

A Run-Group Proposal Submitted to PAC 44

Measurement of Deep Exclusive π^- Production using a Transversely Polarized ^3He Target and the SoLID Spectrometer

DRAFT: May 20, 2016

J. Arrington, K. Hafidi, P. Reimer, Z. Ye*

Argonne National Laboratory, Physics Division, Argonne, IL, USA

Z. Ahmed*, S. Basnet, G.M. Huber[†], W. Li, D. Paudyal, Z. Papandreou

University of Regina, Regina, SK, Canada

K. Aniol

California State University – Los Angeles, Los Angeles, CA, USA

M. Boer

Los Alamos National Laboratory, Physics Division, Los Alamos, NM, USA

A. Camsonne, J-P. Chen, D. Gaskell

Jefferson Lab, Newport News, VA, USA

D. Dutta, L. Ye

Mississippi State University, Mississippi State, MS, USA

H. Gao, X. Li, T. Liu, C. Peng, W. Xiong, X.F. Yan, Z. Zhao

Duke University, Durham, NC, USA

C. E. Hyde, F.R. Wesselmann

Old Dominion University, Norfolk, VA, USA

P. Markowitz

Florida International University, Miami, FL, USA

V. Sulkosky

University of Virginia, Charlottesville, VA, USA

E. Voutier

Institut de Physique Nucléaire IN2P3/CNRS, Université Paris Sud, Orsay, France

[†] Contact person , * Spokesperson

Contents

1	Scientific Justification	4
1.1	Generalized Parton Distributions and Contribution from the Pion Pole	4
1.2	Single spin asymmetry in exclusive pion electroproduction	6
1.3	The Complementarity of Separated and Unseparated Asymmetry Measurements	8
2	Experimental Method	13
2.1	Transversely Polarized ^3He Target	13
2.2	SoLID Spectrometer and Detectors	14
2.3	Recoil Proton Identification	15
2.4	Trigger Design	17
3	Projected Results	18
3.1	Kinematic Coverage	18
3.2	Estimated Rates	18
3.3	Asymmetry Projections	19
3.4	Missing Mass and Background	22
3.5	Systematic Uncertainties	23
4	Summary	24
A	Monte Carlo model of Deep Exclusive π^- Production from the Neutron in ^3He	25
A.1	Data Constraints	25
A.2	Model for Higher Q^2 Kinematics	26
A.3	Parametrization of σ_L , σ_T , σ_{LT} , & σ_{TT}	26
A.4	Single Spin Asymmetry (SSA) \mathbf{A}_L^\perp	27
A.5	Target Neutron Fermi Momentum	27

Abstract

We propose to measure the transverse nucleon, single-spin asymmetry $A_{UT}^{sin(\phi-\phi_s)}$ in the exclusive $\bar{n}(e, e' \pi^-)p$ reaction, during the transversely polarized ^3He target SIDIS experiment (i.e. E12-10-006 [1]) with SoLID [2]. This polarization observable has been noted as being sensitive to the spin-flip generalized parton distribution (GPD) \tilde{E} , and factorization studies have indicated that precocious scaling is likely to set in at moderate $Q^2 \sim 2 - 4 \text{ GeV}^2$, as opposed to the absolute cross section, where scaling is not expected until $Q^2 > 10 \text{ GeV}^2$. Furthermore, this observable has been noted as being important for the reliable extraction of the charged pion form factor from pion electroproduction. The asymmetry data are projected to be of much higher quality than a pioneering measurement by HERMES [3].

This measurement is complementary to a proposal reviewed by PAC39 [4] for the SHMS+HMS in Hall C. The asymmetry that is most sensitive to \tilde{E} is the longitudinal photon, transverse nucleon, single-spin asymmetry A_L^\perp in exclusive charged pion electroproduction. The SHMS+HMS allow the L-T separation needed to reliably measure this quantity. However, the limited detector acceptance and the error-magnification inherent in an L-T separation necessitates the use of a next generation, externally polarized, continuous flow, high luminosity $^3\tilde{\text{He}}$ target based on a large volume polarizer and compressor being developed at the University of New Hampshire.

A wide $-t$ coverage is needed to obtain a good understanding of the asymmetry. Thus, it has always been intended to complement the SHMS+HMS A_L^\perp measurement with an unseparated $A_{UT}^{sin(\phi-\phi_s)}$ measurement using a large solid angle detector. The high luminosity capabilities of SoLID make it well-suited for this measurement. Since an L-T separation is not possible with SoLID, the observed asymmetry is expected to be diluted by the ratio of the longitudinal cross section to the unseparated cross section. This was also true for the pioneering HERMES measurements, which provided a valuable constraint to models for the \tilde{E} GPD. Simultaneously, the $A_{UT}^{sin(\phi_s)}$ asymmetry will be measured, which provides valuable information on transverse photon contributions at small $-t$.

In order to assure a clean measurement of exclusive π^- production, it is required to detect the recoil proton from the $\bar{n}(e, e' \pi^-)p$ reaction. We propose to analyze the E12-10-006 event files off-line to look for $e - \pi^- - p$ triple coincidence events in SoLID for the case where the proton is emitted $8^\circ < \theta < 24^\circ$. This has no impact upon E12-01-006 whatsoever, and yields valuable unseparated asymmetry data.

1 Scientific Justification

1.1 Generalized Parton Distributions and Contribution from the Pion Pole

In recent years, much progress has been made in the theory of generalized parton distributions (GPDs). Unifying the concepts of parton distributions and of hadronic form factors, they contain a wealth of information about how quarks and gluons make up hadrons. The key difference between the usual parton distributions and their generalized counterparts can be seen by representing them in terms of the quark and gluon wavefunctions of the hadron. While the usual parton distributions are obtained from the squared hadron wavefunction representing the probability to find a parton with specified polarization and longitudinal momentum fraction x in the fast moving hadron (Fig. 1a), GPDs represent the interference of different wavefunctions, one where the parton has momentum fraction $x + \xi$ and one where this fraction is $x - \xi$ (Fig. 1b). GPDs thus correlate different parton configurations in the hadron at the quantum mechanical level. A special kinematic regime is probed in deep exclusive meson production, where the initial hadron emits a quark-antiquark or gluon pair (Fig. 1c). This has no counterpart in the usual parton distributions and carries information about $q\bar{q}$ and gg -components in the hadron wavefunction.

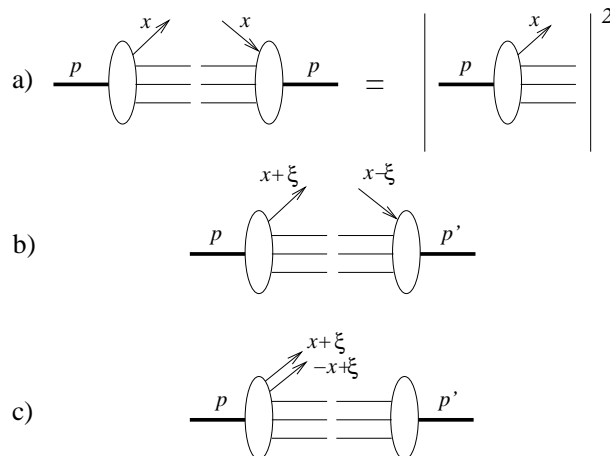


Figure 1: (a) Usual parton distribution, representing the probability to find a parton with momentum fraction x in the nucleon. (b) GPD in the region where it represents the emission of a parton with momentum fraction $x + \xi$ and its reabsorption with momentum fraction $x - \xi$. (c) GPD in the region where it represents the emission of a quark-antiquark pair, and has no counterpart in the usual parton distributions. This figure has been adapted from Ref. [5].

Apart from the momentum fraction variables x and ξ , GPDs depend on the four momentum transfer t . This is an independent variable, because the momenta p and p' may differ in either their longitudinal or transverse components. GPDs thus interrelate the longitudinal and transverse momentum structure of partons within a fast moving hadron.

In order to access the physics contained within GPDs, one is restricted to the hard scattering regime. An important feature of hard scattering reactions is the possibility to separate clearly the perturbative and non-perturbative stages of the interaction. Qualitatively speaking, the presence of a hard probe allows one to create small size quark-antiquark and gluon configurations, whose interactions are described by perturbative QCD (pQCD). The non-perturbative stage of the reaction describes how the hadron reacts to this configuration, or how this probe is transformed into hadrons. This separation is the so-called factorization property

of hard reactions. Deep Exclusive Meson electro-Production (DEMP) was first shown to be factorizable in Ref. [6]. This factorization applies when the virtual photon is longitudinally polarized, which is more probable to produce a small size configuration compared to a transversely polarized photon.

GPDs are universal quantities and reflect the structure of the nucleon independently of the reaction which probes the nucleon. At leading twist-2 level, the nucleon structure information can be parameterized in terms of four quark chirality conserving GPDs, denoted H , E , \tilde{H} and \tilde{E} . H and E are summed over quark helicity, while \tilde{H} and \tilde{E} involve the difference between left and right handed quarks. H and \tilde{H} conserve the helicity of the proton, while E and \tilde{E} allow for the possibility that the proton helicity is flipped. Because quark helicity is conserved in the hard scattering regime, the produced meson acts as a helicity filter. In particular, leading order QCD predicts that vector meson production is sensitive only to the unpolarized GPDs, H and E , whereas pseudoscalar meson production is sensitive only to the polarized GPDs, \tilde{H} and \tilde{E} . In contrast, deeply virtual Compton scattering (DVCS) depends at the same time on both the polarized (\tilde{H} and \tilde{E}) and the unpolarized (H and E) GPDs. This makes DEMP reactions complementary to the DVCS process, as it provides an additional tool to disentangle the different GPDs [7].

Besides coinciding with the parton distributions at vanishing momentum transfer ξ , the GPDs have interesting links with other nucleon structure quantities. Their first moments are related to the elastic form factors of the nucleon through model-independent sum rules [8]:

$$\sum_q e_q \int_{-1}^{+1} dx H^q(x, \xi, t) = F_1(t), \quad (1)$$

$$\sum_q e_q \int_{-1}^{+1} dx E^q(x, \xi, t) = F_2(t), \quad (2)$$

$$\sum_q e_q \int_{-1}^{+1} dx \tilde{H}^q(x, \xi, t) = G_A(t), \quad (3)$$

$$\sum_q e_q \int_{-1}^{+1} dx \tilde{E}^q(x, \xi, t) = G_P(t), \quad (4)$$

where e_q is the charge of the relevant quark, $F_1(t)$, $F_2(t)$ are the Dirac and Pauli elastic nucleon form factors, and $G_A(t)$, $G_P(t)$ are the isovector axial and pseudoscalar nucleon form factors. The t -dependence of $G_A(t)$ is poorly known, and although $G_P(t)$ is an important quantity, it remains highly uncertain because it is negligible at the momentum transfer of β -decay [9]. Because of partial conservation of the axial current (PCAC), $G_P(t)$ alone receives contributions from $J^{PG} = 0^{--}$ states [10], which are the quantum numbers of the pion, and so \tilde{E} contains an important pion pole contribution (Fig. 2a).

Accordingly, Refs. [11, 12] have adopted the pion pole-dominated ansatz

$$\tilde{E}^{ud}(x, \xi, t) = F_\pi(t) \frac{\theta(\xi > |x|)}{2\xi} \phi_\pi\left(\frac{x + \xi}{2\xi}\right), \quad (5)$$

where $F_\pi(t)$ is the pion electromagnetic form factor, and ϕ_π is the pion distribution amplitude. For the kinematic region accessible until the construction of the EIC, the best estimate of \tilde{E} is obtained if one replaces the perturbative (or one-gluon exchange) expression for F_π with a parameterization based on the experimental form factor [13]. Regardless of which expression is used, \tilde{E} cannot be related to already known parton distributions, and so experimental information about \tilde{E} via DEMP can provide new information on nucleon structure which is unlikely to be available from any other source.

