



## Department of Mathematics

(AFFILIATED COLLEGES)

### PONDICHERRY UNIVERSITY

UG Degree (BS Honours) with Research in Mathematics

### NATIONAL EDUCATION POLICY (NEP 2020) REGULATIONS-2023

#### Definitions:

Terms used in the NEP-CBCS Regulations shall have the meaning assigned to them as given below unless the context otherwise requires:

- a. **Credit:** A credit is the number of hours of instruction required per week for the given subject in a given semester of 16-18 weeks. One credit is equivalent to 15 hours of teaching (lecture or tutorial) or 30 hours of practice or field work or community engagement and service per Semester.
  - b. **Academic Year**" means the year starting on 1st day of July and ends on the 30th day of June succeeding year.
  - c. **“Residence time”** means the time a student spends for attending classes in the College/Institution (either Online/Offline) as a full-time student and enrolled in any Academic programme of the Institution.
  - d. **“Semester”** means 18 weeks (90 Working days) of teaching-learning session of which two weeks shall be set apart for examinations and evaluation;
  - e. **“Grade”** means a letter grade assigned to a student in a Course for his performance at academic sessions as denoted in symbols of: O(outstanding), A+(Excellent), A (Very good), B+ (good), B (Above average), C (average), P (Pass) F (fail) and Ab (Absent) with a numeric value of O=10, A+=9, A=8, B+=7, B=6, C=5 P=4, and F=0, Ab=0;
  - f. **“Grade Point Average (GPA)”** means an average of the Grades secured by a student in all courses in a given academic session duly weighted by the number of credits associated to each of the courses;
  - g. **“Cumulative GPA (CGPA)”** is the weighted average of all courses the student has taken in a given Programme;
  - h. **“A common Course”** means the set of courses that all students who are admitted to any Programme of the University are required to study; these courses include, Languages (English-modern Indian languages), NEP specific courses- viz. Understanding India, Environmental sciences/Education, Health and wellbeing/Yoga, Digital & Technological solutions;
  - i. **“Major Discipline”** means the core subject mandatory for the programme, Major discipline may be a single discipline or interdisciplinary/ multidisciplinary courses. Eg. B.Sc. (Maths) or B.Sc. (Maths and Chemistry)
  - j. **“Minor Discipline”** means allied or elective subjects to major discipline.
- (i) **“Minor discipline Cognate”** refers to a pool of courses offered by the parent department/ cognate (allied) departments. Eg. B.Com(General) may have minors streams leading in 2/3 to B.Com (Accounting

& Taxation), B.Com(Banking&Finance), B.Com(Company Law & Corporate Secretaryship) or B.Com(Computer app and Data Analytics)

**(ii) “Minor discipline Generic”** refers to the subsidiary/elective subjects chosen from a basket of courses offered by different departments other than the minors offered by the parent department.

Eg. B.Com. (Corporate Economics)

**k. “Credit Requirement”** for a Degree/Diploma/Certificate Programme means the minimum number of credits that a student shall accumulate to achieve the status of being qualified to receive the said Degree, Diploma/Certificate as the case may be;

**l. “Exit option”** means the option exercised by the students, to leave the Programme at the end of any given Academic year; **“Lateral entry”** means a student being admitted into an ongoing Programme of the University otherwise than in the 1st year of the programme.

**m. “Vocational Studies/Education”** This refer to set of activities for participation in an approved project or practical or lab, practices of application of scientific theories, studio activities involving students in creative artistic activities, workshop-based activities, field-based shop- floor learning, and Community engagement services, etc

**n. Skill-based learning/project** This refers to activities designed to understand the different socio-economic contexts, first-hand understanding of the policies, regulations, organizational structures, processes, and programmes that guide the development process.

**o. Work-based internship -** This refers to structured internships with local industry, businesses, artists, crafts persons etc. which will further improve employability.

## **Programmes to be offered at Colleges:**

The Curriculum Framework designed by UGC for implementing NEP 2020 specifies that all Undergraduate(UG) degree programmes are to be from a period either for 3 years or for 4 years leading to award of UG or UG(Hons) Degrees.

### **BREAKUP OF CREDITS AND COURSES**

<b>Sl. No.</b>	<b>Component</b>	<b>3 Year Degree</b>	<b>4 Year Hons Degree</b>
1	Major Disciplinary Courses	60 Credits (15 Courses of 4 credits each)	80 Credits (20 Courses of 4 credits each)
2	Minor Discipline Courses	24 Credits (6 Courses of 4 Credits each)	32 Credits (8 Courses of 4 credits each)
3	Multi-Disciplinary Courses	9 Credits(3 courses of 3credits each)	9 Credits (3 courses of 3 credits each)
4	Ability Enhancement Courses	8 Credits(4 courses of 2 credits each)	8 Credits (4 courses of 2 credits each)
5	Skill Enhancement Course	9 Credits(3 courses of 3 credits each)	9 Credits ( 3courses of 3 credits each)
6	Common Value added courses	8 Credits( 4 course of 2 credits each)	8 Credits (4 course of 2 credits each)
7	Community Science	2 Credits(1 field based course)	2 Credits (1 field based course)
8	Research Dissertation Project	-	12 Credits(Project report & background subjects)
9	Total credits required	120 Credits	160 Credits

## **4.1. NEP Classification of Courses:**

### **i) Major Disciplinary courses (MJD): (60/80 credits)**

Major disciplinary courses are subject specific compulsory subjects that a student has to complete to obtain the UG/UG (Hons) Degree in the given discipline. Major disciplinary courses shall constitute 50% of the total credits.

All discipline specific major courses shall be designed for 4 credits each with one/two additional hours or guidance of teaching at Tutorials/Practicals.

UG programmes may be offered in a single major discipline or in Multiple Major disciplines giving equal weightage in credits. For example a B.Sc. course may be in a single discipline like B.Sc. (Maths) or with multiple major disciplines like B.Sc. (Maths, Physics & Chemistry).

