

# SC205- Discrete Mathematics

## Home Work 3

**Tutorial Discussion Week:** February 3, 2020

(1) Let  $A = (Q, \Sigma, \delta, q_0, F)$  be the DFA, where  $Q = \{q_0, q_1, q_2, q_3\}$ ,  $\Sigma = \{0, 1\}$ ,  $F = \{q_1, q_2\}$  and the transition function  $\delta$  is defined by the following table:

$\delta$	0	1
$q_0$	$q_1$	$q_3$
$q_1$	$q_2$	$q_3$
$q_2$	$q_2$	$q_2$
$q_3$	$q_3$	$q_3$

Give the state digram of this machine. Also determine if  $A$  accepts the strings 000 and 010 ?

(2) Give state diagrams of *DFA*s recognizing the following languages. In all cases the alphabet  $\Sigma = \{0, 1\}$ .

- (i)  $\{w \mid \text{every odd position of } w \text{ is } 1\}$ .
- (ii)  $\{w \mid w \text{ has } 010 \text{ as a substring}\}$ .
- (iii)  $\{w \mid w \text{ has odd number of } 0\text{'s and even number of } 1\text{'s}\}$ .
- (iv)  $\{w \mid \text{the length of } w \text{ is at most } 5\}$ .
- (v)  $\{w \mid w \text{ does not contain the substring } 110\}$ .
- (vi)  $\{w \mid w \text{ is any string except } 11 \text{ and } 111\}$ .
- (vii)  $\{\epsilon, 0\}$ .
- (viii) The empty set.
- (ix) All strings except the empty string.

(3) Give NFAs (or  $\epsilon$ -NFAs) with the specified number of states recognizing each of the following languages. Convert the NFAs (or  $\epsilon$ -NFAs) to DFAs.

- (i) The language  $\{0\}$  with two states.
- (ii) The language  $\{0\}^*$  with one state.

(4) An  $\epsilon$ -NFA is given by  $A = (Q, \Sigma, \delta, q_0, F)$ , where  $Q = \{q_0, q_1, q_2, q_3, q_4, q_5\}$ ,  $\Sigma = \{0, 1\}$ ,  $F = \{q_3, q_4\}$  and the transition function  $\delta$  is defined by the following table:

$\delta$	0	1	$\epsilon$
$q_0$	$\{q_0\}$	$\{q_0, q_2\}$	$\{q_1\}$
$q_1$	$\{q_5\}$	$\{q_2\}$	$\phi$
$q_2$	$\{q_3\}$	$\phi$	$\phi$
$q_3$	$\phi$	$\phi$	$\{q_4\}$
$q_4$	$\{q_3\}$	$\phi$	$\phi$
$q_5$	$\phi$	$\{q_4\}$	$\phi$

Find a *DFA* equivalent to the  $\epsilon$ -NFA  $A$ .