How does class size affect academic performance: Evidence from primary schools in Israel

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#### Introduction

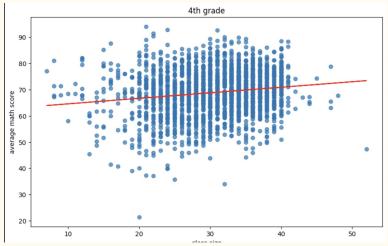
Parents and teachers generally report that they prefer smaller classes because those involved with teaching believe that smaller classes promote student learning and smaller classes offer a more pleasant environment. We will use the data of the 4th and 5th grade students of more than 2000 primary schools classes in Israel. We want to use machine learning models to assess the relationship between class size and academic performance in primary school and compared to the results Refer to the paper "Using Maimonides' Rule to Estimate the Effect of Class Size on Scholastic Achievement" which uses linear models.

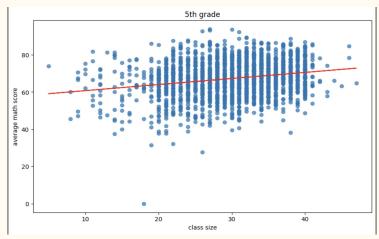
- Is small class or large class more beneficial for pupils' academic performance?
- Is the relationship between class size and educational performance linear?

## Set up

- Variables of Interest
  - $\circ$  Enrollment and class sizes (X)
  - Avg. test scores (y)
  - % disadvantaged students
- Replication of original study (2 Stage Least Squares)
- Polynomial Regression and k-fold cross validation
  - On both 4th and 5th Grade
  - CV on both to pick optimal degree
  - Bootstrap to calculate std. and compare results with 2SLS
- KNN and k-fold cross validation
  - On both 4th and 5th Grade
  - CV on both to pick optimal k
  - Compare bootstrapped standard error and coefficients with 2SLS

OLS - Class size & average math scores



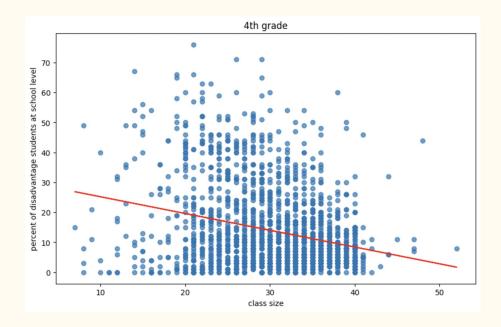


#### Observation:

- OLS generally shows positive correlation between class size and test score (larger class has better performance on test)
- After we add controls, the positive correlation is reduced, but still positive, which does not correspond with our intuition.

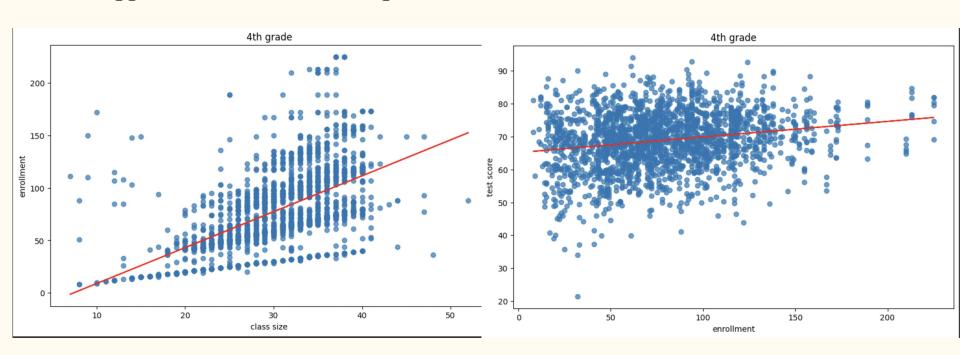
### Bias of OLS

• Greater class size -> less disadvantaged students



## Bias (Cont.)

• Bigger schools tend to have greater class size and better test scores.