### **ii) Minor Disciplinary Course (MID): (24/32 credits)**

Minor disciplinary courses refer to those subjects which are Allied/Specialisation/Elective subjects to the Major discipline. These allied courses are expected to provide additional understanding of the subject in a specific focused area. For example a B.A. (Political Science) student shall study allied subjects like Public Administration, Sociology as these subjects have inter linkages with the Major Disciplinary subjects. Minor disciplinary courses (MID) may also be designed by the parent department or collaborated with sister departments. Parent departments may introduce minor specialisations to students by offering a set of 6 to 8 courses in one/two streams as electives or specialisation subjects. A BBA/MBA programme may have electives in HR, marketing, finance, etc. with a set of 6 to 8 subjects in each. In order to provide choice to the students to choose a particular specialisation/elective, the BOS may develop 2 to 3 streams of minor specialisation courses to focus on such trades for better placement of students. Each stream of 6/8 specialisation/elective subjects may facilitate award of two/three unique degrees in a given major Eg. B.Sc. (Physical Chemistry), B.Sc. (Pharmaceutical chemistry), etc.

### **iii) Multi-Disciplinary courses (MLD): (9 Credits)**

All undergraduate students are mandated to pursue 9 credits worth of courses in such Multi-disciplinary areas/Courses out of 9/10 NEP defined subjects. Colleges may identify any 3 multiple disciplinary streams listed below based on availability of resources and manpower. (from Natural Sciences, Physical Sciences, Mathematics & Statistics, Computer Science/Applications, Data Analysis, Social Sciences, Humanities, Commerce & Management, Library Science, Media Sciences, etc.) Students are expected to learn basic/introductory courses designed by other departments for this purpose. Colleges may list any 3 introductory courses (one each in natural Sciences, Physical Sciences, Humanities) for uniform adoption of all UG students.

### **iv) Ability Enhancement (AEC) courses: (8 Credits)**

All Undergraduate (UG) students are mandated to complete atleast 8 Credits worth of Courses which focus on Communication and Linguistic skills, Critical reading, writing skills. These courses are expected to enhance the ability in articulation and presentation of their thoughts at workplace. Colleges may design these ability enhancement courses tuned to the requirements of given major discipline. Eg. A course in Business Communication is more appropriate in place of literature/prose/poetry.

**a) English Language**

<b>Ability Enhancement Course</b>	
<b>I. English Language</b>	<b>II. Indian Language (two courses)</b>
a) English Language & Literature – 1 and 2 b) Functional English – 1 and 2 c) Communicative English – 1 and 2	a) Indian language & Literature – 1 and 2 b) Functional language – 2 c) Communicative language – 1 and 2

**v) Skill Enhancement Course: (9 Credits)**

These courses focus at imparting practical skills with hands-on Training. In order to enhance the employability of students, Colleges are expected to design such courses that they deem fit for their students for better employment/entrepreneurship/career development, etc. Colleges may also outsource the Skill Enhancement Courses to AICTE approved agencies for conducting short term Training Workshops, Skill India initiatives of GOI and approved Trades by Skill development of corporation are to be considered. short term courses.

**vi) Value Added Common courses(VAC): (8 credits)**

Under NEP, the UGC has proposed for 6 to 8 credits worth of common courses which are likely to add value to overall knowledge base of the students. These courses include: (Understanding India, Environmental Sciences/Education, Digital and technological solutions, Health, Wellness, Yoga Education, Sports & Fitness) The course structure and coverage of topics are suggested by UGC in its draft documents, colleges/UG Boards of Studies may design the methodology for conducting these value added courses.

**vii) Summer Internship ( 2 to 4 Credits)**

As per the UGC guidelines, all UG students should be exposed to a 4 to 6-week Summer Internship in an industrial organisation/Training Centres/Research Institution, etc. Such a Summer Internship is to be conducted in between the 4<sup>th</sup> and 5<sup>th</sup> semesters. A review of the report and award of grade based on work-based learning by students is to be recorded during the 5th Semester.

**a) Community Engagement and Service (CES) (2 credits)**

All UG students are also mandated to participate in a 15-day community engagement activity during their winter vacation between the 5<sup>th</sup> Semester and the 6<sup>th</sup> semester. This Community engagement activity is expected to expose the students to the social problems of the neighbourhood village. students may prepare a report on the activities carried out for the award of 2 credits.

**viii) Research Project (12 Credits)**

All UG (Hons) Degree students are expected to conduct a semester-long Research work - during their 8th Semester, and submit a Research Report. Students may be given necessary guidance by faculty members in identifying the research problem, conducting of study, and preparing a Project Report. All these Research Reports are evaluated by a Jury of external experts. A presentation of Results and Viva may also be part of the evaluation. A Publication out on findings of the Research Project may also be encouraged.

**Levels of Courses:**

The levels are:

0 to 99 = Pre-requisite/ Bridge courses

100 to 199 = Foundation courses/Introductory courses

200 to 299 = Intermediate Level courses

300 to 399 = Core courses/Advanced courses

400 and above =Specialization subjects

### **Semester –wise Break up of Courses for 3 year UG and 4 Year UG (Hons) Degree programmes**

Incorporating the focus of NEP in terms of different categories of courses and award of Certificates, Diplomas and Degrees during different stages of 4 year Degree programmes, a template for Semester-wise course work was designed by the UGC and presented in para 5.3 of “Curriculum Framework”. Salient features of it are as follows:

- Every Semester shall have a minimum of 20 credits worth of courses.
  - Credits for a course shall be decided on the basis of number of Contact hours of the teaching in a classroom. One credit means one hour of Teaching in case of Theory subject and at least 2 hours of conducting Practical in hours case of Lab subjects.
  - All Major and Minor disciplinary Courses shall have 4 credits with 6 hours of work load (including 2 hours of tutorials)
  - Language courses, ability enhancement, skill enhancement and value added common course also will have 2 hours of hands on training.
  - Students can exercise his/her choice for exiting the course at the end of every Academic year.
  - Semester I and II shall focus on introductory courses/subjects in Major/Minor disciplines and shall focus on providing knowledge in Multidisciplinary areas, skill enhancement and ability enhancement courses.
  - Semester III and IV shall focus on Core disciplinary courses with a focus on building strong foundation in the given Discipline.
  - Semester V and VI shall focus on providing in-depth knowledge and skills required for taking up a career in the given discipline.
  - Semester VII and VIII shall focus on Advanced knowledge and shall direct the students to take up socially relevant projects/Research works newer applications of the knowledge.
- While directing the above mentioned requirements, UGC has designed a Template for each Semester.

### **Eligibility:**

All students who have completed their Higher Secondary School Certificate are eligible for admission into an undergraduate degree programme, subject to securing m50% of marks at 12th standard with a minimum of 50% of marks with Mathematics or equivalent stage of education to Level-4 (Levels in NHEQF).

