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## *Algoritmo Viola-Jones*

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# Algoritmo Viola-Jones

## 1 O artigo

Em 2001, *Paul Viola* e *Michael Jones*, dois pesquisadores de Cambridge publicaram um artigo intitulado: “*Rapid Object Detection using a Boosted Cascade of Simple Features*” que demonstrava um novo método de detecção de faces. O artigo se diferencia e se paltava em 3 pontos importantes.

A primeira foi uma nova maneira de se representar uma imagem, a “imagem integral” (*Integral Image*, em inglês), que permitiu os detectores usados por eles, computarem a imagem de maneira mais rápida.

A segunda foi o algoritmo de aprendizado baseado no *AdaBoost*, que selecionava um número pequeno de características visuais críticas de um conjunto maior e com seus classificadores, extremamente eficientes.

O terceiro aspecto importante, foi o método de combinar e incrementar classificadores em “cascata”, o que permitia regiões do fundo da foto de serem rapidamente descartadas, disponibilizando maior processamento computacional em posições com maior possibilidade de ser o objeto no qual se está procurando, como um rosto.

Os autores aprofundaram seus métodos de como construíram esse algoritmo, de como funcionavam as equações e apresentaram os resultados encontrados e compararam com algoritmos similares da época, e como os algoritmos “*Rowley-Baluja-Kanade*”, “*Schneiderman-Kanade*” e “*Roth-Yang-Ahuja*”.

Devido sua implementação seguir uma abordagem diferente para construção de um sistema de detecção de face, aproximadamente 15 vezes mais rápida que os métodos anteriores, o algoritmo *Viola-Jones* revolucionou esse campo da computação se tornando uma referência.

## 2 Funcionamento do algoritmo

## 3 Vantagem

- 15 vezes mais rápido que o algoritmo “*Rowley-Baluja-Kanade*” no processamento da imagem.
- 600 vezes se comparado ao “*Schneiderman-Kanade*”.

## 4 Desvantagem

- A detecção de faces, só é possível se o rosto estiver na posição frontal.
- A base de dados usada, precisa de faces em diferentes condições incluindo: iluminação, brilho, escala, pose e variações de câmera.
- Nível de detecção na literatura - 80% (FAUX,2012)
- É um algoritmo de detecção de face e não de reconhecimento facial.

## 5 Exemplos de Implementação

### 5.1 Python

<https://github.com/Simon-Hohberg/Viola-Jones>

### 5.2 Integral - Image

```
1 import numpy as np
2
3
4 """
5 In an integral image each pixel is the sum of all pixels in the
6 original image
7 that are 'left and above' the pixel.
8
9 Original      Integral
10 +-----+    +-----+
11 | 1 2 3 . |    | 0 0 0 0 . |
12 | 4 5 6 . |    | 0 1 3 6 . |
13 | . . . . |    | 0 5 12 21 . |
14 |         |    | . . . . . |
15
16 """
17
18 def to_integral_image(img_arr):
19     """
20     Calculates the integral image based on this instance's original
21     image data.
22     :param img_arr: Image source data
23     :type img_arr: numpy.ndarray
24     :return Integral image for given image
25     :rtype: numpy.ndarray
26     """
27     # an index of -1 refers to the last row/column
28     # since row_sum is calculated starting from (0,0),
29     # rowSum(x, -1) == 0 holds for all x
30     row_sum = np.zeros(img_arr.shape)
31     # we need an additional column and row
32     integral_image_arr = np.zeros((img_arr.shape[0] + 1, img_arr.shape
33     [1] + 1))
34     for x in range(img_arr.shape[1]):
35         for y in range(img_arr.shape[0]):
36             row_sum[y, x] = row_sum[y-1, x] + img_arr[y, x]
37             integral_image_arr[y+1, x+1] = integral_image_arr[y+1, x
38             -1+1] + row_sum[y, x]
39     return integral_image_arr
40
41
42 def sum_region(integral_img_arr, top_left, bottom_right):
43     """
44     Calculates the sum in the rectangle specified by the given tuples.
45     :param integral_img_arr:
46     :type integral_img_arr: numpy.ndarray
47     :param top_left: (x, y) of the rectangle's top left corner
48     :type top_left: (int, int)
49     :param bottom_right: (x, y) of the rectangle's bottom right corner
50     :type bottom_right: (int, int)
```

```

48     :return The sum of all pixels in the given rectangle
49     :rtype int
50     """
51     # swap tuples
52     top_left = (top_left[1], top_left[0])
53     bottom_right = (bottom_right[1], bottom_right[0])
54     if top_left == bottom_right:
55         return integral_img_arr[top_left]
56     top_right = (bottom_right[0], top_left[1])
57     bottom_left = (top_left[0], bottom_right[1])
58     return integral_img_arr[bottom_right] - integral_img_arr[top_right]
    - integral_img_arr[bottom_left] + integral_img_arr[top_left]