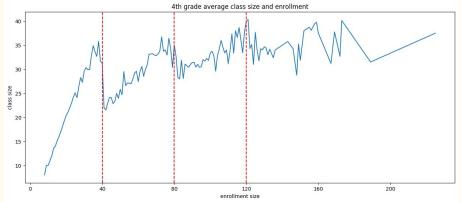


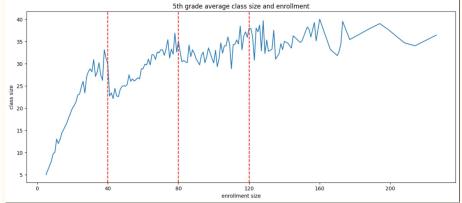
## Why does OLS fail

#### Two reasons:

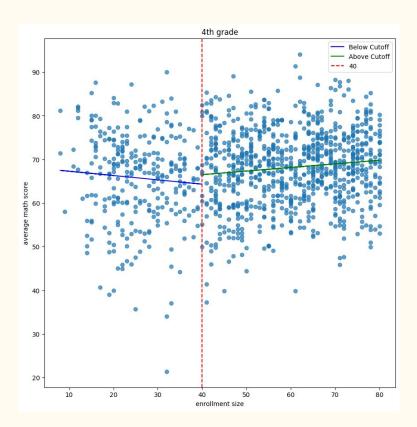
- percent disadvantage variable only track the number of disadvantaged students at the school level, not at the class level within schools, so PD does not explain all the nonrandom selection of students in difference size of class.
- Background info: school principals may group children who are having trouble with their schoolwork into smaller classes, but since we do not have data on the number of disadvantaged students at the class level, we are unable to control for this covariate.

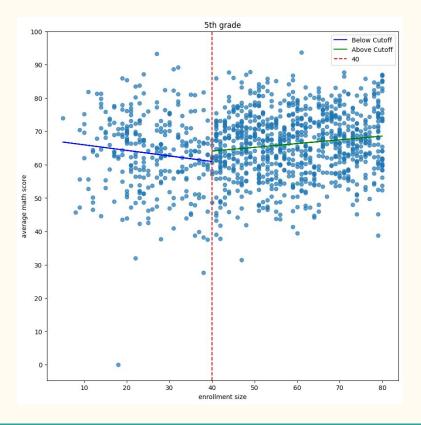
## Another Way Out – RDD





# RDD Using Linear Model





## 2 Stage Least Squares

- Extension of OLS, still assumes linearity
- Adopted by the original paper

```
IV-2SLS Estimation Summary
  Dep. Variable: avgmath
                                    R-squared: 7.308e-05
   Estimator:
                  IV-2SLS
                                  Adj. R-squared: -0.0215
No. Observations: 143
                                    F-statistic: 29.348
      Date:
                  Tue, Nov 28 2023 P-value (F-stat) 0.0000
                                    Distribution: chi2(3)
      Time:
                  00.20.06
 Cov. Estimator: robust
                     Parameter Estimates
         Parameter Std. Err. T-stat P-value Lower Cl Upper Cl
Intercept 123.26
                   55.693 2.2132 0.0269 14.106 232.42
tipuach -0.2294
                   0.0499 -4.6002 0.0000 -0.3271 -0.1317
 c_size -0.9149
                   0.9653 -0.9478 0.3432 -2.8069 0.9770
classize -0.5815
                   0.6300 -0.9230 0.3560 -1.8163 0.6533
Endogenous: classize
Instruments: I class
Robust Covariance (Heteroskedastic)
Debiased: False
id: 0x790418642e90
```

```
IV-2SLS Estimation Summary
  Dep. Variable: avgmath
                                    R-squared: -0.0508
    Estimator:
                  IV-2SLS
                                  Adj. R-squared: -0.0697
No. Observations: 171
                                     F-statistic: 46.666
      Date:
                  Tue. Nov 28 2023 P-value (F-stat) 0.0000
                                    Distribution: chi2(3)
      Time:
                  00.50.08
 Cov. Estimator: robust
                     Parameter Estimates
         Parameter Std. Err. T-stat P-value Lower CI Upper CI
Intercept 94.091
                    47.290 1.9897 0.0466 1.4042
                                                    186.78
 tipuach -0.3601
                   0.0677 -5.3162 0.0000 -0.4928 -0.2273
 c size -0.1214
                   0.6905 -0.1759 0.8604 -1.4748 1.2319
 classize -0.7443
                   0.7614 -0.9776 0.3283 -2.2367 0.7480
Endogenous: classize
Instruments: I class
Robust Covariance (Heteroskedastic)
Debiased: False
id: 0x7904186407f0
```