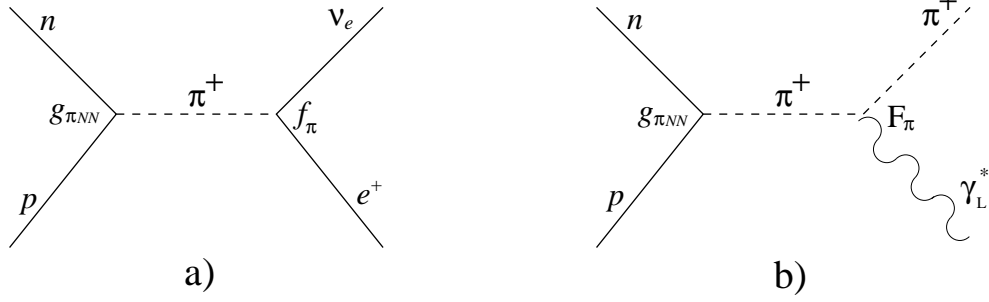


Figure 2: (a) Pion pole contribution to $G_P(t)$, and hence to \tilde{E} . (b) Pion pole contribution to meson electroproduction at low $-t$.

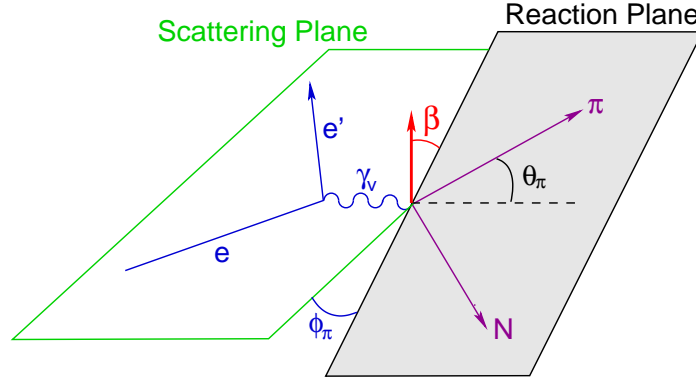


Figure 3: Scattering and hadronic reaction planes for exclusive $\tilde{N}(e, e'\pi)N'$. β is the angle between the target nucleon polarization vector and the reaction plane. Some works alternatively label this angle as $(\phi - \phi_s)$.

1.2 Single spin asymmetry in exclusive pion electroproduction

Frankfurt et al. [14] have considered a specific polarization observable which is the most sensitive observable to probe the spin-flip \tilde{E} . This variable is the single-spin asymmetry for exclusive charged pion production, $\vec{p}(e, e'\pi^+)n$ or $\vec{n}(e, e'\pi^-)p$, from a transversely polarized nucleon target, and is defined [12] as

$$A_L^\perp = \left(\int_0^\pi d\beta \frac{d\sigma_L^\pi}{d\beta} - \int_\pi^{2\pi} d\beta \frac{d\sigma_L^\pi}{d\beta} \right) \left(\int_0^{2\pi} d\beta \frac{d\sigma_L^\pi}{d\beta} \right)^{-1}, \quad (6)$$

where $d\sigma_L^\pi$ is the exclusive charged pion electroproduction cross section using longitudinally polarized photons and β is the angle between the nucleon polarization vector and the reaction plane (Fig. 3).

This asymmetry is related to the parton-helicity-conserving part of the scattering process and is sensitive to the interference between \tilde{H} and \tilde{E} [14, 15]:

$$A_L^\perp = \frac{\sqrt{-t'}}{m_p} \frac{\xi \sqrt{1 - \xi^2} \text{Im}(\tilde{E}^* \tilde{H})}{(1 - \xi^2) \tilde{H}^2 - \frac{t\xi^2}{4m_p} \tilde{E}^2 - 2\xi^2 \text{Re}(\tilde{E}^* \tilde{H})}. \quad (7)$$

Frankfurt et al. [14] have shown that this asymmetry must vanish if \tilde{E} is zero. If \tilde{E} is not zero, the asymmetry will display a $\sin\beta$ dependence. Their predicted asymmetry using the \tilde{E} ansatz from Ref. [16] is shown in Fig. 4. This calculation is Q^2 -independent, depending only on how well the soft contributions cancel in the asymmetry.

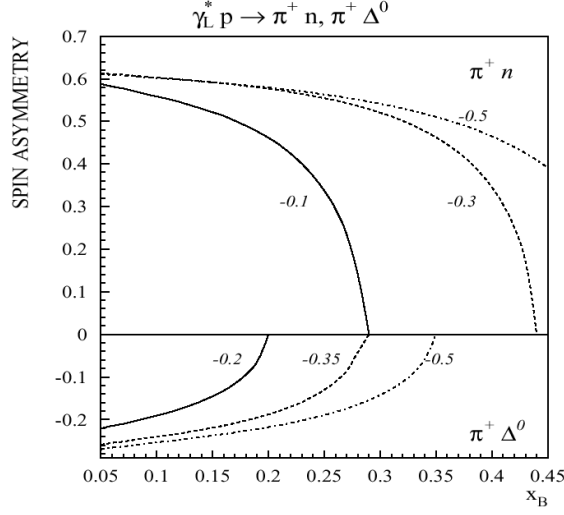


Figure 4: Transverse single-spin asymmetry for the longitudinal electroproduction of $\pi^+ n$ and $\pi^+ \Delta^0$ at different values of t [indicated on the curves in GeV^2]. The asymmetry drops to zero at the parallel kinematic limit, which is different for each t value, because the definition of β is ill-defined at this point. This figure is taken from Ref. [17].

It seems likely that a precocious factorization of the meson production amplitude into three parts – the overlap integral between the photon and pion wave functions, the hard interaction, and the GPD – will lead to a precocious scaling of A_L^\perp as a function of Q^2 at moderate $Q^2 \sim 2 - 4 \text{ GeV}^2$ [14]. This precocious scaling arises from the fact that higher twist corrections, which are expected to be significant at low Q^2 , will likely cancel when one examines the ratio of two longitudinal observables. In contrast, the onset of scaling for the absolute cross section is only expected for much larger values of $Q^2 > 10 \text{ GeV}^2$.

This point is made clear in Fig. 5. This figure shows renormalon model calculations [18] of both the asymmetry and the longitudinal cross section at $Q^2 = 4 \text{ GeV}^2$. While the magnitude of the cross section changes significantly when taking into account the twist-four corrections, A_L^\perp is essentially insensitive to them and displays the expected precocious scaling. The relatively low value of Q^2 for the expected onset of precocious scaling is important, because it will be experimentally accessible after the Jefferson Lab 12 GeV upgrade. This places A_L^\perp among the most important GPD measurements that can be made in the meson scalar. If precocious scaling cannot be experimentally demonstrated in this ratio of two cross sections, then it may not be possible to determine GPDs from DEMP data.

Refs. [7] and [17] also point out that the study of the transverse target single-spin asymmetry versus t is important for the reliable extraction of the pion form factor from electroproduction experiments (Fig. 2b). Investigations of hard exclusive π^+ electroproduction using a pQCD factorization model [19, 20] find that at $x_B = 0.3$ and $-t = -t_{min}$, the pion pole contributes about 80% of the longitudinal cross section. Since the longitudinal photon transverse single-spin asymmetry is an interference between pseudoscalar and pseudovector contributions, its measurement would help constrain the non-pole pseudovector contribution, and so assist the more reliable extraction of the pion form factor. The upper $Q^2 = 6 \text{ GeV}^2$ limit of the approved pion form factor measurements in the JLab 12 GeV program [21] is dictated primarily by the requirement $-t_{min} < 0.2 \text{ GeV}^2$, to keep non-pion pole contributions to σ_L at an acceptable level [20]. Transverse target single-spin asymmetry studies versus t may eventually allow, with theoretical input, the

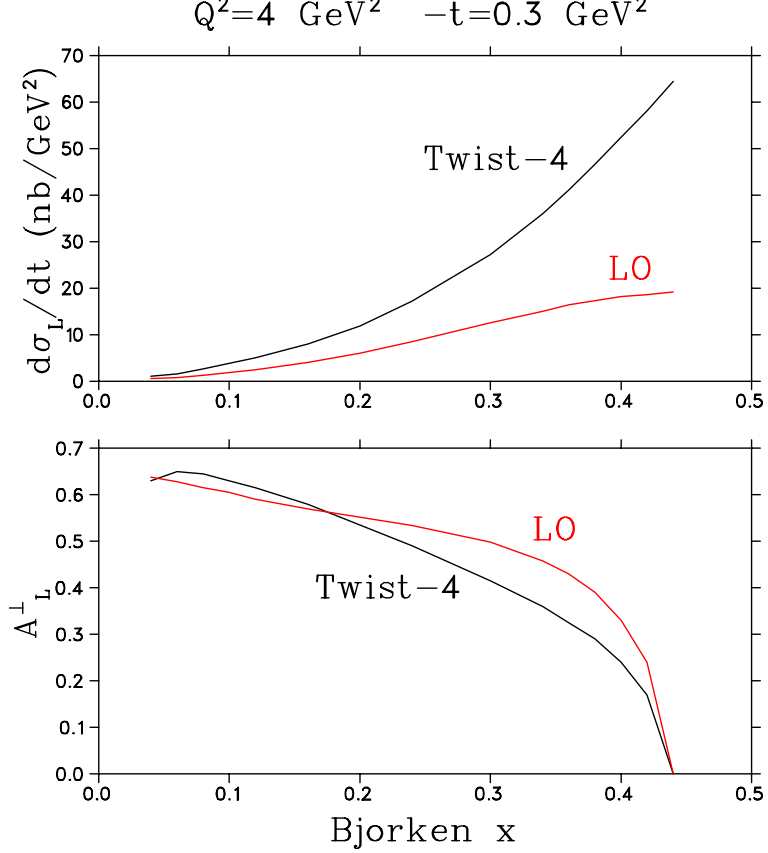


Figure 5: Calculation of the longitudinal photon transverse nucleon spin asymmetry including twist-four corrections by A. Belitsky [18] at $-t = 0.3 \text{ GeV}^2$, $Q^2 = 4 \text{ GeV}^2$. The red curves are the leading order calculation, while the black curves have twist-four power effects taken into account. While the cross section is very sensitive to these corrections, the transverse spin asymmetry is stable.

use of somewhat larger $-t$ data for pion form factor measurements, ultimately extending the Q^2 -reach of pion form factor data acquired with JLab 12 GeV beam. Thus, measurements of the transverse single-spin asymmetry are a logical step in the support of the pion form factor program.

1.3 The Complementarity of Separated and Unseparated Asymmetry Measurements

The reaction of interest is ${}^3\text{He}(e, e'\pi^-)p(pp)_{sp}$. The measurement of the transverse single-spin asymmetry requires the detection of the π^- in non-parallel kinematics. It is the component of the target polarization parallel to $\hat{q} \times \hat{p}_\pi$ that is important, and this direction is uniquely defined only in non-parallel kinematics.

Experimentally, the angle between the target polarization and the reaction plane, β , and the angle between the scattering and reaction planes, ϕ , are not independent. If the target polarization is at some angle, ϕ_s , relative to the scattering plane, then $\beta = \phi_s - \phi$. The polarized nucleon cross section can be

expressed [22] in terms of these variables as:

$$\begin{aligned}
\sigma_t = & -P_\perp \sin \beta [\sigma_{TT}^y + 2\epsilon \sigma_L^y] \\
& - P_\perp \sin \beta [\epsilon(\cos 2\phi_s \cos 2\beta + \sin 2\phi_s \sin 2\beta) \sigma_{TT'}^y] \\
& - P_\perp \sin \beta \left[\sqrt{2\epsilon(1+\epsilon)}(\cos \phi_s \cos \beta + \sin \phi_s \sin \beta) \sigma_{LT}^y \right] \\
& - P_\perp \cos \beta \left[\sqrt{2\epsilon(1+\epsilon)}(\sin \phi_s \sin \beta - \cos \phi_s \cos \beta) \sigma_{LT}^x \right] \\
& - P_\perp \cos \beta [\epsilon(\sin 2\phi_s \sin 2\beta - \cos 2\phi_s \cos 2\beta) \sigma_{TT}^x]. \quad (8)
\end{aligned}$$

From the above equation, it is clear that to extract A_L^\perp it is necessary to first isolate the $\sin \beta$ Fourier component of the polarized nucleon cross section. Once that has been accomplished, one must then separate the σ_L^y term from the σ_{TT}^y term via a Rosenbluth-type separation.