```

recursos/codigo\_python/Viola-Jones-master/violajones/IntegralImage.py

## 5.3 Haar Like Feature

```

1 import violajones.IntegralImage as ii
2
3
4 def enum(**enums):
5     return type('Enum', (), enums)
6
7 FeatureType = enum(TWO_VERTICAL=(1, 2), TWO_HORIZONTAL=(2, 1),
8     THREE_HORIZONTAL=(3, 1), THREE_VERTICAL=(1, 3), FOUR=(2, 2))
9 FeatureTypes = [FeatureType.TWO_VERTICAL, FeatureType.TWO_HORIZONTAL,
10     FeatureType.THREE_VERTICAL, FeatureType.THREE_HORIZONTAL,
11     FeatureType.FOUR]
12
13 class HaarLikeFeature(object):
14     """
15     Class representing a haar-like feature.
16     """
17
18     def __init__(self, feature_type, position, width, height, threshold,
19         polarity):
20         """
21         Creates a new haar-like feature.
22         :param feature_type: Type of new feature, see FeatureType enum
23         :type feature_type: violajonse.HaarLikeFeature.FeatureTypes
24         :param position: Top left corner where the feature begins (x, y)
25
26         :type position: (int, int)
27         :param width: Width of the feature
28         :type width: int
29         :param height: Height of the feature
30         :type height: int
31         :param threshold: Feature threshold
32         :type threshold: float
33         :param polarity: polarity of the feature -1 or 1
34         :type polarity: int
35         """
36         self.type = feature_type
37         self.top_left = position
38         self.bottom_right = (position[0] + width, position[1] + height)
39         self.width = width
40         self.height = height
41         self.threshold = threshold