### **Admissions:**

As per the NEP, students shall be admitted to Undergraduate Programmes on basis of merit order in an All India Admission Test like CUET, NEET, etc. However, the respective State/UT Governments shall decide the order of merit for admission of students for different courses offered at Colleges

### **Lateral Entry:**

As per NEP, students have a choice of exit and entry into the Programme of Study multiple number of times. UGC specifies that about 10% of seats over and above the sanctioned strength shall be allocated to accommodate the Lateral Entry students. Detailed guidelines for lateral Entry would be finalized by the University

**PONDICHERRY UNIVERSITY**

**ANNEXURE - I**

**NEP**

**SEMESTER WISE COURSE STRUCTURE FOR UG AND UG (HONS) COURSES**

Semester	Levels of Teaching	Major Disciplinary Courses  (Total Credits: 60/80)	Minor Disciplinary Courses  (Total Credits: 24/32)	Multi-Disciplinary Courses  (Total Credits: 9)	Ability Enhancement courses  (Total Credits: 8)	Skill Enhancement Courses  (Total Credits: 9)	Value added /Common Course  (Total Credits: 8)	Total Credits
I	100 Level	MJD – I Major Disciplinary Course - 1  <span style="border: 1px solid black; border-radius: 50%; padding: 5px; display: inline-block;">4 Cr</span>	MID-I Minor Disciplinary Course -1 (2 to 3 stream of Minor)  <span style="border: 1px solid black; border-radius: 50%; padding: 5px; display: inline-block;">4 Cr</span>	MLDC-I Multi-Disciplinary Course-1  Natural Sciences (3 Cr)  <span style="border: 1px solid black; border-radius: 50%; padding: 5px; display: inline-block;">3 Cr</span>	AEC-I Ability Enhancement course  English -1 (4 Hours Teaching)  Language Course -1  4 hrs of Teaching  <span style="border: 1px solid black; border-radius: 50%; padding: 5px; display: inline-block;">2+1</span>	SKE-I Skill Enhancement Course-1  15 Practicals (3 Cr)  2 to 3 streams of Hands on Training  <span style="border: 1px solid black; border-radius: 50%; padding: 5px; display: inline-block;">3 Cr</span>	VAC I and II NEP special common courses (two)  1. Environmental Sciences/Education (2 Cr)  2. Understanding India (2 Cr)  <span style="border: 1px solid black; border-radius: 50%; padding: 5px; display: inline-block;">4 Cr</span>	Total courses in Semester I - 7  <span style="border: 1px solid black; border-radius: 50%; padding: 5px; display: inline-block;">20</span>
II	100 Level 1	MJD – 2 Major Disciplinary Course – 2  <span style="border: 1px solid black; border-radius: 50%; padding: 5px; display: inline-block;">4 Cr</span>	MID-II Minor Disciplinary Course -2 2 to 3 streams of minor courses  <span style="border: 1px solid black; border-radius: 50%; padding: 5px; display: inline-block;">4 Cr</span>	MLDC-II Multi-Disciplinary Course-2  Physical Sciences  <span style="border: 1px solid black; border-radius: 50%; padding: 5px; display: inline-block;">3 Cr</span>	AEC -II Language course-2  English - 2 (2 Cr)  (4 Hrs of Teaching)  <span style="border: 1px solid black; border-radius: 50%; padding: 5px; display: inline-block;">2+1</span>	SKE-II Skill Development Course  Practicals - 2 (3 Cr)  <span style="border: 1px solid black; border-radius: 50%; padding: 5px; display: inline-block;">3 Cr</span>	VAC III & IV NEP Special/Common courses -3,4  3. Health & Yoga (2 Cr)  4. Digital Techn (2 Cr)  <span style="border: 1px solid black; border-radius: 50%; padding: 5px; display: inline-block;">4 Cr</span>	Total courses in Semester II - 7  <span style="border: 1px solid black; border-radius: 50%; padding: 5px; display: inline-block;">20</span>

Certificate for exiting students provided that they undergo 4 credits Internship during Summer Vacation in the given stream of skill training

Semester	Levels of Teaching	Major Discipline Course (Total Credits: 60/80)	Minor Discipline Course (Total Credits: 24/32)	Multi-Disciplinary Course (Total Credits: 9)	Ability Enhancement courses (Total Credits: 8)	Skill Enhancement Courses (Total Credits: 9)	Value added /Common Course (Total Credits: 8)	Total Credits
III	200 Level	MJD – III & IV Major Disciplinary Course - 3 Major Disciplinary Course - 4  8 Cr	MID-III Minor Disciplinary Course -3  (Allied/Elective) (4 Cr)  4Cr	MDC-III Multi-Disciplinary Course-3  Basics of Humanities (3 Cr)  3Cr	AEC-III Ability Enhancement course Indian Language - 1 (4 Hours Teaching)  2+1 Cr	SKE-III Skill Development Course Practicals (3 Cr)  3Cr	-  0	Total courses in Semester III - 6  20
IV	200 Level	Major 5 (4 Cr) Major 6 (4 Cr) Major 7 (4 Cr)  12Cr	Minor 4  (4 Cr)  4C	-  0	AEC - 4 Indian Language - 2 (2 Cr)  2+1 Cr	-  0	Winter Project (Community engagement 15 days)  2 Cr	Total courses in Semester IV - 6  20

Semester	Levels of Teaching	Major Discipline Course	Minor Discipline Course	Multi-Disciplinary Course	Ability Enhancement courses	Skill Enhancement Courses	Value added /Common Course	Total Credits
V	300 Level	Major 8 Major 9 Major 10  (12 cr)	Minor 5  (4 Cr)	-	-	Summer Internship for 60 Days (4 Cr) (Main -15)	-	Total courses in Semester V - 5  20
VI	300 Level	Major 11 Major 12 Major 13 Major 14  4*4 (16 Cr)	Minor 6  (4 Cr)	-	-	-	-	Total courses in Semester VI - 5  20
Total courses for a UG Degree		15 Courses  60 Cr	6 Courses	3 Courses	4 Course	3 Course	4 Course	Total courses for a 3 yr UG Degree  120C