5th Grade

## Apply machine learning tools

Main issue with using linear model:

- strong assumption on the relationship between variables, which could be wrong.
- In other words, linear model provides a better sense of the general trend but cannot capture the local variations well, causing inaccurate estimation of the average test score near the cutoff. And this directly affects our final estimation of the treatment effect

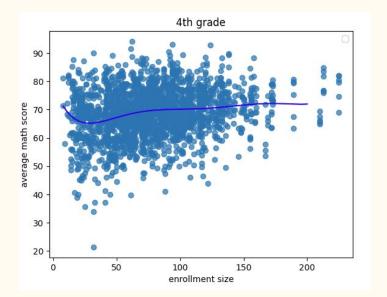
By using machine learning tools:

- We can reduce the error of estimation by selecting the best model that fits the data points, and therefore get a better estimate of the treatment effect.

# Polynomial Regression

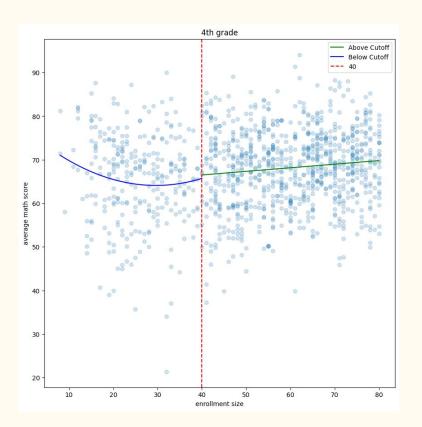
## Full Sample

- Optimal degree = 6 by CV
- Confirms that linearity does not hold

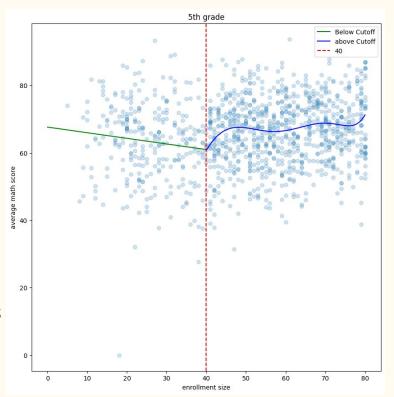


```
degree: 1, error: 72.27507540316613
degree: 2, error: 72.20186217225366
degree: 3, error: 72.22475720044733
degree: 4, error: 72.15140753240284
degree: 5, error: 72.17693359172195
degree: 6, error: 72.06771991309304
degree: 7, error: 169.38810928431312
```

- By k-fold CV...
  - $\circ$  Below cutoff: Degree = 2
  - $\circ$  Above cutoff: Degree = 1
- Model Coef = -0.98
- Stronger than 2SLS Coef (-0.58)
- By Bootstrap...
  - $\circ$  Std. = 1.5247
  - $\circ$  mean = -1.0064
  - $\circ$  -1.0064/1.5247, not significant