It has not yet been possible to perform an experiment to measure A_L^\perp . The conflicting experimental requirements of transversely polarized target, high luminosity, L-T separation, and closely controlled systematic uncertainty, make this an exceptionally challenging observable to measure. The SHMS+HMS is the only facility with the necessary resolution and systematic error control to allow a measurement of A_L^\perp . However, the beamtime required to do a good measurement with current polarized target technology is in the range of 10^3 days. To minimize the beamtime required, PR12-12-005 [4] proposed the use of a next generation, externally polarized, continuous flow, high luminosity ^3He target based on a large volume polarizer and compressor developed at the University of New Hampshire. The science case for this measurement was favorably reviewed by PAC39, and they encouraged the continued development of the target technology. Although the New Hampshire group is making continued progress on the development of the target, there is no timeline for its actual implementation at Jefferson Lab.

The most closely related measurement, of the transverse single-spin asymmetry in exclusive π^+ electroproduction without an L-T separation, was published by the HERMES Collaboration in 2010 [3]. Their data were obtained for average values of $\langle x_B \rangle = 0.13$, $\langle Q^2 \rangle = 2.38 \text{ GeV}^2$ and $\langle t' \rangle = -0.46 \text{ GeV}^2$, subject to the criterion $W^2 > 10 \text{ GeV}^2$. The six Fourier amplitudes in terms of the azimuthal angles ϕ , ϕ_s of the pion-momentum and proton-polarization vectors relative to the lepton scattering plane were determined. Of these, at leading twist only the $\sin(\phi - \phi_s)_{UT}$ Fourier amplitude receives a contribution from longitudinal photons. If one assumes that longitudinal contributions dominate, these $A_{UT}^{\sin(\phi - \phi_s)}$ values can be compared to GPD models for \tilde{E} , \tilde{H} .

Because transverse photon amplitudes are suppressed by $1/Q$, at very high Q^2 it is safe to assume that all observed meson production is due to longitudinal photons. At the lower Q^2 typical of the JLab and HERMES programs, however, this is not the case. Handbag-approach calculations by Goloskokov and Kroll [13] indicate much of the unseparated cross section measured by HERMES [3] is due to contributions from transversely polarized photons. In addition, there are contributions to $A_{UT}^{\sin(\phi - \phi_s)}$ from the interference between two amplitudes, both for longitudinal photons, as well as transverse photons [15]. At the amplitude level, the transverse suppression is given by μ/Q , where $\mu \sim 2 \text{ GeV}$ is a mass parameter given by the pion mass enhanced by the large ratio between the pion mass and the sum of the u and d current quark masses (chiral condensate). For experimentally accessible Q^2 , hardly any suppression of the twist-3 contribution is expected. As indicated in Fig. 6, the contribution from transverse photons tends to make the asymmetry smaller. At the HERMES kinematics, the dilution caused by transverse photons is about 50%. Although

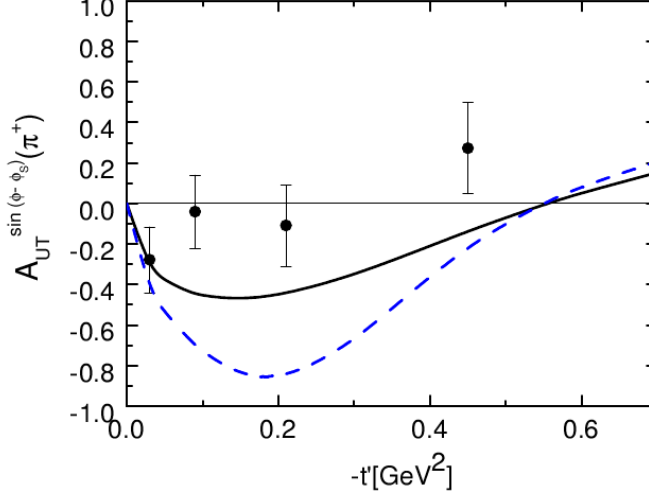


Figure 6: Predictions by Goloskokov and Kroll for the $\sin(\phi - \phi_s)$ moment of A_{UT} in the handbag approach, in comparison to the data from HERMES at $Q^2 = 2.45 \text{ GeV}^2$, $W = 3.99 \text{ GeV}$. The independent variable is $-t' = |t - t_{min}|$. Dashed line: contribution from longitudinal photons only. Solid line: full calculation including both transverse and longitudinal photons. This figure is taken from Ref. [13].

the observed unseparated asymmetry is small, the HERMES data are consistent with GPD models based on the dominance of \tilde{E} over \tilde{H} at low $-t'$, due to the pion pole. An improved measurement of the transverse target spin asymmetry, in particular the $\sin(\phi - \phi_s)$ modulation, is clearly a high priority.

A run-group proposal concurrent with the SoLID transversely polarized ^3He SIDIS experiment allows for an unseparated asymmetry measurement to be obtained on a sooner timescale than the Hall C measurement. In comparison to the HERMES measurement, the experiment proposed here will probe higher Q^2 and x_B , with much smaller statistical errors over a wider range of $-t$. SoLID will allow the first measurement for $Q^2 > 4 \text{ GeV}^2$, where GPD-based calculations are expected to apply. Thus, the measurements should be more readily interpretable than those from HERMES. Similar measurements using CLAS-12 and a transversely polarized ^1H target have been discussed previously [23], but this measurement will allow for smaller statistical uncertainties, due to SoLID's higher luminosity capabilities.

Handbag model calculations by Goloskokov and Kroll [24] shed further light on the expected asymmetry dilution. The bottom panel of Fig. 7 shows their predictions for the cross section components in exclusive charged pion production. Although their calculations tend to underestimate the σ_L values measured in the JLab $F_\pi - 2$ experiment [25], their model is in reasonable agreement with the unseparated cross sections [13]. They predict significant transverse contributions for JLab kinematics. A comparison of the unseparated asymmetry at $-t = 0.3 \text{ GeV}^2$, $x_B = 0.365$ in Fig. 7 with the separated longitudinal asymmetry at the same values of x_B , $-t$ in Fig. 5 indicates a substantial dilution of the unseparated asymmetry due to transverse photon contributions, similar to that observed in Fig. 6.

In addition to allowing a measurement at $Q^2 > 4 \text{ GeV}^2$, a measurement by SoLID of $A_{UT}^{\sin(\phi - \phi_s)}$ will cover a fairly large range of $-t$, allowing the asymmetry to be mapped over its full range with good statistical uncertainties – from its required zero-value in parallel kinematics, through its maximum, and then back to near-zero or even positive at larger $-t$. The shape of the asymmetry curve versus $-t$, as well as its maximum

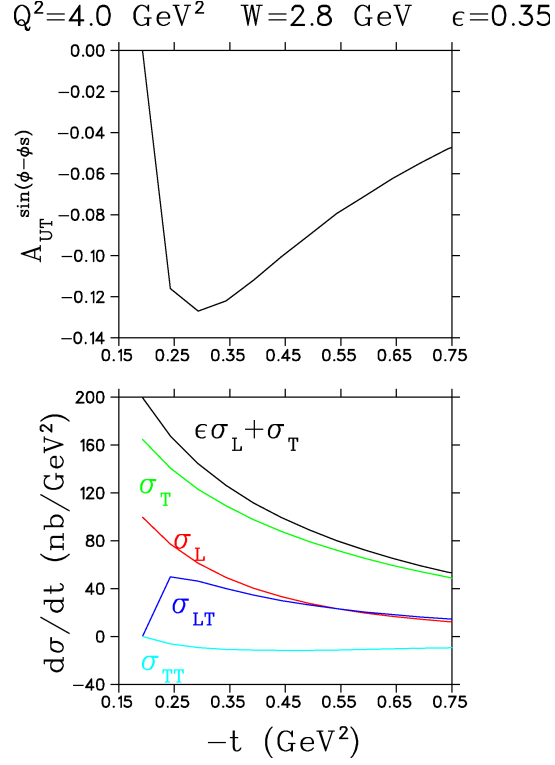


Figure 7: Calculation of the cross section components and $\sin(\phi - \phi_s)$ moment of the transverse nucleon spin asymmetry A_{UT} in the handbag approach by Goloskokov and Kroll [24] for kinematics similar to those in Fig. 5. Our measurement will be at higher $0.55 < \epsilon < 0.75$ than the $\epsilon = 0.35$ kinematics of this figure, so the dilution in the asymmetry will be significantly less.

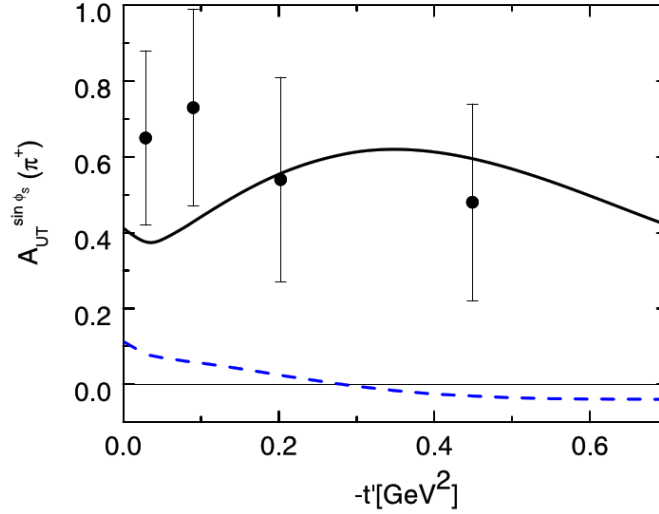


Figure 8: Data from HERMES for the $\sin(\phi_s)$ moment with a transversely polarized target at $Q^2 = 2.45 \text{ GeV}^2$, $W = 3.99 \text{ GeV}$. The solid line is the prediction of the handbag calculation by Goloskokov and Kroll; the dashed line is obtained disregarding the twist-3 contribution. This figure is taken from Ref. [13].

value, are critical information for comparison to GPD-based models.

Simultaneously, the $\sin(\phi_S)_{UT}$ moment can be extracted, which may be interpretable in terms of transversity GPDs. Any model that describes exclusive pion production will need to describe not only the leading-twist Fourier amplitude $A_{UT}^{\sin(\phi-\phi_s)}$, but also these other contributions to the target-spin azimuthal asymmetry, providing additional GPD model constraints. Independent of a specific dynamical interpretation (e.g. the handbag approach), the $A_{UT}^{\sin(\phi_s)}$ asymmetry will say something on the strength of the contributions from transverse photons at small $-t$:

$$A_{UT}^{\sin(\phi_s)} \sim \text{Im}[M_{0+++}^* M_{0-0+} - M_{0-++}^* M_{0+0+}], \quad (9)$$

where the helicities are in the order: pion neutron photon proton [13]. Thus, in contrast to the $\sin(\phi - \phi_S)$ modulation, which has contributions from LL and TT interferences, the $\sin(\phi_s)$ modulation measures only the LT interference. The first term is proportional to t' , as is forced by angular momentum conservation, while the second one is not forced to vanish [24]. Indeed, HERMES measured the $\sin(\phi_s)$ modulation to be large and apparently nonzero at $-t' = 0$ (Fig. 8). Hence, both the amplitudes M_{0-++} and M_{0+0+} must be large, giving the first clear signal for strong contributions from transversely polarized photons at rather large values of W and Q^2 [13]. This is very interesting in its own right.

