

Hailstone Sequence

The purpose of this exercise is to write the user-defined **R** function `hailstoneseq.m` that takes as an input a positive integer N , generates values in the recurrence relation $f(k)$, where

$$f(k) = \begin{cases} k & \text{if } k = 1 \\ 3f(k-1) + 1 & \text{if } k \text{ is odd} \\ \frac{f(k-1)}{2} & \text{if } f(k-1) \text{ is even} \end{cases}$$

until $f(k) = 1$, and plots and returns the vector $(f(1), f(2), \dots, f(k))$.

In words, here's how the sequence is generated:

Take any natural number N . If N is even, divide it by 2 to get $N/2$. If N is odd, multiply it by 3 and add 1. Repeat the process until the number equals 1.

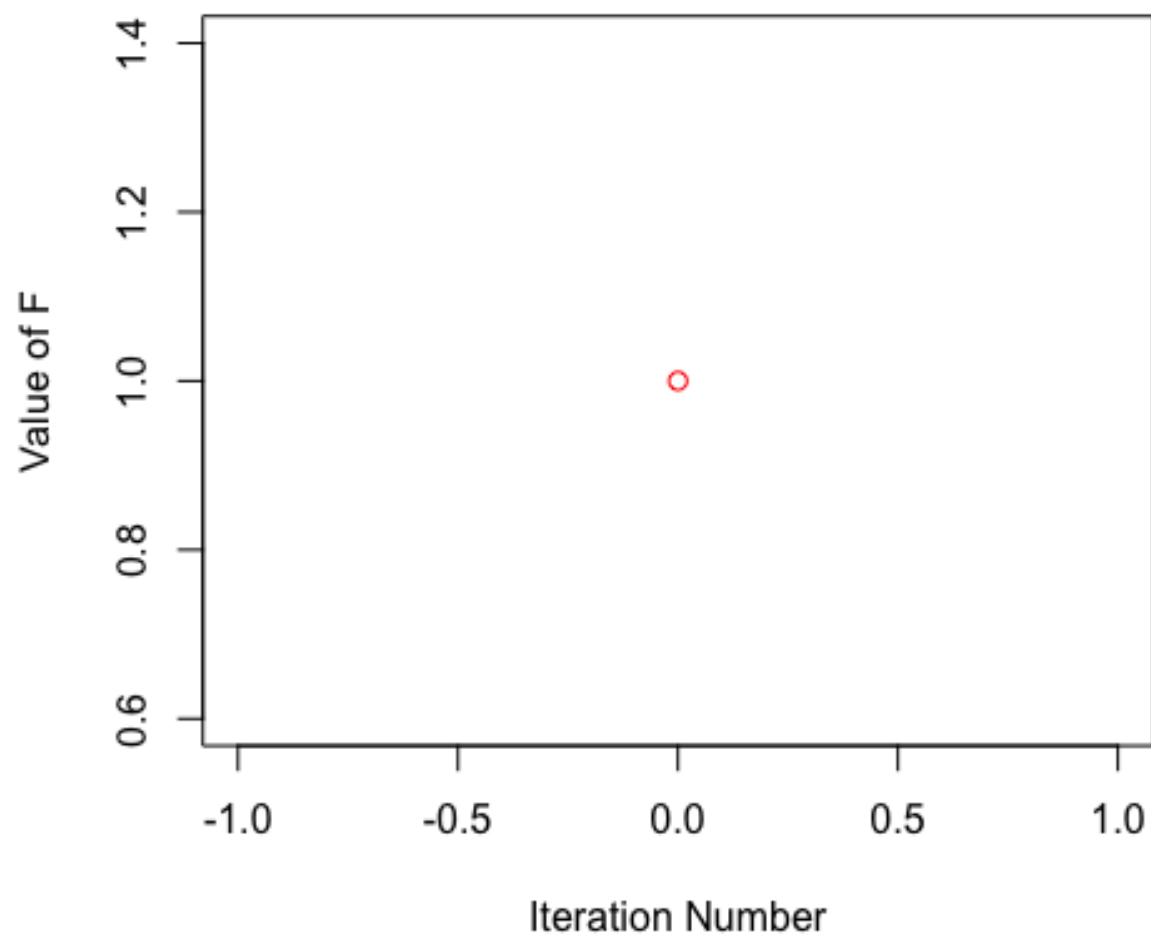
The sequence that is generated is known as the “Hailstone Sequence,” and the “Collatz Conjecture” is that no matter what N is, eventually, you will end up with 1. It has not been proven for all positive integers N . The “Collatz Graph” pictured on the last page shows all starting values N that reach 1 in twenty iterations or fewer.

The function should give an error message and return NA when the user inadvertently enters a value of N that is not a positive integer. The plot of the hailstone sequence should begin at 0, not 1. Note that there is a special case when $n = 1$.