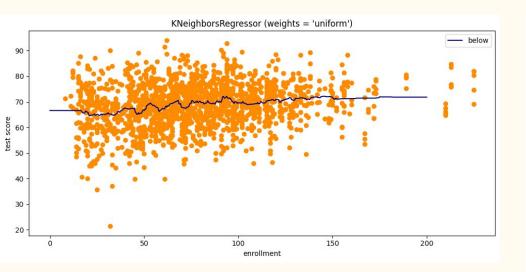


- By k-fold CV...
  - $\circ$  Below cutoff: Degree = 1
  - $\circ$  Above cutoff: Degree = 6
- Model Coef = -3.76
- Stronger than 2SLS Coef (-0.74)
- By Bootstrap...
  - $\circ$  Std. = 1.4678
  - $\circ$  Mean = -3.790
  - -3.790/1.4678, significant local treatment effect

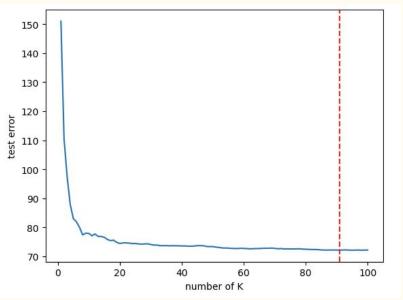


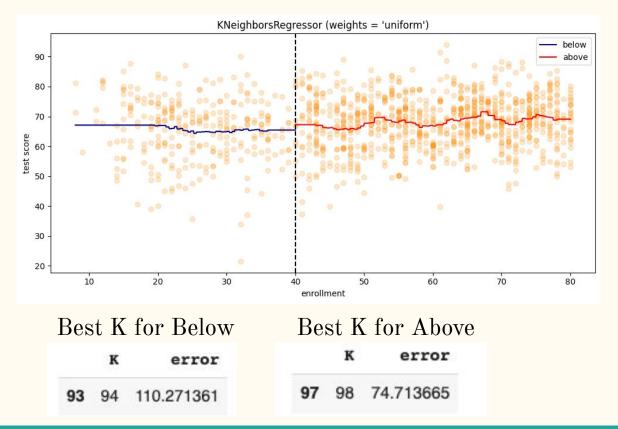
# K-Nearest Neighbors Regression

## KNN Regression

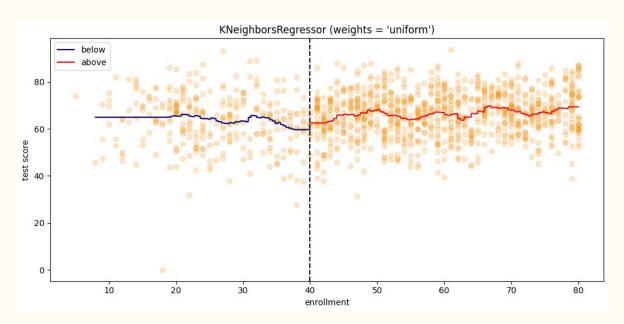








- Model coef = -1.640
- By Bootstrap:
  - o SE=1.4739



- Model coef = -3.358
- By Bootstrap:
  - o SE=1.631

Best K for Below

	K	error
64	65	133.74589

Best K for Above

	K	error
79	80	93.054473

#### Conclusion

- KNN and polynomial regression have similar performance when fitting this dataset (polynomial regression slightly outperforms KNN: test MSE 80.0427 compared to 81.1014)
- Nonlinear relationship

- Different results from nonlinear model compared to linear model:
  - ~ By using the nonlinear model, we found that the average treatment effects are larger than what original paper estimated (larger negative effect of class size on test score)
  - ~ we also found significant treatment effect (for 5th grade) when calculating the variation of the treatment effect by bootstrapping, while the linear model shows no significant results.

#### Discussion

#### Major limitation

- the treatment effect from the sample centered around the cutoff may not be well generalized to the entire population

However, can we increase the bandwidth to include more sample?

- Bias-variance tradeoff
  - ~ Larger bandwidth includes more samples that are not good counterfactual to each other
  - ~ Small bandwidth includes more comparable samples but with much smaller sample size so bigger variance
- Further work could be done in designing the algorithm to select the best bandwidth