In the longer term, the measurement presented in this proposal is important preparatory work for future measurements at the EIC. The Electron-Ion Collider is optimized for transverse single spin asymmetry measurements such as these, and the ability to have both polarized ^3He and proton beams will allow $A_{UT}^{\sin(\phi-\phi_s)}$ to be directly compared for the $\vec{n}(e, e'\pi^-)p$ and $\vec{p}(e, e'\pi^+)n$ reactions, without target dilution, over a broad kinematic range. In the meantime, the proposed measurement with SoLID is our best short-term opportunity to considerably advance over the pioneering HERMES data.

2 Experimental Method

We propose to carry out the ${}^3\text{He}(e, e'\pi^-)p(pp)_{sp}$ measurement using the Solenoidal Large Intensity Device (SoLID [2]), in parallel with the already approved experiment, E12-10-006 [1], which will measure Semi-Inclusive Deep-Inelastic Scattering (SIDIS). Our discussion will concentrate on the region of clearest physics interpretation ($Q^2 > 4 \text{ GeV}^2$), even though lower Q^2 events will also be contained in the experimental data-set.

There are two SoLID configurations, called SoLID-SIDIS and SoLID-PVDIS. Besides E12-10-006, two SIDIS experiments, E12-11-007 [26] and E12-11-108 [27], along with the J/ψ experiment (E12-12-006 [28]), will use the SoLID-SIDIS configuration as well. All of these experiments have been approved with A or A-rating. In addition, two “bonus-run” experiments, E12-10-006A [29] and E12-11-108A [30], have also been approved to run in parallel with the SIDIS experiments. The SoLID-PVDIS configuration is for the Parity Violation in Deep Inelastic Scattering (PVDIS) [31].

In order to assure a clean measurement of exclusive π^- production, it is required to detect the recoil proton from the $\vec{n}(e, e'\pi^-)p$ reaction. The existing SoLID detectors already have the capabilities of detecting protons from 8° up to 24° , while the main proton events from the DEMP process can cover 0° up to 50° . The experiment will use exactly the same setup and online production trigger as E12-10-006, which is the coincidence of electron triggers and hadron triggers from SoLID. We will perform the offline analysis to identify the recoil protons from DEMP and form the triple coincidence events together with electrons and π^- provided by SIDIS triggers. The discussion of proton detection will be given in Section 2.3.

2.1 Transversely Polarized ${}^3\text{He}$ Target

Target	${}^3\text{He}$
Length	40 cm
Target Polarization	$\sim 60\%$
Target Spin Flip	≤ 20 mins
Target Dilution	90%
Effective Neutron	86.5%
Target Polarimetry Accuracy	$\sim 3\%$

Table 1: Key Parameters of the ${}^3\text{He}$ target.

The proposed measurement will utilize the same polarized ${}^3\text{He}$ target as E12-10-006 [1]. Such a target was successfully employed in E06-110, a 6 GeV SIDIS experiment in Hall A. A wide range of experiments have utilized polarized ${}^3\text{He}$ as an effective neutron target over a wide range of kinematics. And over the past decades several authors have calculated the effective neutron polarization in ${}^3\text{He}$ using three-nucleon wave functions and various models of the $N - N$ interaction [32]. These are now well established, and the error introduced by uncertainty in the wave functions are small.

Other nuclear effects which can influence the experimental asymmetry for a neutron bound inside ${}^3\text{He}$ include Fermi motion, off-shell effects, meson exchange currents, delta isobar contributions and π^- final state interactions. The exclusive nature of the process, the selected kinematics such as high Q^2 , large recoil

momentum and a complete coverage of the azimuthal angle ϕ ensures that corrections due to these nuclear effects will be small and can be modeled effectively.

The ^3He polarization direction is held by three sets of Helmholtz coils with a 25 Gauss magnetic field. Both the transverse and longitudinal directions can be provided by rotating the magnetic field. The ^3He gas, with density of about 10 atm (at 0°C), is stored in a 40 cm target cell made of thin glasses. With a $15\ \mu\text{A}$ electron beam, the neutron luminosity can be as high as $10^{36}\ \text{cm}^{-2}\text{s}^{-1}$. In-beam polarization of 60% was archived during the E06-110 experiment. Two kinds of polarimetry, NMR and EPR, were used to measure the polarization with relative 5% precision. We have plans to improve the accuracy of the measurement to reach 3%.

The target spin will be reversed for every 20 minutes by using the RF AFP technique. The additional polarization loss due to the spin reversal was kept at $< 10\%$, which has been taken into account in the overall 60% in-beam polarization. A new method for spin reversal using field rotation has been tested and was able to eliminate the polarization loss. Such an improvement will enable us to perform the spin-reversal in few minutes to reduce the target-spin-correlated systematic errors. The key parameters of the ^3He target are summarized in Table 1.

A collimator, similar to the one used in the E06-110, will be placed next to the target cell window to minimize the target cell contamination and to reduce the event rate. Several calibration targets will also be installed in this target system, including a multi-foil ^{12}C for optics study, a BeO target for beam tuning, and a reference target cell for dilution study and other calibration purposes.

2.2 SoLID Spectrometer and Detectors

The solenoid magnet for SoLID will be based on the CLEO-II magnet built by Cornell University. The magnet is 3 meters long with an outer diameter of 3 meters and an inner diameter of 1 meter. The field strength is greater than 1.35 Tesla, with an integrated BDL of 5 Tesla-meters. The fringe field at the front end after shielding is less than 5 Gauss. In the SIDIS-configuration, the CLEO-II magnet provides 2π acceptance in the azimuthal angle (ϕ) and covers polar angle (θ) from 8° up to 24° . The momentum acceptance is between 0.8 and 7.5 GeV/c for electrons and for hadrons, the momentum can be lower depending on the trigger efficiency. The momentum resolution is about 2%.

The layout of the SoLID detectors in the SIDIS-configuration is shown in Fig. 9. The detector system is divided into two regions for the forward-angle (FA) detection and the large-angle (LA) detection. Six tracking chambers based on Gas Electron Multipliers (GEM) will be used for charged particle tracking in the forward-angle region, and the first four of them will be shared by the large-angle region. In each region, a Shashlyk-type sampling EM calorimeter (LAEC or FAEC) will measure the particle energy and identify electrons from hadrons. A scintillator-pad detector (LASPD and FASPD) will be installed in front of each EC to reject photons and provide timing information. The forward-angle detectors will detect both the electrons and hadrons (mainly π^\pm). A light-gas Čerenkov detector (LGC) and a heavy-gas Čerenkov detector (HGC) will perform the e/π^\pm and π^\pm/K^\pm separation, respectively. The Multi-gas Resistive Plate Chamber (MRPC) will provide a precise timing measurement and serve as a backup of the FASPD on photon rejection. A more detailed discussion of the design, simulation, prototype-test of each detector is given in the SoLID preliminary conceptual design report (pCDR) [2].

Table 2 summarizes the key parameters of the detector system in the SIDIS configuration for both the

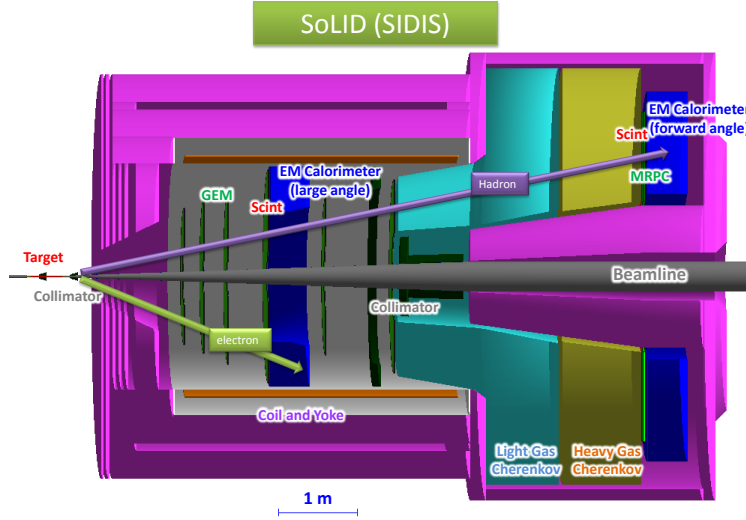


Figure 9: The Detector Layout of the SoLID-SIDIS configuration. The detector system includes six Gas Electron Multiplier (GEM) planes for charged particle tracking, two Scintillator Pad Detectors (SPD) followed by two Shashlyk sampling EM Calorimeters (EC) for energy measurement and particle identification, a Light Gas Čerenkov Detector (LGC) for $e-\pi^\pm$ separation, a Heavy Gas Čerenkov Detector (HGC) for $\pi^\pm-K^\pm$ separation, as well as a Multi-gap Resistive Plate Chamber (MRPC) for timing measurement. The first four GEM trackers, the first SPD (i.e. LASPD) and EC (i.e. LAEC) form the large-angle detection system for electron measurement. The forward-angle detection system, to measure electron and hadrons, is composed of all six GEM trackers, LGC, HGC, MRPC, the second SPD (i.e. FASPD) and the second EC (FAEC).

SIDIS and DEMP measurements.

2.3 Recoil Proton Identification

The cleanest way to identify the DEMP events is to detect all particles in the final state. The SoLID-SIDIS detector system has the capability of measuring electrons and pions, while protons can be isolated from other charged particles by using the time-of-flight (TOF) information. The TOF is provided by the timing detectors, including the MRPC and FASPD at the forward-angle detection region, and the LASPD at the large-angle detection region.

We examined the requirement of the timing resolution on these detectors by looking at the time difference between electrons and other heavier charged particles when they reach these detectors with the same momentum and flight path. As shown in the next section, the good protons from the DEMP reaction carry momenta from 0.3 GeV/c up to 1.2 GeV/c with angles from 0° to 50° . The FA-MRPC covers angles from 8° to 14.8° , and the angular range of the LASPD is from 16° to 24° . Hence we simulated events of electrons, pions, kaons and protons with the momentum from 0.3 GeV/c up to 1.2 GeV/c, and calculated the time when they reach two different detectors with linear trajectories and at fixed angles.

The results are shown in Fig. 10. To clearly identify two types of charged particles with the same momentum, we normally require the timing difference between two particles to be larger than 5 times of the overall timing resolution, while the SoLID timing detectors can reach the resolution in the range of 150 ps down to 50 ps. At the FA-MRPC, which is more than 7 meters from the target, protons come 3 ns later than

Experiments	SIDIS	DEMP
Reaction channel	$\vec{n}(e, e' \pi^\pm) X$	$\vec{n}(e, e' \pi^- p)$
Target	^3He	same
Unpolarized luminosity	$\sim 10^{37} \text{ cm}^{-2} \text{s}^{-1}$ per nucleon	same
Momentum coverage	0.8-7.5 (GeV/c) for e^-, π^\pm	same 0.3 1.2 (GeV/c) for protons
Momentum resolution	$\sim 2\%$	same
Azimuthal angle coverage	$0^\circ - 360^\circ$	same
Azimuthal angle resolution	5 mr	same
Polar angle coverage	8° - 24° for e 8° - 14.8° for π^\pm	same same 8° - 24° for p in SoLID 24° - 50° for p with recoil detector
Polar angle resolution	0.6 mr	same
Target Vertex resolution	0.5 cm	same
Energy resolution on ECs	5%~10%	same
Trigger type	Double Coincidence $e^- + \pi^\pm$	same (online) Triple Coincidence $e^- + \pi^- + p$ (offline)
Expected DAQ rates	<100 kHz	same (online)
Main Backgrounds	$^3\text{He}(e, e' K^\pm / \pi^0) X$ Accidental Coincidence	$^3\text{He}(e, e' \pi^\pm / K^\pm) X$ Accidental Coincidence
Key requirements	Radiation hardness Kaon Rejection DAQ	Proton Detection Exclusivity Timing Resolution

Table 2: Summary of Key Parameters for DEMP Measurement compared with SIDIS Experiments.

kaons, even at the highest momenta in the DEMP reaction. Hence, protons will be easily distinguished from other lighter particles. At the LA-SPD, which is about 3 meters away from the target, the time difference between protons and kaons is still more than 1 ns, which doesn't demand precise timing resolution.