## UG Hons Degree

Semester	Levels of Teaching	Major Discipline Course  (Total Credits 80)	Minor Discipline Course  (Total Credits 32)	Multi-Disciplinary Course	Ability Enhancement courses	Skill Enhancement Courses	Value added /Common Course	Total Credits
VII	400	Major 16 Major 17 Major 18 (12 cr)  <span style="border: 1px solid black; border-radius: 50%; padding: 5px; display: inline-block;">12</span>	Minor 7 Minor 8 (8 Cr)  <span style="border: 1px solid black; border-radius: 50%; padding: 5px; display: inline-block;">8</span>	-	-	-	-	20
VIII	400	Major 19 Major 20 (8 cr)  <span style="border: 1px solid black; border-radius: 50%; padding: 5px; display: inline-block;">8</span>	-	Research Project (12 Cr)  Research + Viva  (or)  3 Additional Major Courses (3*4=12)  <span style="border: 1px solid black; border-radius: 50%; padding: 5px; display: inline-block;">1</span>				
Total Course		20 courses  80 Credits	<span style="border: 1px solid black; border-radius: 50%; padding: 5px; display: inline-block;">32</span>	<span style="border: 1px solid black; border-radius: 50%; padding: 5px; display: inline-block;">8</span>  <span style="border: 1px solid black; border-radius: 50%; padding: 5px; display: inline-block;">9</span>	<span style="border: 1px solid black; border-radius: 50%; padding: 5px; display: inline-block;">4</span>  <span style="border: 1px solid black; border-radius: 50%; padding: 5px; display: inline-block;">8</span>	<span style="border: 1px solid black; border-radius: 50%; padding: 5px; display: inline-block;">3</span>  <span style="border: 1px solid black; border-radius: 50%; padding: 5px; display: inline-block;">4</span>	<span style="border: 1px solid black; border-radius: 50%; padding: 5px; display: inline-block;">4</span>  <span style="border: 1px solid black; border-radius: 50%; padding: 5px; display: inline-block;">8</span>	52 Course

- UG (hons) Degree by Research
- UG (hons) Degree by Coursework

### UG Hons Degree

Semester	Levels of Teaching	Major DisciplineCourse (Total Credits80)	Minor DisciplineCourse (Total Credits32)	Multi-DisciplinaryCourse	Ability Enhancementcourses	Skill Enhancement Courses	Value added /CommonCourse	Total Credits
VII	400	Major 16 Major 17 Major 18 (12 cr)	Minor 7 Minor 8 (8 Cr)  12      8	-	-	-	-	20
VIII	400	Major 19 Major 20 (8 cr)	-	Research Project (12 Cr)  Research + Viva(or) 3 Additional Major Courses (3*4=12)			12  20	
Total Course		20 courses 80 Credits	8  32	3 Course  9	4 Course  8	3 Course  4	4 Course  8	52 Course

- UG (hons) Degree by Research
- UG (hons) Degree by Coursework

## **EVALUATION:**

### **Total Marks: 100:**

All Credit courses are evaluated for 100 marks. Internal Assessment component is for 25 marks and the End Semester University exam is for 75 marks. In case of Practicals, Project work etc., it is 50:50 marks for Internal and End-Semester Exams.

### **Break up of Internal Assessment marks:**

Total Internal Assessment mark for a theory subject is 25 marks. The breakup is:

a)	Mid Semester Exam (one) - 20 Marks
b)	Percentage of Attendance - 5 Marks
<b>Total - 25 Marks</b>	

Marks for Attendance is as follows:

Below 75%	0
75% - 80%	1
80% - 85%	2
85% - 90%	3
90% - 95%	4
95% - 100%	5

### **Internal Test Scheme:**

Principal of the College schedules the Mid-Semester Exam for all courses during 8/9th week of start of classes. All faculty members are expected to conduct this Mid-Semester exam for 1.30 hr duration and evaluate, upload the marks to Controller of Examinations of University. Colleges are also requested to preserve the answer books of Mid-Semester exams until declaration of results by the University.

### **Internal Assessment marks for Practicals/Project work/ Internships subjects:**

Faculty member in-charge of Lab practicals shall evaluate the practical subjects for 50 marks. The break up is as follows:

a) Observation note/Demo note/Work dairy	20
b) Practical Record/Internship Report	30
<b>Total</b>	<b>50</b>

### **End-Semester University Exam:**

Controller of Examinations (COE) of Pondicherry University schedules the End-Semester exams for all theory and practical subjects based on University calendar. A detailed Exam Time Table shall be circulated to all Colleges atleast 15 days before the start of exams mostly during 15/16th week of the Semester. Question Papers shall be set externally based on BOS approved syllabus. All students who have a minimum of 70% attendance are eligible to attend the endsemester exams. The breakup of end semester marks:

a) Theory subjects (Sec A, Sec B and Sec C) Question from all units of syllabus	75 marks
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b) Practical/Internship Project Work subjects (Based on Practical Exams/Presentation/Viva)	50 marks
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**QUESTION PAPER PATTERN**  
**MAXIMUM MARK: 75**  
**TIME : 3 HOURS**

SECTION A	SECTION B
<b>FIVE QUESTIONS</b> $(5 \times 5 = 25)$ Either Or Type Internal Choice 1 set of questions from each Unit.	<b>FIVE QUESTIONS</b> $(5 \times 10 = 50)$ 5 out of 8 questions 1 question from each Unit compulsory.

Section	Number of Questions	Allocation of questions	Choice Type	Mark per question	Total marks
A	5	1 set from each Unit	Either or type	5	<b>5X5=25</b>
B	5	2 questions from Unit 1  2 questions from Unit 2  2 questions from Unit 3  1 question from Unit 4  1 question from Unit 5	5 out of 8	10	<b>5X10=50</b>

**Consolidation of Marks and passing Minimum**

Controller of Examinations of the University consolidates the Internal Assessment marks uploaded by the Colleges and marks secured by students in end-semester examination. The total marks will be converted into letter grades as shown in the following Table

2. As per NEP Regulations, the passing minimum is 50% marks (IA

+ End semester put together) However, Pondicherry University considers 40% marks as pass during first 3 years of study and students who secured less than 50 will be awarded 'P' (Pass Grade)

**Arrear Exam:**

A student who failed to secure 50% marks in aggregate is declared as Failed and he is eligible to take up supplementary examination by registering to the said course in the following Semester. All other candidates who failed due to shortage of attendance, those who are seeking to improve the grade shall repeat the course.

