = \begin{bmatrix} w_{21} - f_{21} + gf_{31} + gf_{41} \\ w_{22} - f_{22} + gf_{32} + gf_{42} \\ w_{23} - f_{23} + gf_{33} + gf_{43} \end{bmatrix} \quad (3.2)$$

where vector positions 1, 2, and 3 denote the x, y, and z dimensions respectively. This equation can be further simplified by restraining movement to the x and y dimensions, and substituting $\vec{w}_2 = [0 \ m_2 g \ 0]'$,

$$m_2 \begin{bmatrix} a_{21} \\ a_{22} \end{bmatrix} = \begin{bmatrix} -f_{21} + gf_{31} + gf_{41} \\ m_2 g - f_{22} + gf_{32} + gf_{42} \end{bmatrix} \quad (3.3)$$

Similarly, the sum of moments equation for the sun gear is derived

$$I_2 \ddot{\theta}_2 == T - r_2 |g\vec{f}_3| + r_2 |g\vec{f}_3| \quad (3.4)$$

where I_2 is the moment of inertia of component 2, θ_2 is the angle of component 2, T is the moment exerted by the motor on component 2, and r_2 is the radius of component 2. Note that in this project, all angles and moments are given in the clockwise direction.

The full list of equations can be found in appendix ??? and in the matlab code.

3.4 Boundary conditions

Depending on the stage of the climbing, components of the device will come into contact with different parts of the steps and at different angles. To model climbing in each stage, a set of equations defining the contact is given for each stage.

Stage 1: Lifting

The front wheel, referred to as component 5, is locked in place by the reaction forces from the step, this leads to the condition,

$$\vec{a}_5 = \vec{0} \quad (3.5a)$$

$$\vec{v}_5 = \vec{0} \quad (3.5b)$$

$$\dot{\theta}_5 = 0 \quad (3.5c)$$

$$\ddot{\theta}_5 = 0 \quad (3.5d)$$

where \vec{v}_x refers to the velocity of component x .

The front wheel must be placed into a two dimensional coordinate system. In stage 1, the front wheel can be on the ground or on one of the steps, so long as the tail can reach the ground, and the front wheel will always be pressed against the edge of the next step. Placing the origin at the start of the steps as seen in Figure ???, the position of the wheel can be defined as,

$$\vec{s}_5 = \begin{bmatrix} \text{StepWidth} \cdot N - r_w \\ \text{StepHeight} \cdot N + r_w \\ 0 \end{bmatrix} \quad (3.6)$$

where \vec{s}_5 is the position vector of the centre of the front wheel, N is the number of the step on which the wheel is placed, with $N = 0$ placing the step on the ground, and r_w is the radius of the wheel.

The end of the tail pushes against the ground, which leads to the following

conditions,

$$s_{7end2} = 0 \quad (3.7a)$$

$$F_{react71} = -\mu_{tail} * F_{react72} \quad (3.7b)$$

$$\ddot{\theta}_7 = \frac{(|\vec{l}_7|^2 - l_{72}^2)a_{12} + l_{72}v_{12}^2}{|\vec{l}_7|^3(1 - \frac{l_{72}^2}{|\vec{l}_7|^2})^{3/2}} \quad (3.7c)$$

where s_{7end2} is the y position of the endpoint of the tail, $F_{react71}$ and $F_{react72}$ are the reaction forces exerted onto the tail by the ground in the x and y dimensions respectively, μ_{tail} is the coefficient of friction between the tail and the ground, \vec{l}_7 is the position of the end of the tail relative to the motor axle, and l_{72} is the component of \vec{l}_7 in the y dimension.

Equation 3.7c is derived from,

$$\theta_7(t) = \arcsin \frac{l_{72}(t)}{|\vec{l}_7|} \quad (3.8a)$$

$$\frac{d^2}{dt^2}\theta_7(t) = \frac{d^2}{dt^2} \arcsin \frac{l_{72}(t)}{|\vec{l}_7|} \quad (3.8b)$$

where θ_7 and l_{72} are treated as functions of time, t . This relation can be seen in figure ???. v_{12} and a_{12} refer to the velocity and acceleration of the motor axle in the y dimension, and are equivalent to \dot{l}_{72} and \ddot{l}_{72} respectively.

Stage 2: Flipping

Once the LIM is vertical, there is no longer a force pushing the bottom wheel forward into the step, instead it rolls backwards. This leads to a new condition,

$$\vec{a}_5 = \begin{bmatrix} \ddot{\theta}_5 r_w \\ 0 \\ 0 \end{bmatrix} \quad (3.9a)$$

$$\vec{v}_5 = \begin{bmatrix} \dot{\theta}_5 r_w \\ 0 \\ 0 \end{bmatrix} \quad (3.9b)$$

$$s_{51} = \theta_5 * r_w; \quad (3.9c)$$

$$M_{react5} = -F_{react51} * r_w; \quad (3.9d)$$

where M_{react5} is the reaction moment on wheel 5 as a result of the reaction forces. and the tail is still on the ground, so will still be subject to Equations 3.7.