```

```

38         self.polarity = polarity
39         self.weight = 1
40
41     def get_score(self, int_img):
42         """
43         Get score for given integral image array.
44         :param int_img: Integral image array
45         :type int_img: numpy.ndarray
46         :return: Score for given feature
47         :rtype: float
48         """
49         score = 0
50         if self.type == FeatureType.TWO_VERTICAL:
51             first = ii.sum_region(int_img, self.top_left, (self.
top_left[0] + self.width, int(self.top_left[1] + self.height / 2)))
52             second = ii.sum_region(int_img, (self.top_left[0], int(self
.top_left[1] + self.height / 2)), self.bottom_right)
53             score = first - second
54         elif self.type == FeatureType.TWO_HORIZONTAL:
55             first = ii.sum_region(int_img, self.top_left, (int(self.
top_left[0] + self.width / 2), self.top_left[1] + self.height))
56             second = ii.sum_region(int_img, (int(self.top_left[0] +
self.width / 2), self.top_left[1]), self.bottom_right)
57             score = first - second
58         elif self.type == FeatureType.THREE_HORIZONTAL:
59             first = ii.sum_region(int_img, self.top_left, (int(self.
top_left[0] + self.width / 3), self.top_left[1] + self.height))
60             second = ii.sum_region(int_img, (int(self.top_left[0] +
self.width / 3), self.top_left[1]), (int(self.top_left[0] + 2 *
self.width / 3), self.top_left[1] + self.height))
61             third = ii.sum_region(int_img, (int(self.top_left[0] + 2 *
self.width / 3), self.top_left[1]), self.bottom_right)
62             score = first - second + third
63         elif self.type == FeatureType.THREE_VERTICAL:
64             first = ii.sum_region(int_img, self.top_left, (self.
bottom_right[0], int(self.top_left[1] + self.height / 3)))
65             second = ii.sum_region(int_img, (self.top_left[0], int(self
.top_left[1] + self.height / 3)), (self.bottom_right[0], int(self.
top_left[1] + 2 * self.height / 3)))
66             third = ii.sum_region(int_img, (self.top_left[0], int(self.
top_left[1] + 2 * self.height / 3)), self.bottom_right)
67             score = first - second + third
68         elif self.type == FeatureType.FOUR:
69             # top left area
70             first = ii.sum_region(int_img, self.top_left, (int(self.
top_left[0] + self.width / 2), int(self.top_left[1] + self.height /
2)))
71             # top right area
72             second = ii.sum_region(int_img, (int(self.top_left[0] +
self.width / 2), self.top_left[1]), (self.bottom_right[0], int(self
.top_left[1] + self.height / 2)))
73             # bottom left area
74             third = ii.sum_region(int_img, (self.top_left[0], int(self.
top_left[1] + self.height / 2)), (int(self.top_left[0] + self.width
/ 2), self.bottom_right[1]))
75             # bottom right area
76             fourth = ii.sum_region(int_img, (int(self.top_left[0] +
self.width / 2), int(self.top_left[1] + self.height / 2)), self.
bottom_right)
77             score = first - second - third + fourth

```

```

78         return score
79
80     def get_vote(self, int_img):
81         """
82         Get vote of this feature for given integral image.
83         :param int_img: Integral image array
84         :type int_img: numpy.ndarray
85         :return: 1 iff this feature votes positively, otherwise -1
86         :rtype: int
87         """
88         score = self.get_score(int_img)
89         return self.weight * (1 if score < self.polarity * self.
threshold else -1)

```

recursos/codigo-python/Viola-Jones-master/violajones/HaarLikeFeature.py

## 5.4 AdaBoost

```

1 from functools import partial
2 import numpy as np
3 from violajones.HaarLikeFeature import HaarLikeFeature
4 from violajones.HaarLikeFeature import FeatureTypes
5 import progressbar
6 from multiprocessing import Pool
7
8 LOADING_BAR_LENGTH = 50
9
10
11 # TODO: select optimal threshold for each feature
12 # TODO: attentional cascading
13
14 def learn(positive_iis, negative_iis, num_classifiers=-1,
min_feature_width=1, max_feature_width=-1, min_feature_height=1,
max_feature_height=-1):
15     """
16     Selects a set of classifiers. Iteratively takes the best
17     classifiers based
18     on a weighted error.
19     :param positive_iis: List of positive integral image examples
20     :type positive_iis: list[numpy.ndarray]
21     :param negative_iis: List of negative integral image examples
22     :type negative_iis: list[numpy.ndarray]
23     :param num_classifiers: Number of classifiers to select, -1 will
use all
24     classifiers
25     :type num_classifiers: int
26
27     :return: List of selected features
28     :rtype: list[violajones.HaarLikeFeature.HaarLikeFeature]
29     """
30     num_pos = len(positive_iis)
31     num_neg = len(negative_iis)
32     num_imgs = num_pos + num_neg
33     img_height, img_width = positive_iis[0].shape
34
35     # Maximum feature width and height default to image width and
height
36     max_feature_height = img_height if max_feature_height == -1 else
max_feature_height

