

ASSIGNMENT 10  
MSO-201: PROBABILITY AND STATISTICS

1. Suppose  $X$  and  $Y$  are independent  $N(0,1)$  random variables. If the PDF and CDF are denoted by  $\phi(x)$  and  $\Phi(x)$  respectively, find the PDF of  $U = \max\{X, Y\}$ .
2. Suppose  $X$  and  $Y$  are independent  $N(0,1)$  random variables. If the PDF and CDF are denoted by  $\phi(x)$  and  $\Phi(x)$  respectively, find the PDF of  $U = \min\{X, Y\}$ .
3. Suppose  $X$  and  $Y$  are independent  $N(0,1)$  random variables, find  $P(2X + 3Y < 0)$
4. Suppose the random vector  $(X, Y)$  has the following joint PDF

$$f_{X,Y}(x, y) = 2e^{-(x+y)}; 0 < x < y < \infty$$

and zero, otherwise. Find the joint PDF of  $(U, V)$ , where  $U = 2X + 3Y$  and  $V = 3X + 2Y$ .

5. Suppose the random vector  $(X, Y)$  has the following joint PDF

$$f_{X,Y}(x, y) = 2e^{-(x+y)}; 0 < x < y < \infty$$

and zero, otherwise. Find the joint PDF of  $(U, V)$ , where  $U = X + Y$  and  $V = X + 2Y$ .

6. Suppose the random vector  $(X, Y)$  has the following joint PDF

$$f_{X,Y}(x, y) = xye^{-(x+y)}; 0 < x, y < \infty$$

and zero, otherwise. Find the joint PDF of  $(U, V)$ , where  $U = X + Y$  and  $V = X - Y$ .

7. Suppose  $X$  is a random variable with the following PDF for  $\lambda > 0$

$$f_X(x) = \frac{\lambda}{2}e^{-\lambda|x|}; \quad -\infty < x < \infty.$$

Find the MGF of  $X$

8. Suppose  $X$  and  $Y$  are independent identically distributed exponential random variables with mean 1. Find the joint MGF of  $(U, V)$ , where  $U = X + Y$  and  $V = X - Y$ . Find the PDF of  $U$  and the PDF of  $V$ . Are they independent.
9. Suppose  $X$  and  $Y$  are independent identically distributed non-negative random variables with PDF  $f(x)$  and CDF  $F(x)$ . Find the PDF of  $U = XY$ .
10. Suppose  $X$  and  $Y$  are independent identically distributed exponential random variables with mean 1. Find the joint PDF of  $(U, V)$ , where  $U = XY$  and  $V = X/Y$ .