Solving technique

Required torque

Required coefficient of friction

The device can climb up steps. In doing so, the wheels and tail make contact with different parts of the steps. In order to model the device, the overall movement is broken down into individual sequential motions.

The first motion is simple, the device rolls forward on a flat surface.

The second motion is referred to as climbing. The front wheel is blocked by a step and fixed in place. The tail pushes against the ground and the LIM starts rotating up the step. This motion ends when the LIM is vertical.

In the third motion, the top wheel falls forward onto the step and the bottom wheel rolls backwards until the top wheel lands. The distance that it rolls depends on the speed of the LIM and the height of the step. If the frame of the LIM hits the edge of the step, the device may slip backwards until the top wheel makes contact with the step. This motion ends when the top wheel is on the step.

In the fourth motion, the device pulls itself up the steps. The front wheel rests on the step while the back wheel is on the ground. The tail pushes against the ground and the bottom wheel lifts while the front wheel simultaneously rolls forward on the step. This motion ends when the top wheel reaches the next step. The fifth motion is similar to the second motion, with the exception that the tail is angled further down to reach the ground.

The sixth motion is similar to the third motion, with the exception that the tail is angled further down to reach the ground.

The seventh motion deviates significantly from the previous motions. The front wheel starts on the next step while the bottom wheel starts on the previous step. The tail now contacts the edge of the previous step rather than the ground, which causes a significant force to pull the LIMs backwards. Because of this, unlike in the fourth motion, the front wheel will not initially roll forward on the next step. The back wheel will lift from below until it is at a certain angle above the front wheel, at which point the front wheel will start to roll forward, bringing it to the base of the next step.

The eighth motion is similar to the second motion, except the tail pushes against the edge of the previous step and the back wheel is already partially lifted. The back wheel then lifts up further until the LIM is vertical.

The ninth motion is similar to the sixth motion, except the tail pushes against the surface of the previous step instead of the ground.

Chapter 4

Design Requirements

The objective of the design phase is to design a LIMed platform that can be used to validate the mathematical model. The requirements for this design are documented in this section.

4.1 Stakeholder requirements

This project is done at the request of Justin Pead, who supervised previous LIM projects at UCT. For the purposes of this section, this project's supervisor, Mr. Wayne Swart, acts as an intermediary between the stakeholder and the designer.

Table 4.1: Stakeholder Requirements

Number	Stakeholder	Description	Priority
SR1	Justin Pead	The device must be able to climb stairs	High
SR2	Justin Pead	The device must roll on its wheels when it is not obstructed, and climb over obstacles when it is obstructed.	High
SR3	Justin Pead	The device must use LIMs for locomotion	Must-have
SR4	Justin Pead	The device should be described by the model	Must have
SR5	Justin Pead	The device should be relevant to USAR applications	High
SR6	Wayne Swart	The design and construction of the device must demonstrate the relevant graduate attributes	Must have
SR7	Wayne Swart	The budget for the project is R5000	Must have

4.2 Engineering Requirements

In this section, the stakeholder requirements (SRs) are expressed as functional requirements (FRs) and performance requirements (PRs). FRs describe the actions that the system must perform, while PRs are measures of how well the system performs the functions.

Table 4.2: Functional Requirements

Number	Description	Relevant Stakeholder Requirement
FR1	Climb obstacles	SR1, SR2
FR2	Roll	SR2
FR3	Accept user control	SR5

Table 4.3: Performance Requirements

Number	Description	Target	Range	Unit	Relevant Stakeholder Requirement
PR1	Height of obstacles that can be climbed	Maximise	200+ ¹	mm	SR1, SR2
PR2	Climbing success rate	Maximise	90 - 100	%	SR1, SR2
PR3	Top speed	Maximise	1+	m/s	SR2
PR4	Acceleration	Maximise	1+	m/s ²	SR2
PR5	Height Clearance	Minimise	50 - 300	mm	SR5
PR6	Cost	Minimise	0 - 5000	ZAR	SR6

¹Maximum step rise specified by the SANS10400 building regulation (SAN, 2010)

Chapter 5

Design

Overview and objectives

Selection of design parameters - Powrie's device

Motor selection

Housing design

Control circuits and code

Chapter 6

Drake Simulation

Overview and objectives

Selection of simulator

CAD to simulation pipeline

Notes on friction

Chapter 7

Experiment

Overview and objectives
Voltage-torque calibration
Motions
Results

In order to validate that the model is accurate for each motion, the torque that causes the device to perform each motion determined experimentally. The equivalent values produced by can be compared with the measured torques to validate the model quantitatively. However, the torque produced by a DC motor cannot be measured or set directly. Instead, The voltage across the motor is varied. The torque of a DC motor is proportional to the current running through it, and the stalling torque is proportional to the voltage. To characterise the motors, an experiment was set up to determine the stalling torque produced at different input voltages.

A lever was placed on the output shaft of the motor gearbox, and a mass was attached to the end of the lever. The voltage of the motor was varied and the distance that it lifts the weight was recorded at each voltage.

