Chapter 1

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```
{r setup, include=FALSE} knitr::opts_chunk$set(fig.width=6,
fig.height=4, fig.align="center", echo = FALSE)
```

```
{r message=FALSE} if (!require(mosaic)) install.packages("mosaic",
repos = 'https://cloud.r-project.org') library(mosaic) # load
the package mosaic to use its functions
```

```
library(float)
```

#5.3, 5.4 Estimation

Def Parameter : a numerical value that describes the population. This value is fixed but often unknown in practice.

Def Statistic : a numerical value that describes a sample

- known from sample data
- varies from sample to sample
- use it to estimate the parameter
- use cap letters to denote R.V.
  - $\overline{X}$ is used for the sample mean R.V.
- use lower case letters to denote a calculated value of the statistic
  - $\overline{x}$ is used for a specific value of the sample mean

Def The R.V.'s $X_1, X_2, \ldots, X_n$ are said to form a simple random sample of size n. If

1. The X_i's are independent R.V's
2. Every X_i has the same probability distribution
    - independent and identically distributed (iid.)

The idea of a sampling distribution

1. a random sample is selected from a population
2. A statistic is calculated from the random data
    - a statistic is random as it arises from sample to sample according to random selection
    - the distribution of the statistic is called sampling distribution
    - the sampling distribution describes all possible values of the statistic and the probability (likelihood) of those values

Ex Let X be the # of packages being mailed by a random customer.

x	1	2	3	4
$p(x)$	.4	.3	.2	.1

a. Consider a random sample of size $n = 2$. Let $\overline{X}$ be the # of packages shipped.

Obtain the pdf of $\overline{X}$

x_1	x_2	$p(x_1, x_2)$	$\overline{x}$
1	1	$.4 * .4 = .16$	$\frac{1+1}{2} = 1$
1	2	$.4 * .3 = .12$	$\frac{1+2}{2} = 1.5$
1	3	$.4 * .2 = .08$	2
1	4	$.4 * .1 = .04$	2.5
2	1	.12	1.5
2	2	.09	2
2	3	.06	2.5
2	4	.03	3
$\vdots$	$\vdots$	$\vdots$	$\vdots$

$\overline{x}$	1	1.5	2	2.5	3	3.5	4
$p(\overline{x})$	.16	.24	.25	.2	.1	.04	.01

b. $P(\overline{x} \leq 2.5) = .16 + .24 + .25 + .2 = .85$