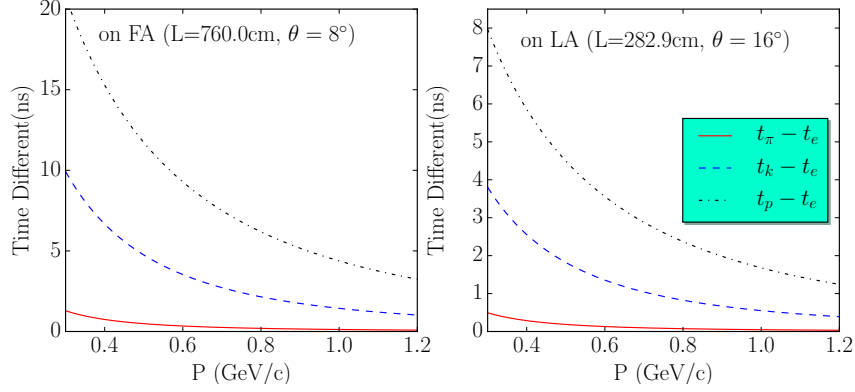


Figure 10: The time differences (in ns) between electrons and other charged particles, i.e. pions (red solid line), kaons (blue dashed line) and proton (black dash-dotted line), and their distributions as functions of particles' momentum at two different timing detectors, including the forward-angle (FA) MRPC and the large-angle (LA) SPD.

In general, the misidentified proton events can be mostly removed by cutting on the reconstructed missing quantities, e.g. angles, momenta and masses. The residual background will also be largely suppressed in the target-spin asymmetry extraction.

2.4 Trigger Design

In E12-10-006, the online production trigger will be the double-coincidence of the scattered electrons and hadrons. One will use the particle identification detectors, such as LGC, HGC and ECs, during the offline analysis to select π^\pm out from other hadrons. The DEMP events will be identified with the triple-coincidence of the scattered electron, π^- and proton, while the proton identification has been discussed above. We will use the same online trigger as the SIDIS one, and hence the new experiment will share exactly the same data-set as E12-10-006. The actual design of the SIDIS triggers will be far more complicated, and the detailed discussion of the trigger and DAQ designs is given in the SoLID pCDR [2].

3 Projected Results

To perform the simulation study and obtain the projected results, we used a DEMP generator, as discussed in Appendix-A, and generated events within a kinematic phase space slightly larger than the SoLID-SIDIS acceptance. The Fermi motion of the neutron in ^3He and the radiative effect have already been taken in account in this generator. Then for every detected particle in each event, we added the acceptance profiles obtained from the GEANT4 simulation with the SoLID-SIDIS configuration.

3.1 Kinematic Coverage

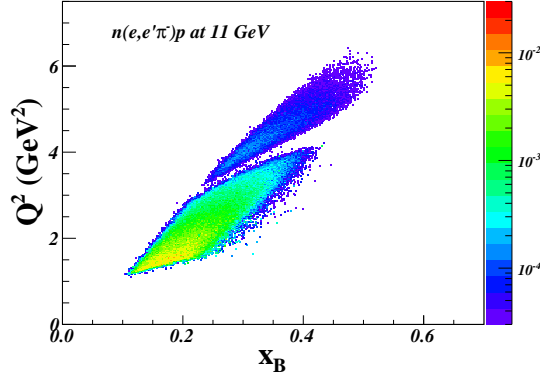


Figure 11: The kinematic coverage at different acceptances at 11 GeV. Colors correspond to rates (Hz) in log scale.

The kinematic coverage in Q^2 vs. x_B is shown in Fig. 11, using the existing SoLID detectors to detect protons at $8^\circ \sim 24^\circ$. These distributions were weighted by the DEMP unpolarized cross sections and the SoLID acceptance. As shown in these plots, the range of Q^2 is from 1.0 GeV^2 to 8.0 GeV^2 , x_B goes from 0.1 up to 0.75.

Fig. 12 shows the momentum and angular acceptance of electrons, π^- and protons which form the DEMP events and can be detected with the SoLID detectors. A cut of $Q^2 > 4 \text{ GeV}^2$ is applied since this is the region of greatest physics interest. The recoil protons shown in Fig. 12 have low momenta ranging from $0.3 \text{ GeV}/c$ up to $1.2 \text{ GeV}/c$ and their rates are distributed nearly uniformly in scattering angle.

3.2 Estimated Rates

$1 < Q^2 < 4 \text{ GeV}^2$	$Q^2 > 4 \text{ GeV}^2$	Total
DEMP: $\vec{n}(e, e' \pi^- p)$ Triple-Coincidence (Hz)		
6.11	0.26	6.37
SIDIS: $\vec{n}(e, e' \pi^-) X$ Double-Coincidence (Hz)		
1388.85	35.77	1424.62

Table 3: Triple-Coincidence rates for DEMP events compared with the SIDIS rates. The online production trigger will be the SIDIS double-coincidence trigger of which rates are also given.

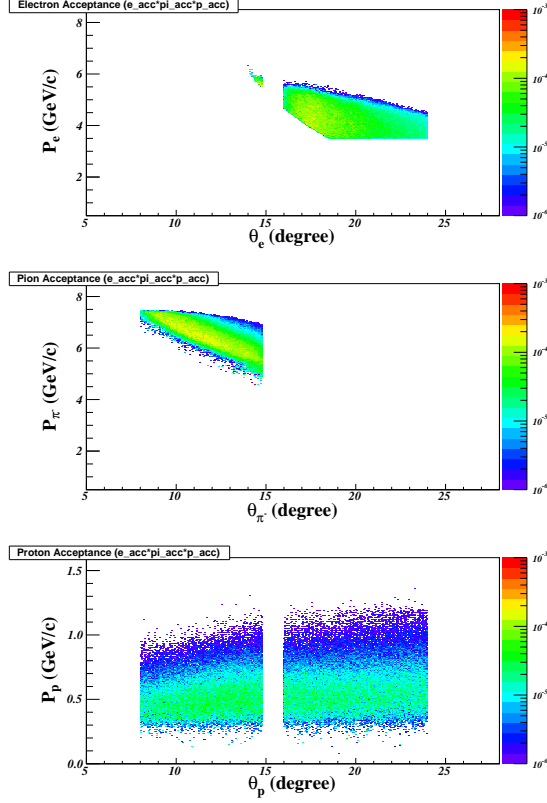


Figure 12: The acceptance of the momenta and polar angles. The top, middle and bottom plots are for electrons, π^- and protons, respectively. A cut of $Q^2 > 4 \text{ GeV}^2$ is applied. Colors correspond to rates (Hz) in log scale.

Table 3 lists the triple-coincidence rate of the DEMP events. The rates were calculated with the simulated events weighted by the target luminosity, the SoLID acceptances and unpolarized cross sections. The rates are not corrected by the beam and target polarization, target dilution and so on. The total integrated physics rate is estimated to be around 6 Hz at 11 GeV, or 0.26 Hz at $Q^2 > 4 \text{ GeV}^2$. For comparison, the table also gives the SIDIS rate which will be the online production trigger rates and is the main background of the DEMP events.

3.3 Asymmetry Projections

The proposed experiment will run in parallel with E12-10-006, which has already been approved to run 48 days at $E_0=11 \text{ GeV}$. As shown in Fig. 13, we defined 7 $-t$ bins of which the boundaries are defined by the array:

$$-t[8] = [0.0, 0.15, 0.25, 0.35, 0.45, 0.55, 0.75, 1.10] \quad (\text{in } \text{GeV}^2) \quad (10)$$

The number of events (N_i) in the i th bin is calculated from the total simulated events after applying cuts on important kinematic variables, e.g. $Q^2 > 4 \text{ GeV}^2$, $W > 2 \text{ GeV}$, $0.55 < \epsilon < 0.75$ and $-t_{min} < -t < -t_{max}$. As shown in Eqn. 11, each event surviving the cuts is then weighted by the unpolarized cross section, together with the acceptance of the electron, pion and proton. N_i is further corrected by the phase-space factor (PSF) defined in the event generator, the total number of randomly generated events (N_{gen}), beam-time

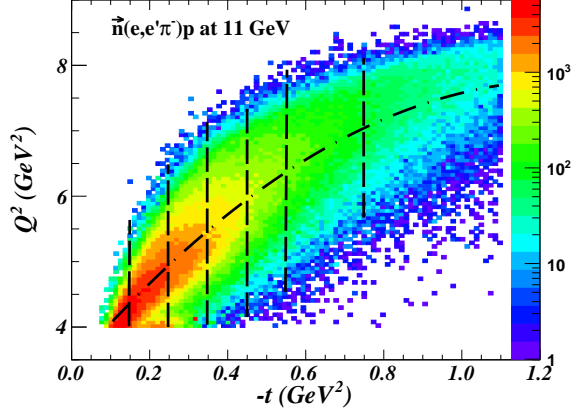


Figure 13: Q^2 vs. $-t$ where the black dash lines specify the boundaries of 7 $-t$ bins and the black dash-dot lines indicate the additional two Q^2 bins. The color panel indicates the raw counts with 48 days of beam time at 11 GeV.

(T), the target luminosity ($L = 10^{36} \text{ cm}^{-2}\text{s}^{-1}$), and the overall detector efficiency (ϵ_{eff}):

$$N_i = \left(\sum_{j \in i\text{-bin}} \sigma_j \cdot A_j^e \cdot A_j^{\pi^-} \cdot A_j^p \right) \cdot (PSF/N_{gen}) \cdot T \cdot L \cdot \epsilon_{eff}, \quad (11)$$

where j is the j th event in the i th bin, σ_j is the cross section of the j th event. $A_j^{e(\pi^-,p)}$ is the acceptance weight of the electron (pion, proton) in this event. The detector efficiency, ϵ_{eff} , is approximately fixed at 85% as was used in SIDIS proposals. N_i corresponds to the raw experimental count of electrons scattering on neutrons in ^3He before taking into account the target polarization ($P \sim 60\%$), the effective polarization of neutrons ($\eta_n \sim 0.865$), and the dilution effect from other reaction channels when electrons scattering on ^3He ($f \sim 0.9$).

In addition, we further divide each $-t$ -bin into two Q^2 bins with similar statistics. By doing that, we are able to examine the Q^2 -dependence of the asymmetries, and also check the model dependence of the other corrections that are directly related to the values of Q^2 .

The statistical error of the target single spin asymmetry (A_{UT}) in each bin can be given as:

$$\delta A_{UT} = \frac{1}{P \cdot \eta_n \cdot f} \sqrt{\frac{1 - (P \cdot \langle A_{UT} \rangle)^2}{N_i^+ + N_i^-}}, \quad (12)$$

where $N_i^{+(-)}$ is the number of counts in each bin when the target polarization is up (down), and we easily have $N_i = N_i^+ + N_i^-$; $\langle A_{UT} \rangle$ is the average asymmetry in the bin, and experimentally, it can be extracted as the following:

$$\langle A_{UT} \rangle = \frac{1}{P \cdot \eta_n \cdot f} \frac{N^+ - N^-}{N^+ + N^-}. \quad (13)$$

In this projection study, A_{UT} is predicted with a phenomenological model, as discussed in Appendix-A. Because of not performing a L/T separation in this experiment, the asymmetry should be corrected by another dilution factor, which is defined as:

$$f_{L/T} = \frac{\epsilon \sigma_L}{\sigma_T + \epsilon \cdot \sigma_L}, \quad (14)$$

where $\epsilon = (1 + \frac{2\nu^2}{Q^2} \tan^2(\theta))^{-1}$. Additional dilution due to σ_{TT} is assumed to be small. A factor of -1 is also applied after comparing Eq. 6 and Eq. 8. Hence, $A_{UT} = -f_{L/T} \cdot A_L^{\perp, model}$.