```

```

36     max_feature_width = img_width if max_feature_width == -1 else
max_feature_width
37
38     # Create initial weights and labels
39     pos_weights = np.ones(num_pos) * 1. / (2 * num_pos)
40     neg_weights = np.ones(num_neg) * 1. / (2 * num_neg)
41     weights = np.hstack((pos_weights, neg_weights))
42     labels = np.hstack((np.ones(num_pos), np.ones(num_neg) * -1))
43
44     images = positive_iis + negative_iis
45
46     # Create features for all sizes and locations
47     features = _create_features(img_height, img_width,
min_feature_width, max_feature_width, min_feature_height,
max_feature_height)
48     num_features = len(features)
49     feature_indexes = list(range(num_features))
50
51     num_classifiers = num_features if num_classifiers == -1 else
num_classifiers
52
53     print('Calculating scores for images..')
54
55     votes = np.zeros((num_imgs, num_features))
56     bar = progressbar.ProgressBar()
57     # Use as many workers as there are CPUs
58     pool = Pool(processes=None)
59     for i in bar(range(num_imgs)):
60         votes[i, :] = np.array(list(pool.map(partial(_get_feature_vote,
image=images[i]), features)))
61
62     # select classifiers
63
64     classifiers = []
65
66     print('Selecting classifiers..')
67     bar = progressbar.ProgressBar()
68     for _ in bar(range(num_classifiers)):
69
70         classification_errors = np.zeros(len(feature_indexes))
71
72         # normalize weights
73         weights *= 1. / np.sum(weights)
74
75         # select best classifier based on the weighted error
76         for f in range(len(feature_indexes)):
77             f_idx = feature_indexes[f]
78             # classifier error is the sum of image weights where the
classifier
79             # is right
80             error = sum(map(lambda img_idx: weights[img_idx] if labels[
img_idx] != votes[img_idx, f_idx] else 0, range(num_imgs)))
81             classification_errors[f] = error
82
83             # get best feature, i.e. with smallest error
84             min_error_idx = np.argmin(classification_errors)
85             best_error = classification_errors[min_error_idx]
86             best_feature_idx = feature_indexes[min_error_idx]
87
88             # set feature weight

```



```

89         best_feature = features[best_feature_idx]
90         feature_weight = 0.5 * np.log((1 - best_error) / best_error)
91         best_feature.weight = feature_weight
92
93         classifiers.append(best_feature)
94
95         # update image weights
96         weights = np.array(list(map(lambda img_idx: weights[img_idx] *
np.sqrt((1-best_error)/best_error) if labels[img_idx] != votes[
img_idx, best_feature_idx] else weights[img_idx] * np.sqrt(
best_error/(1-best_error)), range(num_imgs))))
97
98         # remove feature (a feature can't be selected twice)
99         feature_indexes.remove(best_feature_idx)
100
101     return classifiers
102
103
104 def _get_feature_vote(feature, image):
105     return feature.get_vote(image)
106
107
108 def _create_features(img_height, img_width, min_feature_width,
max_feature_width, min_feature_height, max_feature_height):
109     print('Creating haar-like features..')
110     features = []
111     for feature in FeatureTypes:
112         # FeatureTypes are just tuples
113         feature_start_width = max(min_feature_width, feature[0])
114         for feature_width in range(feature_start_width,
max_feature_width, feature[0]):
115             feature_start_height = max(min_feature_height, feature[1])
116             for feature_height in range(feature_start_height,
max_feature_height, feature[1]):
117                 for x in range(img_width - feature_width):
118                     for y in range(img_height - feature_height):
119                         features.append(HaarLikeFeature(feature, (x, y)
, feature_width, feature_height, 0, 1))
120                         features.append(HaarLikeFeature(feature, (x, y)
, feature_width, feature_height, 0, -1))
121     print('..done.' + str(len(features)) + ' features created.\n')
122     return features

```

recursos/codigo-python/Viola-Jones-master/viola-jones/AdaBoost.py

## 5.5 Utils

```

1 import numpy as np
2 from PIL import Image
3 from violajones.HaarLikeFeature import FeatureType
4 from functools import partial
5 import os
6
7
8 def ensemble_vote(int_img, classifiers):
9     """
10     Classifies given integral image (numpy array) using given
    classifiers, i.e.

