

# Chapter 2

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## 2.1

**Def** Experiment : any activity / situation w/ uncertainty about which  $x \geq 2$  outcomes are possible

- coin toss, roll a die, draw a card

**Def**

### Sample Space

- collection of all possible outcomes of a chance experiment

Notate - s or  $\mathcal{U}$

- Toss a coin : heads or tails

**Def**

**Event :**

- any collection of outcomes from a sample space of a chance experiment

Notate

CAP letters :  $A, B, C, \dots$

**Def** Simple Event : event that consists of one outcome

Compound Event : event that consists of more than one outcome

**Ex** Tennis : A tennis shop carries 5 brands of rackets (Head, Prince, Sazenger, Wimbledon, Wilson). Each racket comes in midsize / oversize

- a. sample space

*insert diagram here*

- b. Let A be the event an oversized racket is purchased

$$A = \{HO, PO, SO, WimO, WilO\}$$

- c. Let B be the event the name brand starts w/ a W

$$B = \{WimM, WimO, WilM, WilO\}$$

### Forming New Sets

Let A and B be any 2 events

**Def** Complement of A :

- all outcomes in S, not in A

**Notate**  $A', \bar{A}, A^c$

**Notate** union - A or B - inclusive

$$A \cup B$$

intersection - A and B

$$A \cap B$$

**Ex** Tennis Cont.

- d.  $\bar{B}$  = brand does not start w/ W

$$\bar{B} = \{HO, HM, PO, PM, SO, SM\}$$

- e. Head, Prince, and Wilson are US companies. Let C define rackets from the U.S.

$$C = \{HO, HM, PO, PM, WilO, WilM\}$$

$$B \cup C = \{HO, HM, PO, PM, WilO, WilM, WimO, WimM\}$$

- f. List outcomes in  $B \cap C$ .

$$B \cap C = \{WilO, WilM\}$$

- g.  $\overline{(B \cap C)} = \{HO, HM, PO, PM, WimO, WimM\}$

### Two Mutually Exclusive Events

**Def** mutually exclusive : no outcomes in common

**Def** Disjoint : no outcomes in common

*include figure here*

**Note** If A and B are disjoint,  $A \cap B = \emptyset$

*include figure here*

**Ex**

$$A = \{4, 6, 8, 10, 12\} \quad B = \{8, 10, 12, 14\} \quad C = \{12, 14, 16\} \quad D = \{16, 18\}$$

$$A \cap B = \{8, 10, 12\}$$

$$B \cap C = \{12, 14\}$$

$$A \cap (C \cap D) = A \cap \{16\} = \emptyset$$

$$A \cap C = \{12\}$$

$$B \cap D = \{\} = \emptyset$$

$$(A \cap B) \cup C = \{8, 10, 12\} \cup C = \{8, 10, 12, 14, 16\}$$

$$(A \cap B) \cup (B \cap C) = \{8, 10, 12\} \cup \{12, 14\} = \{8, 10, 12, 14\}$$

## 2.2 Classical Probability

- N equal likely outcomes
- each outcome has probability  $\frac{1}{N}$