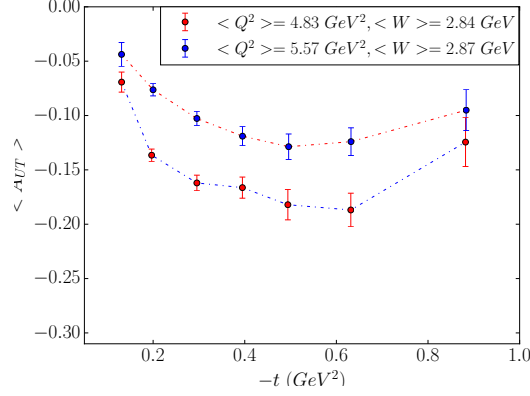


Figure 14: Projection of target single spin asymmetry (A_{UT}) as a function of $-t$ for DEMP with transversely polarized ^3He at $E_0=11$ GeV (directly compare with Fig. 6). The data in each $-t$ bin are further divided into two Q^2 bins with similar statistics. The error bars are the projected statistical uncertainties defined in Eq. 12. The asymmetry value in each bin is predicted with the model given in Appendix-A and is diluted due to not separating the L/T contributions.

Fig. 14 shows the distribution of A_{UT} vs. $-t$ with projected statistical errors discussed above. Compared with the existing HERMES results (Fig. 6), the new measurement could provide more precision data to be directly compared with theoretical predictions. Extra binning on Q^2 enables us to study the Q^2 -dependence of asymmetries as well as to constraint some corrections during the asymmetry extraction. The detailed information of each bin is listed in Table 4.

	t-bin#1	t-bin#2	t-bin#3	t-bin#4	t-bin#5	t-bin#6	t-bin#7
$\langle -t \rangle$	0.13	0.20	0.30	0.39	0.49	0.63	0.88
Q^2 bin-set#1							
$\langle Q^2 \rangle$	4.13	4.42	4.90	5.35	5.76	6.23	6.86
$\langle \sigma_L/\sigma_T \rangle$	6.43	5.13	3.90	3.09	2.43	1.65	0.69
$\langle f_{L/T} \rangle$	0.80	0.77	0.73	0.68	0.62	0.52	0.30
$\langle A_{UT} \rangle$	-6.93×10^{-2}	-1.36×10^{-1}	-1.62×10^{-1}	-1.66×10^{-1}	-1.82×10^{-1}	-1.87×10^{-1}	-1.24×10^{-1}
δA_{UT}	9.23×10^{-3}	5.62×10^{-3}	7.16×10^{-3}	9.72×10^{-3}	1.39×10^{-2}	1.54×10^{-2}	2.24×10^{-2}
N	3.26×10^4	8.73×10^4	5.37×10^4	2.91×10^4	1.42×10^4	1.15×10^4	5.50×10^3
Q^2 bin-set#2							
$\langle Q^2 \rangle$	4.39	4.93	5.58	6.13	6.59	7.09	7.73
$\langle \sigma_L/\sigma_T \rangle$	7.19	6.38	5.51	4.63	3.70	2.57	1.21
$\langle f_{L/T} \rangle$	0.81	0.80	0.78	0.74	0.70	0.61	0.42
$\langle A_{UT} \rangle$	-4.38×10^{-2}	-7.63×10^{-2}	-1.03×10^{-1}	-1.19×10^{-1}	-1.29×10^{-1}	-1.24×10^{-1}	-9.51×10^{-2}
δA_{UT}	1.13×10^{-2}	5.82×10^{-3}	6.83×10^{-3}	9.05×10^{-3}	1.21×10^{-2}	1.32×10^{-2}	1.94×10^{-2}
N	2.17×10^4	8.19×10^4	5.94×10^4	3.38×10^4	1.88×10^4	1.59×10^4	7.32×10^3

Table 4: Detailed information of projected bins from the new DEMP measurements with SoLID, while $\langle Q^2 \rangle$ and $\langle -t \rangle$ are in the unit of GeV^2 . The data are divided into 14 $-t$ bins in both $-t$ (7 bins) and Q^2 (2 bins).

3.4 Missing Mass and Background

In the DEMP reaction on a neutron, all three charged particles in the final state, e , π^- and p , can be cleanly measured by the detector system. Hence, contamination from other reactions, including DEMP with other two protons in ${}^3\text{He}$, can be greatly eliminated. The dominant background of the DEMP measurement comes from the SIDIS reactions of electrons scattering on the neutron and two protons in ${}^3\text{He}$. In addition to detecting the recoil protons, which should largely suppress most of background, we will also rely on reconstructing the neutron missing mass spectrum to ensure the exclusivity of the DEMP events. In SIDIS, however, the final states include the scattered electron, the hadrons (π^\pm , K^\pm etc.), as well as the undetected target fragments which could contain protons. Hence, the SIDIS events will possibly leak into the DEMP missing mass spectrum.

We studied the contamination of the SIDIS events in the DEMP missing momentum and mass spectra. The SIDIS reactions, $p(e, e'\pi^-)X$ and $n(e, e'\pi^-)X$, were simulated with the same generator used for the SoLID-SIDIS proposals, and their rates were calculated by matching the acceptance of scattered electrons and pions with the ones in DEMP. We then fold the SoLID detector resolutions into the spectra. Based on the current tracking study, the SoLID-SIDIS system can provide a momentum resolution of $2\%/\sqrt{E}$, a polar angle resolution of 0.6 mrad, an azimuthal angle resolution of 5 mrad and a vertex target position of 0.5 cm. It is difficult to estimate what percentage of the SIDIS target fragments contain protons, so we assumed the target fragments ("X") all contain one or more protons. Such an assumption likely results in the SIDIS background being significantly overestimated.

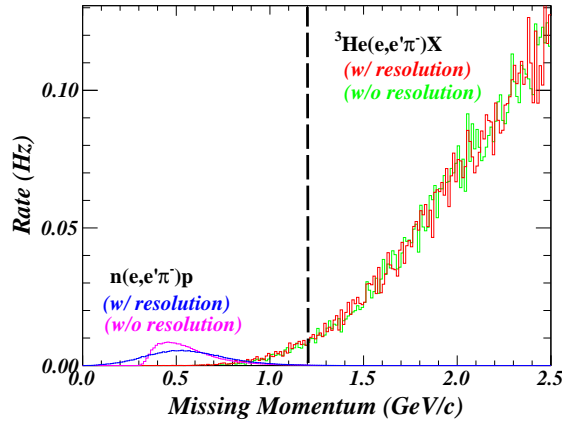


Figure 15: Missing momentum spectra of DEMP and SIDIS events. The missing momentum distributions are well separated between the two processes and one can apply a cut at $P_{miss} < 1.2$ GeV/c (indicated by the black dashed line) to remove most of the SIDIS events.

Shown in Fig. 15, is a reconstruction of the missing momenta of both processes. One immediately sees that the missing momentum distributions of two processes are well separated. The SIDIS background can be largely rejected when we apply a cut, $P_{miss} < 1.2$ GeV/c.

We then reconstructed the missing mass spectra of the DEMP and SIDIS events w/ and w/o the missing momentum cuts, as shown in Fig. 16. Before applying the missing momentum cut, the SIDIS background overwhelms the DEMP peak (note that, however, the SIDIS rate is likely overestimated). After applying

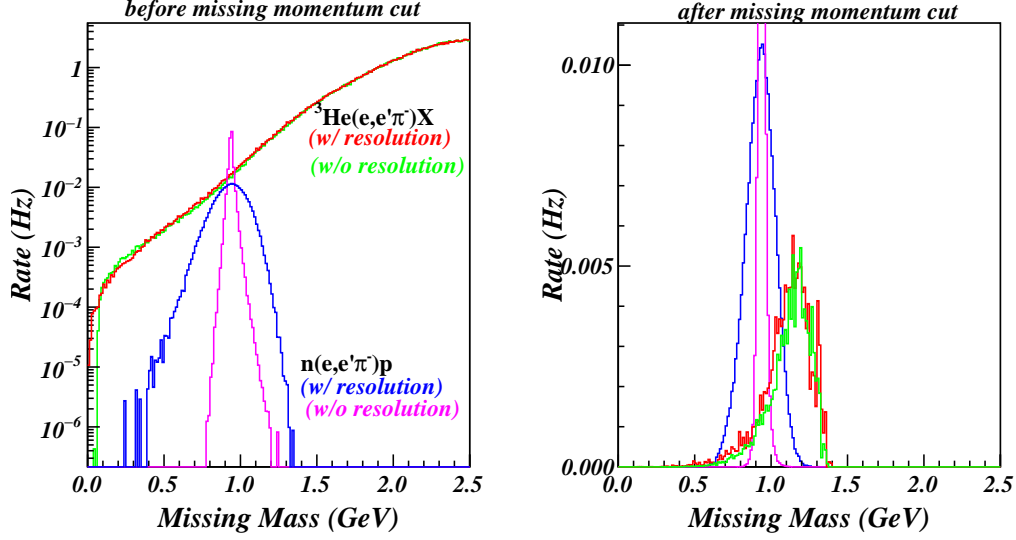


Figure 16: Missing mass spectra of DEMP and SIDIS events. Top (bottom) panel shows the missing mass distribution of DEMP events. The left (right) plot of each panel shows the background contamination from SIDIS events before (after) the missing momentum cut shown in Fig. 15. The broadening effect of the missing mass due to only the Fermi motion is indicated by the magenta curve. The SIDIS background is already small compared with DEMP events before optimizing the cut. The actual SIDIS background should be much smaller, since we overestimated the SIDIS rate by assuming all target fragments ("X") in the SIDIS process contain protons.

the cut, the DEMP peak dominates and the SIDIS background is largely suppressed. If we consider the fact that not every "X" in SIDIS contains a proton, the remaining background should be negligible.

Other random coincident background events will show up in the missing mass spectrum with more uniform distributions. We should be able to suppress most of them with tight missing momentum and missing mass cuts, and for these residuals that contaminate the real events, we are able to evaluate their asymmetries if nonzero, and apply corrections on the real asymmetry values. In general, we expect to have a clean measurement of the DEMP process because all of the final particles being detected.

3.5 Systematic Uncertainties

Sources	Relative Value
Beam Polarization	2%
Target Polarization	3%
Dilution Factor	1%
Nuclear Effect	< 4%
Acceptance	3%
Radiation Correction	2%
Background Contamination	< 5%

Table 5: Expected systematic errors.

The systematic errors are expected to be close to the ones given in the E12-10-006 proposal as well as in other SIDIS experiments with SoLID. The procedure of extracting DEMP asymmetries is also expected to be similar to the SIDIS asymmetry extraction. The contamination of background should be well controlled by the proton detection and cuts on missing momenta and mass. However, to be conservative, we quote the overall systematic errors of background contamination to be 5% level. Here we list several major sources of systematic uncertainties as shown in Table 5.

4 Summary

The transverse single-spin asymmetry in the exclusive $\vec{n}(e, e' \pi^-)p$ reaction has been noted as being especially sensitive to the spin-flip generalized parton distribution (GPD) \tilde{E} . Factorization studies have indicated that precocious scaling is likely to set in at moderate $Q^2 \sim 2 - 4 \text{ GeV}^2$, as opposed to the absolute cross section, where scaling is not expected until $Q^2 > 10 \text{ GeV}^2$. This relatively low value of Q^2 for the expected onset of precocious scaling is important, because it will be experimentally accessible at Jefferson Lab.