```

```

11     if the sum of all classifier votes is greater 0, image is
12     classified
13     positively (1) else negatively (0). The threshold is 0, because
14     votes can be
15     +1 or -1.
16     :param int_img: Integral image to be classified
17     :type int_img: numpy.ndarray
18     :param classifiers: List of classifiers
19     :type classifiers: list[violajones.HaarLikeFeature.HaarLikeFeature]
20     :return: 1 iff sum of classifier votes is greater 0, else 0
21     :rtype: int
22     """
23     return 1 if sum([c.get_vote(int_img) for c in classifiers]) >= 0
24     else 0
25
26 def ensemble_vote_all(int_imgs, classifiers):
27     """
28     Classifies given list of integral images (numpy arrays) using
29     classifiers,
30     i.e. if the sum of all classifier votes is greater 0, an image is
31     classified
32     positively (1) else negatively (0). The threshold is 0, because
33     votes can be
34     +1 or -1.
35     :param int_imgs: List of integral images to be classified
36     :type int_imgs: list[numpy.ndarray]
37     :param classifiers: List of classifiers
38     :type classifiers: list[violajones.HaarLikeFeature.HaarLikeFeature]
39     :return: List of assigned labels, 1 if image was classified
40     positively, else
41     0
42     :rtype: list[int]
43     """
44     vote_partial = partial(ensemble_vote, classifiers=classifiers)
45     return list(map(vote_partial, int_imgs))
46
47 def reconstruct(classifiers, img_size):
48     """
49     Creates an image by putting all given classifiers on top of each
50     other
51     producing an archetype of the learned class of object.
52     :param classifiers: List of classifiers
53     :type classifiers: list[violajones.HaarLikeFeature.HaarLikeFeature]
54     :param img_size: Tuple of width and height
55     :type img_size: (int, int)
56     :return: Reconstructed image
57     :rtype: PIL.Image
58     """
59     image = np.zeros(img_size)
60     for c in classifiers:
61         # map polarity: -1 -> 0, 1 -> 1
62         polarity = pow(1 + c.polarity, 2)/4
63         if c.type == FeatureType.TWO_VERTICAL:
64             for x in range(c.width):
65                 sign = polarity
66                 for y in range(c.height):
67                     if y >= c.height/2:
68                         sign = (sign + 1) % 2

```

```

63         image[c.top_left[1] + y, c.top_left[0] + x] += 1 *
sign * c.weight
64     elif c.type == FeatureType.TWO_HORIZONTAL:
65         sign = polarity
66         for x in range(c.width):
67             if x >= c.width/2:
68                 sign = (sign + 1) % 2
69             for y in range(c.height):
70                 image[c.top_left[0] + x, c.top_left[1] + y] += 1 *
sign * c.weight
71     elif c.type == FeatureType.THREE_HORIZONTAL:
72         sign = polarity
73         for x in range(c.width):
74             if x % c.width/3 == 0:
75                 sign = (sign + 1) % 2
76             for y in range(c.height):
77                 image[c.top_left[0] + x, c.top_left[1] + y] += 1 *
sign * c.weight
78     elif c.type == FeatureType.THREE_VERTICAL:
79         for x in range(c.width):
80             sign = polarity
81             for y in range(c.height):
82                 if x % c.height/3 == 0:
83                     sign = (sign + 1) % 2
84                 image[c.top_left[0] + x, c.top_left[1] + y] += 1 *
sign * c.weight
85     elif c.type == FeatureType.FOUR:
86         sign = polarity
87         for x in range(c.width):
88             if x % c.width/2 == 0:
89                 sign = (sign + 1) % 2
90             for y in range(c.height):
91                 if x % c.height/2 == 0:
92                     sign = (sign + 1) % 2
93                 image[c.top_left[0] + x, c.top_left[1] + y] += 1 *
sign * c.weight
94     image -= image.min()
95     image /= image.max()
96     image *= 255
97     result = Image.fromarray(image.astype(np.uint8))
98     return result
99
100
101 def load_images(path):
102     images = []
103     for _file in os.listdir(path):
104         if _file.endswith('.png'):
105             img_arr = np.array(Image.open((os.path.join(path, _file))),
dtype=np.float64)
106             img_arr /= img_arr.max()
107             images.append(img_arr)
108     return images