### **Letter Grades and Calculation of CGPA:**

Total Marks Secured by a student in each subject shall be converted into a letter grade. UGC Framework has suggested a Country wide uniform letter grades for all UG courses. The following Table shows the seven letter grades and corresponding meaning and the grade points for calculation of CGPA.

<b>Equivalent Letter Grade</b>	<b>Meaning</b>	<b>Grade Points for Calculation of CGPA</b>
O	Outstanding	10
A+	Excellent	9
A	Very Good	8
B+	Good	7
B	Above Average	6
C	Average	5
P	Pass	4
F	Fail	0
Ab	Absent	0

In order to work out the above letter grades, the marks secured by a student (Total of IA and Semester End) would be categorized for relative grading. The ranges of marks for each grades would be worked as follows:

Highest marks in the given subject : X

Cut off marks for grading purpose : 50 marks

Passing mark (for 3 year of UG) = 40

Number of grades (excepting P grade) (O,A+,A,B+,B,C) = 6

$$\text{Range of marks} = K = (x - 50)/G$$

The following table given the range of marks and letter grades. According to K value, one of the following grading scheme will be followed.

- (i) If  $K \geq 5$ , then the grades shall be awarded as given in Table II.

<b>Table II</b>		
<b>Range of Marks in %</b>	<b>Letter Grade Points for</b>	<b>Letter Grade Points for</b>
X to $(X-K)+1$	O	10
$(X-K)$ to $(X-2K)+1$	A+	9
$(X-2K)$ to $(X-3K)+1$	A	8
$(X-3K)$ to $(X-4K)+1$	B+	7
$(X-4K)$ to $(X-5K)+1$	B	6
$(X-5K)$ to 50	C	5
40 – 49	P	4
Below 40	F	0
Absent (Lack of Attendance)	Ab	0

(ii) If  $K < 5$ , then the grades shall be awarded as given in Table III.

<b>Table III</b>		
<b>Range of Marks in %</b>	<b>Letter Grade Points for</b>	<b>Letter Grade Points for</b>
80-100	O	10
71-79	A+	9
66-70	A	8
61-65	B+	7
56-60	B	6
50-55	C	5
40-49	P	4
Below 40	F	0
Absent (lack of attendance)	Ab	0

#### **Calculation of Semester Grade Point average and CGPA: Computation of SGPA and CGPA**

The following procedure shall be followed to compute the Semester Grade Point Average (SGPA) and Cumulative Grade Point Average (CGPA):

The SGPA is the ratio of the sum of the product of the number of credits with the grade points scored by a student in all the courses taken by a student and the sum of the number of credits of all the courses undergone by a student,

i.e.  $\text{SGPA } (S_i) = \frac{\sum(C_i \times G_i)}{\sum C_i}$ , Where  $C_i$  is the number of credits of the  $i$ th course and  $G_i$  is the grade point scored by the student in the  $i$ th course.

#### **(i) Example for Computation of SGPA (candidate not failed in any course.)**

Semester	Course	Credit	Letter Grade	Grade point	Credit Point (Credit x Grade)
I	Course 1	3	A	8	$3 \times 8 = 24$
I	Course 2	4	B+	7	$4 \times 7 = 28$
I	Course 3	3	B	6	$3 \times 6 = 18$
I	Course 4	3	O	10	$3 \times 10 = 30$
I	Course 5	3	C	5	$3 \times 5 = 15$
I	Course 6	4	B	6	$4 \times 6 = 24$
		20			139
	SGPA				139/20=6.95

**(ii) Example for Computation of SGPA (candidate has failed in one course.)**

Semester	Course	Credit	Letter Grade	Grade point	Credit Point (Credit x Grade)
I	Course 1	3	A	8	$3 \times 8 = 24$
I	Course 2	4	B+	7	$4 \times 7 = 28$
I	Course 3	3	B	6	$3 \times 6 = 18$
I	Course 4	3	O	10	$3 \times 10 = 30$
I	Course 5	3	C	5	$3 \times 5 = 15$
I	Course 6	4	F	0	$4 \times 0 = 00$
		20			115
			SGPA		115/20=5.75

**(iii) Example for Computation of SGPA (candidate has failed in two courses.)**

Semester	Course	Credit	Letter Grade	Grade point	Credit Point (Credit x Grade)
I	Course 1	3	A14	8	$3 \times 8 = 24$
I	Course 2	4	B+	7	$4 \times 7 = 28$
I	Course 3	3	F	0	$3 \times 0 = 00$
I	Course 4	3	B	6	$3 \times 6 = 18$
I	Course 5	3	C	5	$3 \times 5 = 15$
I	Course 6	4	F	0	$4 \times 0 = 00$
		20			85
			SG A		85/20=4.25

The CGPA shall also be calculated in similar way as shown in examples (i), (ii) and (iii) of SGPA for all subjects taken by the students in all the semesters. However, if any student fails more than once in the same subject, then while calculating CGPA, the credit and grade point related to the subject in which the student fails in multiple attempts will be restricted to one time only. The SGPA and CGPA shall be rounded off to 2 decimal points and reported in the transcripts. In case of audit courses offered, the students may be given (P) or (F) grade without any credits. This may be indicated in the mark sheet. Audit courses will not be considered towards the calculation of CGPA.

**Declaration of Results:** Controller of Examinations (COE) of the University shall declare the results of given UG programme following the CGPA secured by students by the end of 6th Semester and 8th Semester.

**PASS CLASSES**

Range of CGPA	Result
9.0 above	First Class with distinction
6.0 above	First Class
5.0 Below 5.99	Second Class
4.0 4.99	Pass Class

**PONDICHERRY UNIVERSITY**

**RAMANUJAN SCHOOL OF MATHEMATICAL SCIENCES**

**DEPARTMENT OF MATHEMATICS**

**NEP CURRICULUM & SYLLABI  
FOR THE**

**FOUR YEAR B. Sc (Honours) / Research in  
MATHEMATICS WITH STATISTICS**

**OFFERED IN**

**AFFILIATED COLLEGES**

**PONDICHERRY UNIVERSITY**

**TO BE IMPLEMENTED  
WITH EFFECT FROM THE ACADEMIC YEAR  
(2023-24 onwards)**

## Implementation of NEP in Affiliated Colleges NEP courses structure from the Academic Year 2023-24

Title of the Degree Programme (4 years):

Bachelor of Science in Mathematics (Honours with Research)