This measurement is complementary to a proposal to measure the longitudinal photon, transverse nucleon, single-spin asymmetry A_L^\perp with the SHMS+HMS in Hall C [4]. The good resolution and reproducible systematic uncertainties of the SHMS+HMS setup allow the L-T separation needed to reliably measure this quantity. However, a wide $-t$ coverage is needed to obtain a good understanding of the asymmetry, and it always been intended to complement the SHMS+HMS A_L^\perp measurement with an unseparated $A_{UT}^{\sin(\phi-\phi_s)}$ measurement using a large solid angle detector. The high luminosity capabilities of SoLID make it well-suited for this measurement. Since an L-T separation is not possible with SoLID, the observed asymmetry is expected to be diluted by the ratio of the longitudinal cross section to the unseparated cross section. This was also true for the pioneering HERMES measurements, which provided a valuable constraint to models for the \tilde{E} GPD. The $A_{UT}^{\sin(\phi_s)}$ asymmetry can also be extracted from the same data, providing powerful additional GPD model constraints. This measurement is also important preparatory work for future measurements at the EIC, which will allow $A_{UT}^{\sin(\phi-\phi_s)}$ to be directly compared for the $\vec{n}(e, e' \pi^-)p$ and $\vec{p}(e, e' \pi^+)n$ reactions over a broad kinematic range.

In our proposal, we will analyze the E12-10-006 event files off-line to look for $e - \pi^- - p$ triple coincidence events in SoLID for the case where the recoil proton is emitted $8^\circ < \theta < 24^\circ$. This study yields data that are a considerable advance over the HERMES measurement in terms of kinematic coverage and statistical precision.

A Monte Carlo model of Deep Exclusive π^- Production from the Neutron in ${}^3\text{He}$

One of the primary goals of this proposed measurement is to extend our knowledge of the σ_L , σ_T , σ_{LT} and σ_{TT} to larger values of Q^2 , $-t$ and W . Initial Monte Carlo studies require a model for experimentally unexplored region of kinematics. The electroproduction of charged pion is best described by the VR model [33]. A brief description of VR model is given in section 1.2. The scattering cross section for $n(e, e'\pi^-)p$ in one-photon exchange is given by equation 15:

$$\frac{d^5\sigma}{dE'd\Omega_{e'}d\Omega_\pi} = \Gamma_V \frac{d^2\sigma}{d\Omega_\pi}. \quad (15)$$

The virtual photon flux factor Γ_V in equation 15 is defined as:

$$\Gamma_v = \frac{\alpha}{2\pi^2} \frac{E'}{E} \frac{K}{Q^2} \frac{1}{1-\epsilon}, \quad (16)$$

where α is the fine structure constant, K is the energy of real photon equal to the photon energy required to create a system with invariant mass equal to W and ϵ is the polarization of the virtual photon.

$$K = (W^2 - M_p^2)/(2M_p) \quad (17)$$

$$\epsilon = \left(1 + \frac{2|\mathbf{q}|^2}{Q^2} \tan^2 \frac{\theta_e}{2}\right)^{-1}, \quad (18)$$

where θ_e is the scattering angle of scattered electron. The two-fold differential cross section $\frac{d^2\sigma}{d\Omega_\pi}$ in the lab frame can be expressed in terms of the invariant cross section in centre of mass frame of photon and proton:

$$\frac{d^2\sigma}{d\Omega_\pi} = J \frac{d^2\sigma}{dt d\phi}, \quad (19)$$

where J is the Jacobian of transformation of coordinates from lab Ω_π to t and ϕ (CM). The invariant cross section of equation 19 can be expressed in four terms. Two terms correspond to the polarization states of the virtual photon (L and T) and two states correspond to the interference of polarization states (LT and TT),

$$2\pi \frac{d^2\sigma}{dt d\phi} = \epsilon \frac{d\sigma_L}{dt} + \frac{d\sigma_T}{dt} + \sqrt{2\epsilon(\epsilon+1)} \frac{d\sigma_{LT}}{dt} \cos \phi + \epsilon \frac{d\sigma_{TT}}{dt} \cos 2\phi \quad (20)$$

A.1 Data Constraints

Precise L/T separated experimental data of exclusive electroproduction of π^- on ${}^2\text{H}$ are available up to $Q^2 = 2.57 \text{ GeV}^2$, $-t = 0.350 \text{ GeV}^2$ and $W = 2.168 \text{ GeV}$ [34]. Precise L/T separated experimental data of exclusive electroproduction of π^+ on ${}^1\text{H}$ are available up to $Q^2 = 2.703 \text{ GeV}^2$, $-t = 0.365 \text{ GeV}^2$ and $W = 2.127 \text{ GeV}$ [35]. In [36] and [37], separated σ_L and σ_T are measured up to $Q^2 = 4.703 \text{ GeV}^2$ and $W = 2.2 \text{ GeV}$. CLAS experiment E99-105 measured the unseparated cross section at Q^2 up to 4.35 GeV^2 and $-t$ up to 4.5 GeV^2 [38]. The HERMES collaboration measured the unseparated cross section for $Q^2 = 3.44 \text{ GeV}^2$ and 5.4 GeV^2 [39] at $W = 4 \text{ GeV}$.

A.2 Model for Higher Q^2 Kinematics

The electroproduction of charged pion is best described by the VR model [33]. The VR model is a Regge model with a parametrization of deep inelastic scattering amplitude to improve the description of σ_T . The description of σ_L is constrained by a fit to our F_π data from JLab [35]. In figure 17 we plotted the last six data points of table v of [34], our parametrization and VR model points for exactly same values of Q^2 , $-t$ and W . It shows the comparison of the same points of $\sigma_{L,T,LT,TT}$ vs. Q^2 .

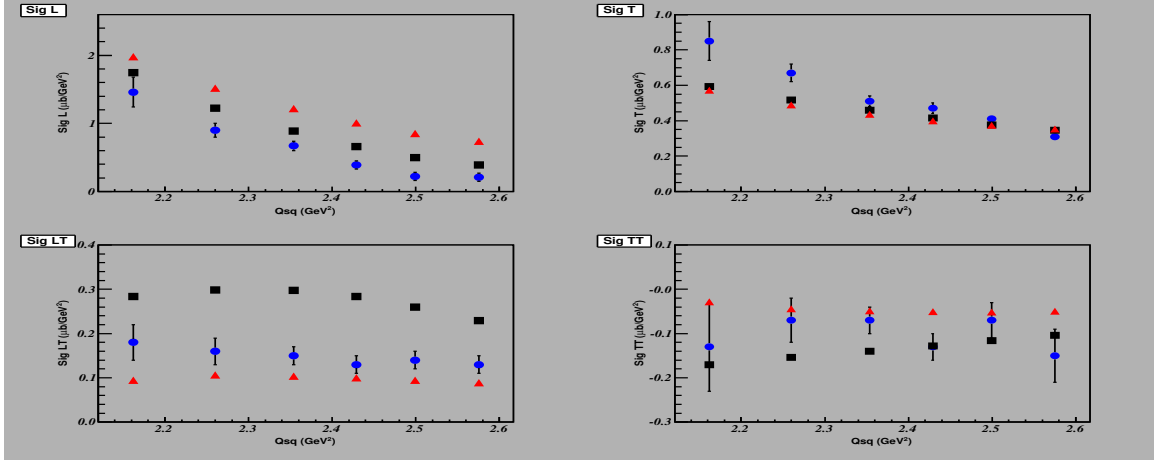


Figure 17: A comparison of last six points of table v of [34], VR model and our parametrization values vs. Q^2 of π^- electroproduction. Experimental data is shown in blue circles, VR model is shown in red triangles and our parametrization is shown in black boxes. In each graph value of $-t$ is decreasing left to right from maximum value 0.35 GeV^2 to 0.15 GeV^2 . Value of W also decreases left to Right from 2.2978 GeV to 2.1688 GeV .

A.3 Parametrization of σ_L , σ_T , σ_{LT} , & σ_{TT}

For exclusive DEMP in SoLID the kinematic region of interest for parametrization of $\sigma_{L,T,LT,TT}$ is Q^2 from 4.5 GeV to 7.5 GeV , $-t$ from 0 GeV^2 to 1.0 GeV^2 and we set $W = 3.0 \text{ GeV}$. After the parametrization of $\sigma_{L,T,LT,TT}$ for $-t$ and Q^2 , we used the same W dependence given by [35] which is $(W^2 - M^2)^{-2}$ where M is the proton mass. Our parametrization of all four cross sections is given in equations 21 to 24:

$$\sigma_L = \exp(P_1(Q^2) + |t| * P'_1(Q^2)) + \exp(P_2(Q^2) + |t| * P'_2(Q^2)) \quad (21)$$

$$\sigma_T = \frac{\exp(P_1(Q^2) + |t| * P'_1(Q^2))}{P_1(|t|)} \quad (22)$$

$$\sigma_{LT} = P_5(t(Q^2)) \quad (23)$$

$$\sigma_{TT} = P_5(t(Q^2)), \quad (24)$$

where the parameters P_i are polynomial functions of i th order. Each coefficient (P_i) of fifth order equations 23 and 24 is a further second order polynomial of Q^2 . Deep exclusive π^- events are generated

using a C++ code. The quality of parametrization is checked by plotting the parametrization functions of $\sigma_{L,T,LT,TT}$ versus the VR model as shown in figure 18.

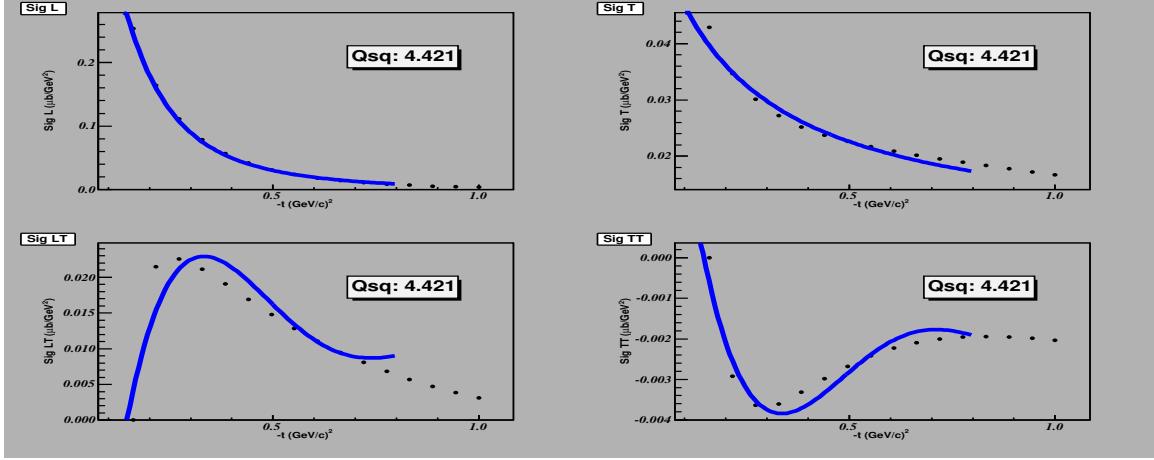


Figure 18: A comparison of parametrized $\sigma_{L,T,LT,TT}$ and VR model values at $Q^2 = 4.421 \text{ GeV}^2$ and $W = 3.0 \text{ GeV}$. Black points are VR model values and blue line is parametrized $\sigma_{L,T,LT,TT}$ given by equations 21 to 24.

Figure 18 shows the comparison of parametrization of $\sigma_{L,T,LT,TT}$ and VR model points. The blue line is the parametrization curve and black points are the VR model points.