```

recursos/codigo\_python/Viola-Jones-master/violajones/Utils.py

## 5.6 example

```

1 import violajones.IntegralImage as ii
2 import violajones.AdaBoost as ab

```

```

3 import violajones.Uutils as utils
4
5 if __name__ == "__main__":
6     pos_training_path = 'trainingdata/faces'
7     neg_training_path = 'trainingdata/nonfaces'
8     pos_testing_path = 'trainingdata/faces/test'
9     neg_testing_path = 'trainingdata/nonfaces/test'
10
11     num_classifiers = 2
12     # For performance reasons restricting feature size
13     min_feature_height = 8
14     max_feature_height = 10
15     min_feature_width = 8
16     max_feature_width = 10
17
18     print('Loading faces..')
19     faces_training = utils.load_images(pos_training_path)
20     faces_ii_training = list(map(ii.to_integral_image, faces_training))
21     print('..done. ' + str(len(faces_training)) + ' faces loaded.\n\
nLoading non faces..')
22     non_faces_training = utils.load_images(neg_training_path)
23     non_faces_ii_training = list(map(ii.to_integral_image,
non_faces_training))
24     print('..done. ' + str(len(non_faces_training)) + ' non faces
loaded.\n')
25
26     # classifiers are haar like features
27     classifiers = ab.learn(faces_ii_training, non_faces_ii_training,
num_classifiers, min_feature_height, max_feature_height,
min_feature_width, max_feature_width)
28
29     print('Loading test faces..')
30     faces_testing = utils.load_images(pos_testing_path)
31     faces_ii_testing = list(map(ii.to_integral_image, faces_testing))
32     print('..done. ' + str(len(faces_testing)) + ' faces loaded.\n\
nLoading test non faces..')
33     non_faces_testing = utils.load_images(neg_testing_path)
34     non_faces_ii_testing = list(map(ii.to_integral_image,
non_faces_testing))
35     print('..done. ' + str(len(non_faces_testing)) + ' non faces loaded
.\n')
36
37     print('Testing selected classifiers..')
38     correct_faces = 0
39     correct_non_faces = 0
40     correct_faces = sum(utils.ensemble_vote_all(faces_ii_testing,
classifiers))
41     correct_non_faces = len(non_faces_testing) - sum(utils.
ensemble_vote_all(non_faces_ii_testing, classifiers))
42
43     print('..done.\n\nResult:\n      Faces: ' + str(correct_faces) + '/'
+ str(len(faces_testing))
44           + ' (' + str((float(correct_faces) / len(faces_testing)) *
100) + '%)\n      non-Faces: '
45           + str(correct_non_faces) + '/' + str(len(non_faces_testing))
+ ' ('
46           + str((float(correct_non_faces) / len(non_faces_testing)) *
100) + '%)')
47

```

```
48 | # Just for fun: putting all haar-like features over each other  
    | generates a face-like image  
49 | recon = utils.reconstruct(classifiers , faces_testing[0].shape)  
50 | recon.save('reconstruction.png')
```

recursos/codigo-python/Viola-Jones-master/example.py

## 6 Referências Bibliográfica

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