Titles of the Degree Programme (3 years):

Bachelor of Science in Mathematics with Statistics (B.Sc Mathematics with Statistics)

Titles of Diplomas embodied ( 2 years):

UG Diploma in Mathematics (Dip. Mathematics)

Titles of Certificates embodied (1 year):

UG Certificate of Mathematics

### **I. LIST OF MAJOR COURSES (Single Major)**

SI No	Nature of Course	Title of the Course(Single Major)	Credits	No. Hrs of Teacher
1.	Major 1	Calculus	4	5
2.	Major 2	Matrices and Theory of Equations	4	5
3.	Major 3	Real Analysis - I	4	5
4.	Major 4	Elements of Discrete Mathematics	4	5
5.	Major 5	Real Analysis - II	4	5
6.	Major 6	Group Theory	4	5
7.	Major 7	Elements of Differential Equations	4	5
8.	Major 8	Programming Using SCILAB- Practical	4	5
9.	Major 9	Ring Theory	4	5
10.	Major 10	Complex Analysis-I	4	5
11.	Major 11	Graph Theory	4	5
12.	Major 12	Introduction to Linear Algebra	4	5
13.	Major 13	Complex Analysis-II	4	5
14.	Major 14	Numerical Methods Using SCILAB – Practical	4	5
15.	Major 15	Advanced Algebra	4	5
16	Major 16	Topology	4	5
17	Major 17	Advanced Real Analysis-I	4	5
18	Major 18	Advanced Real Analysis -II	4	5

19	Major 19	Advanced Linear Algebra	4	5
21	Major 20	1. Differential Geometry 2. Number Theory 3. Discrete Dynamical Systems	4	5
22	Major 21	4. Numerical Analysis for Ordinary Differential Equations	4	5
23	Major 22	5. Lattice Theory 6. Integral Transforms and Their Applications 7. Integral Equations 8. Partial Differential Equations <u>Note:-</u> Students shall choose any of the above three courses from (1) to (8) if they do not choose the Research Project/ Dissertation.	4	5

1. In semester V, MJD-8 (Programming Using SCILAB - Practical) will each include two additional hours of practical work. Similarly, in semester VI, MJD-14 (Numerical Methods Using SCILAB - Practical) will include two additional hours of practical work.
2. Tutorial hours of one hour can be added to problem-oriented papers, depending on the available free hours..

## II. LIST OF MINOR COURSES (ELECTIVES/ALLIED/SPECIALISATION)

UG courses having different streams of specialisations may consider the minor stream Eg, B.Com(General), B.Com (Computer Science), B.Com (Foreign Trade), B.Com (Cooperative management), etc.

### a) With Minor Stream I (Within the Department)

Sl No	Title of the Minor Course(Single Major)	Credits	No. Hrs of Teacher
Minor 1	Statistics-I	4	5
Minor 2	Statistics-II	4	5
Minor 3	Statistics-III	4	5
Minor 4	Statistics-IV	4	5
Minor 5	Operations Research - I	4	5
Minor 6	Operations Research - II	4	5
Minor 7	Calculus of variations	4	5
Minor 8	Differential equations and special functions	4	5

**b) Minor Stream II (12 credits from the disciplines + 12 credits from the discipline)**

- o Stream II is designated for students from Arts, Commerce, and Humanities.

<b>Sl No</b>	<b>Title of the Minor Course(Single Major)</b>	<b>Credits</b>	<b>No. Hrs of Teacher</b>
Minor 1	Mathematics of Finance	4	5
Minor 2	Business Statistics	4	5
Minor 3	Numerical Analysis	4	5
Minor 4	Optimization Techniques-I	4	5
Minor 5	Optimization Techniques-II	4	5
Minor 6	Applied Statistics	4	5

**c) Minor Stream III**

- o Minor Stream III is tailored for students pursuing B.Sc. in Physics , Chemistry, other science students(Other than Mathematics).

<b>Sl No</b>	<b>Title of the Minor Course(Single Major)</b>	<b>Credits</b>	<b>No. Hrs of Teacher</b>
Minor 1	Matrices and Trigonometry	4	5
Minor 2	Calculus	4	5
Minor 3	Vector Calculus	4	5
Minor 4	Introduction to Differential Equations	4	5
Minor 5	Fourier Series and Laplace Transforms	4	5
Minor 6	Numerical Analysis	4	5

### **III. MULTI DISCIPLINARY COURSES \***

<b>Sl No</b>	<b>Title</b>	<b>Credits</b>	<b>No. Hrs of Teacher</b>
1.	Natural Sciences	3	4
2.	Physical Sciences	3	4
3.	Humanities / Social Sciences	3	4

\* Common syllabus for all UG courses, Deans of respective schools will design the syllabus

### **\* IV. ABILITY ENHANCEMENT COURSES \***

#### a) English

<b>Sl No</b>	<b>Title UG BOS may choose one course for the given UG Degree</b>	<b>Credits</b>	<b>No. Hrs of Teacher</b>
1.	English Language & Literature	2	4
2.	Functional English	2	4
3.	Spoken English	2	4

#### b) Indian Language

<b>Sl.No</b>	<b>Title</b>	<b>Credits</b>	<b>No. Hrs of Teacher</b>
1.	Literature & Language	2	4
2.	Functional English	2	4
3.	Spoken English	2	4

\* All UG courses will have 4 credits of English and 4 credits of Indian Language

### **V. SKILL ENHANCEMENT COURSES (ONLINE COURSES FROM SKILL INDIA)**

<b>Sl .No</b>	<b>Title of the Skill/Vocational courses</b>	<b>Credit</b>	<b>No. Hrs of Teacher</b>
1.	Quantitative Aptitude ( <b>Practical</b> )	3	4
2.	Logical Reasoning ( <b>Practical</b> )	3	4
3.	Latex ( <b>Practical</b> )	3	4

BOS identifies courses suitable to the students from Skill India courses offered by MOOCs/SWAYAM courses/Any other approved list of 3<sup>rd</sup> party certificate courses sponsored by Industry, GOI at special apprenticeship courses designed by any polytechnic college, Govt. MSME Training centers, BOS may also consider any other skill programmes that other Departments of the given institution. These may include skill training on computer programming, other emerging technologies.