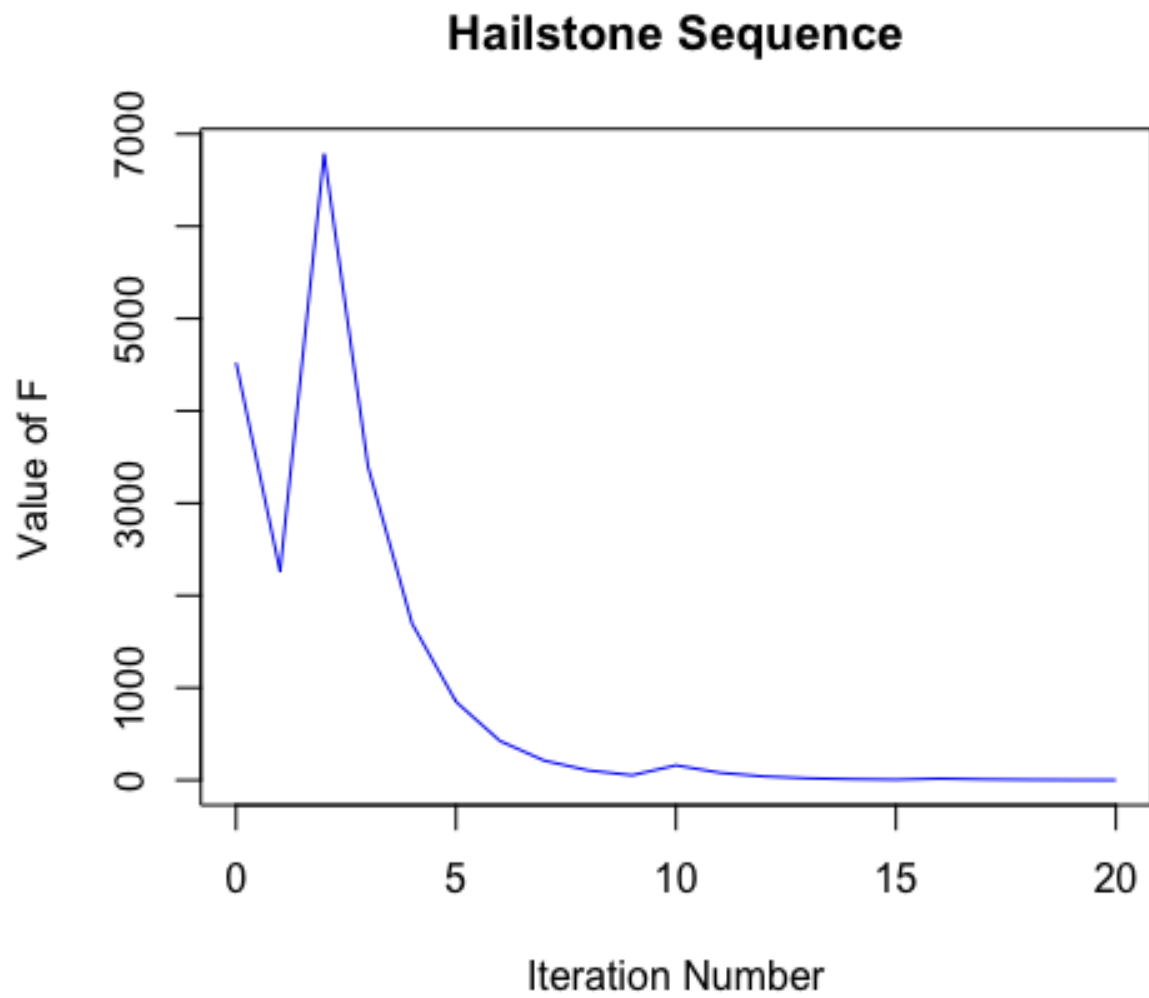
Here are several examples and their associated plots.

```
> hailstone(0)
Error, N must be a natural number.
[1] NA
> hailstone(5.6)
Error, N must be a natural number.
[1] NA
> hailstone(-3)
Error, N must be a natural number.
[1] NA
> hailstone(-8.1)
Error, N must be a natural number.
[1] NA
> hailstone(-1)
Error, N must be a natural number.
[1] NA
> hailstone(1)
[1] 1
```

Hailstone Sequence



```
> hailstone(4522)
[1] 4522 2261 6784 3392 1696 848 424 212 106 53 160 80 40
[14] 20 10 5 16 8 4 2 1
```



```

> hailstone(2018)
[1] 2018 1009 3028 1514 757 2272 1136 568 284 142 71 214 107
[14] 322 161 484 242 121 364 182 91 274 137 412 206 103
[27] 310 155 466 233 700 350 175 526 263 790 395 1186 593
[40] 1780 890 445 1336 668 334 167 502 251 754 377 1132 566
[53] 283 850 425 1276 638 319 958 479 1438 719 2158 1079 3238
[66] 1619 4858 2429 7288 3644 1822 911 2734 1367 4102 2051 6154 3077
[79] 9232 4616 2308 1154 577 1732 866 433 1300 650 325 976 488
[92] 244 122 61 184 92 46 23 70 35 106 53 160 80
[105] 40 20 10 5 16 8 4 2 1

```

Hailstone Sequence