Experiment:

Independent variable:

- Motor voltage (V)

Dependent variable:

- Distance the weight is lifted (mm)

Controlled variables:

- Motor used
- Lever used
- Power supply used
- Multimeter used
- Ruler used

Now that the relation between motor voltage and stalling torque has been calculated, the torque required to perform each motion

Chapter 8

Analysis

Overview and objectives

Quantitative comparison

Qualitative comparison

Assessment of error

Chapter 9

Recommendations

Recommendation fro future work
Recommendation for design of LIMs

Chapter 10

Design- 1st iteration

Starting with Powrie's device as it is the most developed of the previous projects. Attempted to use mathematical model to identify potential improvements, however I struggled to get objective improvements, increasing one parameter often may improve the ability to flip but hinder the ability to climb overall, and removing material should only be done if it has minimal effect on structure strength, something that would take much time to determine (possibly with FEM?). Such optimisations are beyond the scope of the project, I'm not trying to create a perfectly optimised device, I'm trying to create a working device so I can describe its function. Powrie's device is working to some extent, so the first design iteration should deviate minimally from his design.

Powrie's design for the LIMs is copied as accurately as possible, could possibly even use his laser cutting templates to manufacture. Fortunately he provides a detailed builder's guide, allowing me to design and build ASAP so I can focus on the math model. The robot body is changed significantly. Powrie uses external gears on an already geared motor, this is unnecessary, as geared motors come in a variety of ratios. I use a JGY-370 motor, as I believe the worm gearbox is well suited to this purpose, it allows me to make a thinner body that doesn't protrude as far forward beyond the axle. The tail is designed based on Powrie's concepts. The motors selected produce more torque than the ones Powrie selected, even with his additional gearing, so they should be up to the task. Later iterations could combine the worm gearbox with even more powerful brushless motors.

Chapter 11

Description of motion

The device can climb up steps. In doing so, the wheels and tail make contact with different parts of the steps. In order to model the device, the overall movement is broken down into individual sequential motions.

The first motion is simple, the device rolls forward on a flat surface.

The second motion is referred to as climbing. The front wheel is blocked by a step and fixed in place. The tail pushes against the ground and the LIM starts rotating up the step. This motion ends when the LIM is vertical.

In the third motion, the top wheel falls forward onto the step and the bottom wheel rolls backwards until the top wheel lands. The distance that it rolls depends on the speed of the LIM and the height of the step. If the frame of the LIM hits the edge of the step, the device may slip backwards until the top wheel makes contact with the step. This motion ends when the top wheel is on the step.

In the fourth motion, the device pulls itself up the steps. The front wheel rests on the step while the back wheel is on the ground. The tail pushes against the ground and the bottom wheel lifts while the front wheel simultaneously rolls forward on the step. This motion ends when the top wheel reaches the next step. The fifth motion is similar to the second motion, with the exception that the tail is angled further down to reach the ground.

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The seventh motion deviates significantly from the previous motions. The front wheel starts on the next step while the bottom wheel starts on the previous step. The tail now contacts the edge of the previous step rather than the ground, which causes a significant force to pull the LIMs backwards. Because of this, unlike in the fourth motion, the front wheel will not initially roll forward on the next step. The back wheel will lift from below until it is at a certain angle above the front wheel, at which point the front wheel will start to roll forward, bringing it to the base of the next step.

The eighth motion is similar to the second motion, except the tail pushes against the edge of the previous step and the back wheel is already partially lifted. The back wheel then lifts up further until the LIM is vertical.

The ninth motion is similar to the sixth motion, except the tail pushes against the surface of the previous step instead of the ground.

Appendix A

ECSA Outcome Self Assessment

Table A.1: ECSA outcome self assessment

ECSA outcome	Application
Demonstrate competence to identify, assess, formulate and solve convergent and divergent engineering problems creatively and innovatively.	The design aspect of this project will require creative solutions to overcome the limitations of previous designs.
Application of scientific and engineering knowledge: Demonstrate competence to apply knowledge of mathematics, basic science and engineering sciences from first principles to solve engineering problems.	Producing the mathematical model will require kinematic calculations.
Engineering Design: Demonstrate competence to perform creative, procedural and non-procedural design and synthesis of components, systems, engineering works, products or processes.	A prototype of a USAR platform will be designed and produced.
Engineering methods, skills and tools, including Information Technology: Demonstrate competence to use appropriate engineering methods, skills and tools, including those based on information technology.	The project involves a CAD drawing and simulation of the platform, which will be based on information technology.
Professional and technical communication: Demonstrate competence to communicate effectively, both orally and in writing, with engineering audiences and the community at large.	All deliverables, including the proposal, progress report, final report, and presentation will demonstrate competent and effective communication.
Individual, Team and Multidisciplinary Working: Demonstrate competence to work effectively as an individual, in teams and in multi-disciplinary environments.	This project is done individually, with some input from the project supervisor.
Independent Learning Ability: Demonstrate competence to engage in independent learning through well-developed learning skills.	Research will be done in the literature review.

Appendix B

Mathematical proofs

B.1 Euler's equation

B.2 Navier Stokes equation

Appendix C

Experimental results

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