## **VI. VALUE-ADDED COMMON COURSES**

<b>Sl.No</b>	<b>Title</b>	<b>Credits</b>	<b>No. Hrs of Teacher</b>
1.	Understanding India (1)	2	4
2.	Environmental Sciences/ Education (2)	2	4
3.	Health & Wellness / Yoga Education (3)	2	4
4.	Digital Technology Education (4)	2	4

Common course structure and syllabus shall be prepared by:

Dean, School of Social Sciences for subject 1

Dean, School of Life Sciences for subject 2

Director, Directorate of Sports & Physical Education for subject 3

Dean, School of Computer Science for subject 4

## **FIRST-YEAR**

### **SEMESTER I**

<b>Course Code</b>	<b>Type of Course</b>	<b>Credits</b>	<b>Hours</b>	<b>Title of the Course</b>
MJD-I	Major Course 1	4	5	Calculus
MID-I	Minor Course1	4	5	Statistics-I
MLDC-I	Multi-Disciplinary Course 1	3	4	Natural Sciences
AEC-I	Ability Enhancement Course 1	2	4	English-1 or Indian Language - 1
SEC-I	Skill Enhancement Course 1	3	4	Quantitative Aptitude (Practical)
VAC-I	Value-added Course 1	2	4	Understanding India (Theory/Field based)
VAC-II	Value-added Course 2	2	4	Environmental Sciences/ Education
Total Courses/ Credits/ Hours	7 Courses	20	30	

## SEMESTER II

<b>Course Code</b>	<b>Type of Course</b>	<b>Credits</b>	<b>Hours</b>	<b>Title of the Course</b>
MJD-II	Major Course 2	4	5	Matrices and Theory of Equations
MID-II	Minor Course 2	4	5	Statistics-II
MLDC-II	Multi-Disciplinary Course 2	3	4	Physical Sciences
AEC-II	Ability Enhancement Course 2	2	4	English-1 or Indian Language - 1
SEC-II	Skill Enhancement Course 2	3	4	Logical Reasoning (Practical)
VAC-III	Value-added Course 3	2	4	Health, Wellness, Yoga Education, Sports & Fitness
VAC-IV	Value-added Course 4	2	4	Digital Technology Education
Total Courses/ Credits/	7 Courses	20	30	

## SECOND YEAR

### SEMESTER III

<b>Course Code</b>	<b>Type of Course</b>	<b>Credits</b>	<b>Hours</b>	<b>Title of the Course</b>
MJD-III	Major Course 3	4	5	Real Analysis - I
MJD-IV	Major Course 4	4	5	Elements of Discrete Mathematics
MID-III	Minor Course 3	4	5	Statistics - III
MLDC-III	Multi-Disciplinary Course 3	3	4	Humanities/ Social Sciences
AEC-III	Ability Enhancement Course 3	2	4	English-2 or Indian Language - 2
SEC-III	Skill Enhancement Course 3	3	4	Latex (Practical)
Total Courses/ Credits/ Hours	6 Courses	20	27	

**SEMESTER IV**

<b>Course Code</b>	<b>Type of Course</b>	<b>Credits</b>	<b>Hours</b>	<b>Title of the Course</b>
MJD-V	Major Course 5	4	5	Real Analysis - II
MJD-VI	Major Course 6	4	5	Group Theory
MJD-VII	Major Course 7	4	5	Elements of Differential Equations
MID-IV	Minor Course 4	4	5	Statistics - IV
AEC-IV	Ability Enhancement Course 4	2	4	English-2 or Indian Language - 2
VAC-V	Value Added course	2	6	Community Engagement and Service
Total Courses/ Credits/ Hours	6 Courses	20	30	

**THIRD YEAR**

**SEMESTER V**

<b>Course Code</b>	<b>Type of Course</b>	<b>Credits</b>	<b>Hours</b>	<b>Title of the Course</b>
MJD-VIII	Major Course 8	4	4+2	Programming Using SCILAB – Practical
MJD-IX	Major Course 9	4	5*	Ring Theory
MJD-X	Major Course 10	4	5*	Complex Analysis- I
MID-V	Minor Course 5	4	5*	Operations Research - I
SEC	Skill Enhancement Course	4	6	Summer Internship for 45 days
Total Courses/ Credits/ Hours	5 Courses	20	27	

\*Tutorial hours of one hour can be added to problem-oriented papers as per the available free hours

## SEMESTER VI

<b>Course Code</b>	<b>Type of Course</b>	<b>Credits</b>	<b>Hours</b>	<b>Title of the Course</b>
MJD-XI	Major Course 11	4	5*	Graph Theory
MJD-XII	Major Course 12	4	5*	Introduction to Linear Algebra
MJD-XIII	Major Course 13	4	5*	Complex Analysis- II
MJD-XIV	Major Course 14	4	5*	Numerical Methods Using SCILAB – Practical
MID-VI	Minor Course 6	4	5*	Operations Research - II
Total Courses/ Credits/ Hours	5 Courses	20	26	

\*Tutorial hours of one hour can be added to problem oriented papers as per the available free hours

## FOURTH YEAR

### SEMESTER VII

<b>Course Code</b>	<b>Type of Course</b>	<b>Credits</b>	<b>Hours</b>	<b>Title of the Course</b>
MJD-XV	Major Course 15	4	5*	Advanced Algebra
MJD-XVI	Major Course 16	4	5*	Topology
MJD-XVII	Major Course 17	4	5*	Advanced Real Analysis-I
MID-VII	Minor Course 7	4	5*	Calculus of Variations
MID-VIII	Minor Course 8	4	5*	Differential equations and special functions
Total Courses/ Credits/ Hours	5 Courses	20	25	

\*Tutorial hours of one hour can be added to problem-oriented papers as per the available free hours

## SEMESTER VIII

<b>Course Code</b>	<b>Type of Course</b>	<b>Credits</b>	<b>Hours</b>	<b>Title of the Course</b>
MJD-XVIII	Major Course 18	4	5*	Advanced Real Analysis -II
MJD-XIX	Major Course 19	4	5*	Advanced Linear Algebra
		12	15	Research Project / Dissertation
MJD-XX	Major Course 20	4	5*	1. Differential Geometry 2. Number Theory 3. Discrete Dynamical Systems 4. Numerical Analysis for Ordinary Differential Equations 5. Lattice Theory 6. Integral Transforms and Their Applications 7. Integral Equations 8. Partial Differential Equations
MJD-XXI	Major Course 21	4	5*	
MJD- XXII	Major Course 22	4	5*	
Total Courses/ Credits/ Hours	5 Courses	20	25	<u>Note:-</u> Students shall choose any of the above three courses from (1) to (8) if they do not choose the Research Project/ Dissertation.