A.4 Single Spin Asymmetry (SSA) A_L^\perp

It is shown in [40] that the generalized parton distribution (\tilde{E}) can be probed by measuring the single spin asymmetry (SSA). The SSA is defined in equation 25, where β is the angle between the transversely polarized target vector and the reaction plane, and $\sigma_L^{\pi^-}$ is the exclusive π^- cross section for longitudinal virtual photons. We parametrized the single spin asymmetry using the model of [40] at $x = 0.1$ and $x = 0.3$. Parametrization of SSA is shown in Figure 19 and equation 26 is the parameterized function of single spin asymmetry.

$$A_L^\perp = \frac{\int_0^\pi d\beta \frac{d\sigma_L^{\pi^-}}{d\beta} - \int_\pi^{2\pi} d\beta \frac{d\sigma_L^{\pi^-}}{d\beta}}{\int_0^{2\pi} d\beta \frac{d\sigma_L^{\pi^-}}{d\beta}} \quad (25)$$

$$A_L^\perp = \begin{cases} A_0 [1 - \exp[-\lambda \times (t - t_{min})]] & \text{if } t \geq t_{min}, \\ 0 & \text{if } t < t_{min}. \end{cases} \quad (26)$$

A.5 Target Neutron Fermi Momentum

A histogram of the spectral function of ^3He is shown in Fig. 20, generated according to Ref. [41]. Neutron momenta up to 300 MeV/c are generated according to this distribution, uniformly distributed in spherical coordinates. The quasi-free collision between virtual photon and moving neutron is then transformed to the fixed neutron frame, after which the parameterizations of Secs. A.3, A.4 are applied. The outgoing particles are then transformed back to the lab frame for tracking.

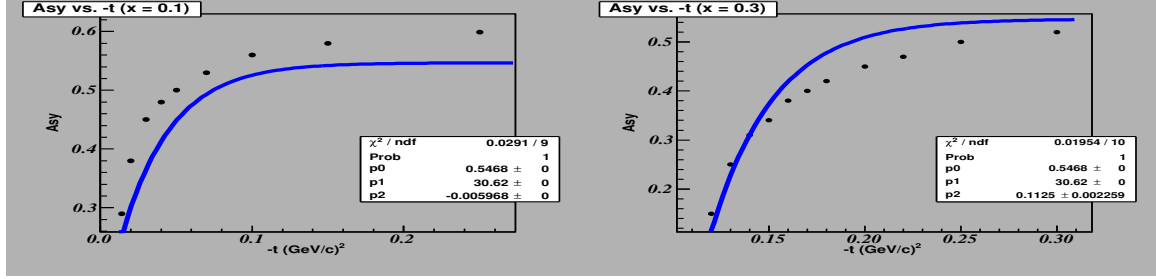


Figure 19: Parametrization of single spin asymmetry \mathbf{A}_L^\perp vs. $-t$ at $Q^2 = 10 \text{ GeV}^2$ in left graph $x = 0.1$ and in right graph $x = 0.3$ where the points are from the model defined in [40] and blue line is our parametrization function.

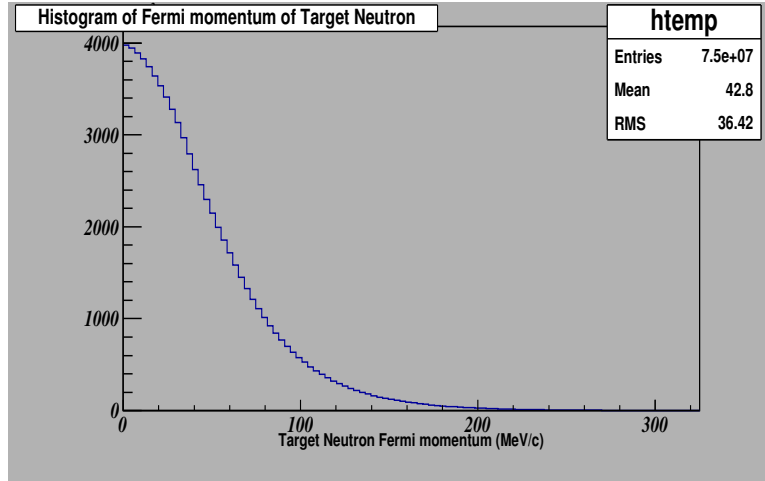


Figure 20: Fermi momentum spectral function of a target nucleon in ^3He generated according to the Argonne potential of Ref [41]. The horizontal axis is nucleon momentum in MeV/c.

References

- [1] Approved SoLID SIDIS experiment E12-10-006, “Target Single Spin Asymmetry in Semi-Inclusive Deep-Inelastic ($e, e'\pi^\pm$) Reaction on a Transversely Polarized ^3He Target at 11 GeV”, [https : //www.jlab.org/exp_prog/proposals/14/E12 – 10 – 006A.pdf](https://www.jlab.org/exp_prog/proposals/14/E12-10-006A.pdf)
- [2] SoLID Collaboration, “Solenoidal Large Intensity Device Preliminary Conceptual Design Report,” [http : //hallaweb.jlab.org/12GeV/SoLID/files/solid-precdr.pdf](http://hallaweb.jlab.org/12GeV/SoLID/files/solid-precdr.pdf)
- [3] A. Airapetian, Phys. Lett. **B 682** (2010) 345-350, arXiv:0907.2596 [hep-ex].
- [4] PR12-12-005: D. Dutta, D. Gaskell, W. Hersman, G.M. Huber, et al., “The Longitudinal Photon, Transverse Nucleon, Single-Spin Asymmetry in Exclusive Pion Production”.
- [5] M. Diehl, Contribution to the eRHIC White Paper, arXiv:hep-ph/0010200.
- [6] J.C. Collins, L. Frankfurt, M. Strikman, Phys. Rev. D **56** (1997) 2982.
- [7] K. Goeke, M.V. Polyakov, M. Vanderhaeghen, Prog. Part. Nucl. Phys. **47** (2001) 401-515.
- [8] A.V. Radyushkin, arXiv:hep-ph/0101225.
- [9] A.W. Thomas, W. Weise, “The Structure of the Nucleon”, J. Wiley-VCH, 2001.
- [10] R.E. Marshak, Riazuddin, C.P. Ryan, “Theory of Weak Interactions in Particle Physics”, J. Wiley, 1969.
- [11] M. Penttinen, M.V. Polyakov, K. Goeke, Phys. Rev. C **62** (2000) 014024 1-11.
- [12] A.V. Belitsky, D. Mueller, Phys. Lett. **B 513** (2001) 349-360.
- [13] S. V. Goloskokov and P. Kroll, Eur. Phys. J. C **65**, 137 (2010), arXiv:0906.0460 [hep-ph].
- [14] L.L. Frankfurt, P.V. Pobylitsa, M.V. Polyakov, M. Strikman, Phys. Rev. D **60** (1999) 014010 1-11.
- [15] M. Diehl, S. Sapeta, Eur. Phys. J. C **41** (2005) 515, arXiv:hep-ph/0503023.
- [16] M. Vanderhaeghen, P.A.M. Guichon, M. Guidal, Phys. Rev. D **60** (1999) 094017 1-28.
- [17] L.L. Frankfurt, M.V. Polyakov, M. Strikman, M. Vanderhaeghen, Phys. Rev. Lett. **84** (2000) 2589-2592.
- [18] A.V. Belitsky, CIPANP 2003 proceedings. arXiv: hep-ph/0307256.
- [19] L. Mankiewicz, G. Piller, A. Radyushkin, Eur. Phys. J. **C 10** (1999) 307-312.
- [20] C.E. Carlson, J. Milana, Phys. Rev. Lett. **65** (1990) 1717.
- [21] E12-06-101, “Measurement of the Charged Pion Form Factor to High Q^2 ”, G.M. Huber, D. Gaskell, spokespersons.
- [22] A. Bartl, W. Majerotto, Nucl. Phys. **B62** (1973) 267-285.
- [23] pCDR for the Science and Experimental Equipment for the 12 GeV Upgrade of CEBAF, June, 2004. V. Burkert et al., PAC18 Review of the Science Driving the 12 GeV Upgrade, July, 2000.

- [24] S. V. Goloskokov and P. Kroll, private communications 2009-2016.
- [25] H.P. Blok, et al., Phys. Rev. C **78** (2008) 045202.
- [26] Approved SoLID SIDIS experiment E12-11-007, “Asymmetries in Semi-Inclusive Deep-Inelastic ($e, e'\pi^\pm$) Reactions on a Longitudinally Polarized ^3He Target at 8.8 and 11 GeV”, [https : //www.jlab.org/exp_prog/PACpage/PAC37/proposals/Proposals/New%20Proposals/PR - 11 - 007.pdf](https://www.jlab.org/exp_prog/PACpage/PAC37/proposals/Proposals/New%20Proposals/PR-11-007.pdf)
- [27] Approved SoLID SIDIS experiment E12-11-108, “Target Single Spin Asymmetry in Semi-Inclusive Deep-Inelastic ($e, e'\pi^\pm$) Reactions on a Transversely Polarized Proton Target”, [https : //www.jlab.org/exp_prog/proposals/11/PR12 - 11 - 108.pdf](https://www.jlab.org/exp_prog/proposals/11/PR12-11-108.pdf)
- [28] Approved SoLID J/ ψ experiment E12-12-006A, “Near Threshold Electroproduction of J/ ψ at 11 GeV”, [https : //www.jlab.org/exp_prog/proposals/12/PR12 - 12 - 006.pdf](https://www.jlab.org/exp_prog/proposals/12/PR12-12-006.pdf)
- [29] Approved SoLID SIDIS experiment E12-10-006A, “Dihadron Electroproduction in DIS with Transversely Polarized ^3He Target at 11 and 8.8 GeV”, [https : //www.jlab.org/exp_prog/proposals/14/E12 - 10 - 006A.pdf](https://www.jlab.org/exp_prog/proposals/14/E12-10-006A.pdf)
- [30] Approved SoLID SIDIS experiment E12-11-108A, “Target Single Spin Asymmetry Measurements in the Inclusive Deep-Inelastic $\vec{N}(e, e')$ Reaction on Transversely Polarized Proton and Neutron (^3He) Targets using the SoLID Spectrometer” [https : //www.jlab.org/exp_prog/proposals/14/E12 - 11 - 108A_E12 - 10 - 006A.pdf](https://www.jlab.org/exp_prog/proposals/14/E12-11-108A_E12-10-006A.pdf)
- [31] Approved SoLID PVDIS experiment E12-10-007, “Precision Measurement of Parity-violation in Deep Inelastic Scattering Over a Broad Kinematic Range”, [https : //www.jlab.org/exp_prog/PACpage/PAC37/proposals/Proposals/Previously%20Approved/E12 - 10 - 007.pdf](https://www.jlab.org/exp_prog/PACpage/PAC37/proposals/Proposals/Previously%20Approved/E12-10-007.pdf)
- [32] J. L. Friar et al., Phys. Rev. C **42**, (1990) 2310; C. Ciofi degli Atti, and S. Scopetta, Phys. Lett. **B404**, (1997) 223; R.W. Schulze and P.U. Sauer, Phys. Rev. **C56** (1997) 2293; F. Bissey, A.W. Thomas, and I.R. Afnan, Phys. Rev. **C64**, (2001) 024004.
- [33] T. Vrancx and J. Ryckebusch., Phys. Rev. **C89**, 025203 (2014).
- [34] G. M. Huber *et al.*, Phys. Rev. **C91**, 015202 (2015).
- [35] H. Blok *et al.*, Phys. Rev. **C78**, 045202 (2008).
- [36] T. Horn *et al.*, Phys. Rev. Lett **97**, 192001 (2006).
- [37] T. Horn *et al.*, Phys. Rev. **C78**, 058201 (2008).
- [38] <http://clas.sinp.msu.ru/cgi-bin/jlab/db.cgi?eid=36;search=on>
- [39] A. Airapetian *et al.*, Phys. Lett. B. **659**, (2008).
- [40] L. L. Frankfurt *et al.*, Phys. Rev. Lett. **84**, 2589 (2000).
- [41] R. Schivavilla and V. R. Pandharipande., Nucl. Phys. A. **449**, 219 (1986).