2021-March Session-03-18-2021-shift-2

AI24BTECH11006 - Bugada Roopansha

I. SECTION - A

- 16) If P and Q are two statements, then which of the following compound statements is a tautology?
 - a) $((P \Rightarrow Q) \land \neg Q) \Rightarrow P$
 - b) $((P \Rightarrow Q) \land \neg Q) \Rightarrow \neg P$
 - c) $(P \Rightarrow Q) \land \neg Q$
 - d) $((P \Rightarrow Q) \land \neg Q) \Rightarrow Q$
- 17) Consider a hyperbola H: $x^2 2y^2 = 4$. Let the tangent at a point P $(4, \sqrt{6})$ meet the x-axis at Q and latus rectum at R (x_1, y_1) , $x_1>0$. If F is a focus of H which is nearer to the point P, then the area of $\triangle QFR$ is equal to:
 - a) $\sqrt{6} 1$
 - b) $4\sqrt{6} 1$

 - c) $4\sqrt{6}$ d) $\frac{7}{\sqrt{6}} 2$
- 18) Let $f: \mathbb{R} \to \mathbb{R}$ be a function defined as

$$f(x) = \begin{cases} \frac{\sin((a+1)x) + \sin(2x)}{2x}, & \text{if } x < 0\\ b, & \text{if } x = 0\\ \frac{\sqrt{x + bx^3 - \sqrt{x}}}{bx^{5/2}}, & \text{if } x > 0 \end{cases}$$
 (1)

. If f is continuous at x = 0, then the value of a + b is equal to

- a) -2

- b) $\frac{-2}{5}$ c) $\frac{-3}{2}$ d) -3
- 19) Let y=y(x)be the solution of equation the differential $(y+1) \left[(y+1) e^{x^2/2} - x \right], 0 < x < 2.1, \text{ with }$ y(2) = 0. Then the value of $\frac{dy}{dx}$ at x=1 is equal to:

20) Let a tangent be drawn to the ellipse $(x^2/27)$ + $y^2 = 1$ at $(3\sqrt{3}\cos\theta, \sin\theta)$ where $\theta \in (0, \frac{\pi}{2})$. Then the value of θ such that the sum of intercepts on axes made by a tangent is minimum is equal to:

1

- a) $\frac{\pi}{8}$ b) $\frac{\pi}{6}$ c) $\frac{\pi}{3}$ d) $\frac{\pi}{4}$

II. SECTION - B

- 21) Let P be a plane containing the line $\frac{[x-1]}{3}$ = $\frac{\left[y+6\right]}{4} = \frac{\left[z+5\right]}{2} \text{ and parallel to the line } \frac{\left[x-3\right]}{4} = \frac{\left[y-2\right]}{-3} = \frac{\left[z+5\right]}{7}. \text{ If the point } (1,-1,\alpha) \text{ lies on the plane P, then the value of } |5\alpha| \text{ is equal to } \dots$
- 22) $\sum_{r=1}^{10} r! (r^3 + 6r^2 + 2r + 5) = \alpha (11!)$. Then the value of α is equal to
- 23) The term independent of x in the expansion of $\left[\frac{x+1}{x^{2/3}-x^{1/3}+1} \frac{x-1}{x-x^{1/2}}\right]^{10}$, $x \ne 1$, is equal to...
- 24) Let $\binom{n}{r}$ denote the binomial coefficient of x^{r} in the expansion of $(1+x)^n$. If $\sum_{k=0}^{10} \left[2^2 + 3k\right] \binom{n}{k} = \alpha \cdot 3^{10} + \beta \cdot 2^{10}$ then $\alpha + \beta$ is equal to...
- 25) Let P (x) be a real polynomial of degree 3 which vanishes at x = -3. Let P(x) have local minima at x = 1, local maxima at x = -1and $\int_{-1}^{1} P(x) dx = 18$, then the sum of all the coefficients of the polynomial P (x) is equal to...
- 26) Let the mirror image of the point (1,3,a) with respect to the plane r. (2i - j + k) - b = 0 be (-3,5,2). Then, the value of |a+b| is equal to...
- 27) If f(x) and g(x) are two polynomials such that the polynomial $P(x) = f(x^3) + xg(x^3)$ is divisible by $^2 + x + 1$, then P(1) is equal to...
- 28) Let I be an identity matrix of order 2×2 and $P = \begin{bmatrix} 2 & -1 \\ 5 & -3 \end{bmatrix}$. Then the value of $n \in N$ for which $P^n = 5I - 8P$ is equal to...
- 29) Let $f: \mathbb{R} \to \mathbb{R}$ satisfy the equation f(x+y) = $f(x) \cdot f(y)$ for all $x, y \in \mathbb{R}$ and $f(x) \neq 0$ for

- any $x \in \mathbb{R}$. If the function f is differentiable at x = 0 and f'(0) = 3, then $\lim_{h\to 0} \frac{1}{h} [f(h) 1]$ is equal to ...
- 30) Let y = y(x) be the solution of the differential equation $x dy y dx = \sqrt{x^2 y^2} dx$, $x \ge 1$ with y(1) = 0. If the area bounded by the line x = 1, $x = e^{\pi}$, y = 0 and y = y(x) is $\alpha e^{2\pi} + \beta$ then the value of $10(\alpha + \beta)$ is equal to ...