2022-July Session-07-27-2022-shift-1

AI24BTECH11006 - Bugada Roopansha

I. SECTION - A

- 1) Let a die be rolled until a 2 is obtained. The probability that a 2 is obtained on an evennumbered toss is equal to:
- 2) $\lim_{x \to \frac{\pi^{-}}{2}} \frac{\int_{x^{3}}^{\left(\frac{\pi}{2}\right)^{2}} \cos t^{\frac{1}{3}} dt}{\left(x \frac{\pi}{2}\right)^{2}}$
- 3) Consider the equation $4\sqrt{2}x^3 3\sqrt{2}x 1 = 0$. Statement 1: The solution of this equation is $\cos \frac{\pi}{12}$.

Statement 2: This equation has only one real solution.

- a) Both statements are true.
- b) Statement 1 is true but Statement 2 is false.
- c) Statement 1 is false but Statement 2 is true.
- d) Both statements are false.
- 4) If $\mod 2A^3 = 2^{21}$ and $A = \begin{bmatrix} 1 & 0 & 0 \\ 0 & \alpha & \beta \\ 0 & \beta & \alpha \end{bmatrix}$, then
 - α is:
 - a) 5
 - b) 3
 - c) 9
 - d) 17
- 5) In a GP with 64 terms, if the sum of all terms is seven times the sum of the odd terms, the common ratio is:
 - a) 3
 - b) 4
 - c) 5
- 6) Given $\frac{dy}{dx} \left(\frac{\sin 2x}{1 + \cos^2 x}\right) y = \left(\frac{\sin x}{1 + \cos^2 x}\right)$ and y(0) = 0, find $y\left(\frac{\pi}{2}\right)$.

- a) -1
- b) 1
- c) 0
- d) 2
- 7) $4\cos\theta + 5\sin\theta = 1$. Then find $\tan\theta$, where $\theta \in \left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$.

1

- a) $\frac{10-\sqrt{10}}{6}$ b) $\frac{10-\sqrt{10}}{12}$ c) $\frac{\sqrt{10-10}}{6}$ d) $\frac{\sqrt{10-10}}{12}$
- 8) In an increasing arithmetic progression a_1, a_2, \dots, a_n , if $a_6 = 2$ and the product of a_1, a_5, a_4 is the greatest, then the common difference d is:
 - a) 1.6
 - b) 1.8
 - c) 0.6
 - d) 2.0
- 9) If the relation R:(a,b)R(c,d) holds only if ad - bc is divisible by 5 where $a, b, c, d \in \mathbb{Z}$, then R is:
 - a) Reflexive
 - b) Symmetric, Reflexive but not Transitive
 - c) Reflexive, Transitive but not Symmetric
 - d) An Equivalence Relation
- 10) Let f(x) and g(x) be defined as follows:

$$f(x) = \begin{cases} 2x + 2 & \text{if } x \in (-1, 0) \\ 1 - \frac{x}{3} & \text{if } x \in [0, 3] \end{cases}$$
$$g(x) = \begin{cases} x & \text{if } x \in [0, 1] \\ -x & \text{if } x \in (-3, 0) \end{cases}$$

The range of $f \circ g(x)$ is:

- a) [0, 1]
- b) [-1,1]
- c) [0, 1]
- d) (-1,1)
- 11) If $\int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \left(\frac{x^2 \cos x}{1 + \pi^x} + \frac{1 + \sin^2 x}{1 + e^{(\sin x)^2 023}} \right) dx = \frac{\pi}{4} (\pi + \alpha) 2$, then α is equal to:
 - a) 1
 - b) 2

- c) 3
- d) 4
- 12) The area under the curve $x^2 + y^2 = 169$ and below the line 5x y = 13 is:
- a) $\frac{169\pi}{4} \frac{65}{2} + \frac{169}{2} \sin^{-1} \frac{12}{13}$ b) $\frac{169\pi}{4} + \frac{65}{2} \frac{169}{2} \sin^{-1} \frac{12}{13}$ c) $\frac{169\pi}{4} \frac{65}{2} + \frac{169}{2} \sin^{-1} \frac{13}{14}$ d) $\frac{169\pi}{4} + \frac{65}{2} + \frac{169}{2} \sin^{-1} \frac{13}{14}$ 13) If $f(x) = \frac{(2^{x} + 2^{-x})(\tan x)\tan^{-1}(2x^{2} 3x + 1)}{(7x^{2} 3x + 1)^{3}}$, then f(0)
 - is:
 - a) $\sqrt{\pi}$
 - b) $\sqrt{\frac{\pi}{4}}$
 - c) π
 - d) $2 \cdot \pi^{\frac{3}{2}}$
- 14) Evaluate $\int \frac{(\sin x \cos x) \sin^2 x}{\sin x \cos^2 x + \tan x \sin^3 x} dx$ is equal to

 a) $\frac{1}{3} \ln \left| \sin^3 x \cos^3 x \right| + C$

 b) $\frac{1}{3} \ln \left| \sin^3 x + \cos^3 x \right| + C$

 c) $\frac{1}{2} \ln \left| \sin^3 x \cos^3 x \right| + C$

 d) $\frac{1}{4} \ln \left| \sin^3 x + \cos^3 x \right| + C$