\*Tutorial hours of one hour can be added to problem oriented papers as per the available free hours

\*Free hours apart from Major courses can be utilized for research project and Dissertations.

## **LIST OF MINOR COURSES (ELECTIVES/ALLIED/SPECIALISATION)**

These courses are designed for students from Physics, Chemistry, Biology, Computer Science, B.Com (General), B.Com (CS), etc. These courses will be floated depending on the number of students registering and the availability on the faculty. The number students may be restricted depending on the available classroom facility and first-cum-first serve basis.

### **a) With Minor Stream I (Within the Department)**

<b>Course Code</b>	<b>Type of Course</b>	<b>Credits</b>	<b>Hours</b>	<b>Title of the Course</b>
MID-I	Minor Course 1	4	5	Statistics-I
MID-II	Minor Course 2	4	5	Statistics-II
MID-III	Minor Course 3	4	5	Statistics-III
MID-IV	Minor Course 4	4	5	Statistics-IV
MID-V	Minor Course 5	4	5	Operations Research-I
MID-VI	Minor Course 6	4	5	Operations Research-II
MID-VII	Minor Course 7	4	5	Calculus of variations
MID-VIII	Minor Course 8	4	5	Integral equations

### **b) With Minor Stream II**

<b>Course Code</b>	<b>Type of Course</b>	<b>Credits</b>	<b>Hours</b>	<b>Title of the Course</b>
MID-I	Minor Course 1	4	5	Mathematics of Finance
MID-II	Minor Course 2	4	5	Business Statistics
MID-III	Minor Course 3	4	5	Numerical Analysis
MID-IV	Minor Course 4	4	5	Optimization Techniques I
MID-V	Minor Course 5	4	5	Optimization Techniques II
MID-VI	Minor Course 6	4	5	Applied Statistics

**c) With Minor Stream III (The subjects are for other disciplines)**

Course Code	Type of Course	Credits	Hours	Title of the Course
MID-I	Minor Course 1	4	5	Matrices and Trigonometry
MID-II	Minor Course 2	4	5	Calculus
MID-III	Minor Course 3	4	5	Vector Calculus
MID-IV	Minor Course 4	4	5	Introduction to Differential Equations
MID-V	Minor Course 5	4	5	Fourier Series and Laplace Transforms
MID-VI	Minor Course 6	4	5	Numerical Analysis

**Skill Enhancement Courses (Online Courses from Skill India)**

Course Code	Offered in the Semester	NEP Classification	Credits	Hours	Title of the Course
SEC-I	I	Skill Enhancement Course 1	3	4	Quantitative Aptitude <b>(Practical)</b>
SEC-II	II	Skill Enhancement Course 2	3	4	Logical Reasoning <b>(Practical)</b>
SEC-III	III	Skill Enhancement Course 3	3	5	Latex <b>(Practical)</b>

**Multi-Disciplinary Course for all Arts, Commerce, and Science students(Except Mathematics)**

Course Code	Offered in the Semester	NEP Classification	Credits	Hours	Title of the Course
MLDC-II	II	Multi-Disciplinary Course 2	3	4	Basic Mathematics

## **LIST OF MAJOR COURSES (SINGLE MAJOR)**

### **I YEAR: SEMESTER – I** **MAJOR - 1: CALCULUS -4 CREDITS (60 HOURS)**

#### **UNIT I :**

nth derivative – Standard results – Trigonometrical transformation – Formation of equations involving derivatives – Leibnitz formula

#### **UNIT II :**

Total differential coefficients – Euler's theorem – Partial derivatives of a function of two functions - Maxima and Minima of two variables – Lagrange's method of undetermined multipliers

#### **UNIT- III :**

Circle, radius and centre of curvature – Cartesian formula for radius of curvature – envelope

#### **UNIT- IV :**

Integration of rational algebraic functions – Integration of irrational algebraic functions - Properties of definite integrals

#### **UNIT- V :**

Integration by parts – reduction formula, Bernoulli's formula - Evaluation of double integral (Cartesian form only) – Triple integral (Cartesian form only)

#### **Prescribed Text(specify sections clearly)**

Calculus Volume — I, T. K. Manickavachagom Pillai, Printers and Publishers (May1992 Edition)

Unit 1: Chapter 3 – 1.1, 1.2, 1.3, 1.4, 1.5, 1.6, 2.1,

Unit 2: Chapter 8-1.3, 1.4, 1.5, 1.6, 1.7, 4, 4.1, 5,

Unit 3: Chapter 10 – 1.1, 1.2, 2.1, 2.2, 2.3, 2.4, 2.5

Calculus Volume II , S.Narayanan and T.K. Manickavasagam Pillai (2008)

Unit 4 : Chapter 1 : 7.3, 7.4, 7.5, 8, 11

Unit 5 : Chapter 1: 12,13,14, 15.1, and Chapter 5: 2, 4,

#### **Reference books**

1. Integral Calculus, N. P. Bali, Laxmi Publications, Delhi, (1991)
2. Calculus(2nd Edition), Lipman Bers and Frank Karal, Holt McDougal, 1976.
3. Thomas' Calculus 12th Edition, George B.Thomas, Maurice D.Weir and Joel Hass, Pearson Education, 2015.

## I – YEAR: SEMESTER - II

### MAJOR – 2: MATRICES AND THEORY OF EQUATIONS 4 CREDITS (60 HOURS)

#### Course Objectives:

1. To introduce the idea of matrices and to learn about the algebra of matrices
2. To solve system linear equations using matrix Theory

	Course Outcome
<b>CO 1</b>	To learn the relation between the co-efficient and roots of polynomial equations.
<b>CO 2</b>	To learn various methods for solving polynomial equations and study the nature & position of roots.
<b>CO 3</b>	Analytic Methods for solving the polynomial equation of degrees 3 & 4.

#### Unit I: (Section 1.1, 1.2, 1.3,1.4,1.5 of [1])

Linear systems - Matrices - Dot product and Matrix multiplication - Properties of Matrix operation, Matrix transformations.

#### Unit II: ( Section 1.6,1.7,1.8[1])

Solutions of Linear systems of equations - Row echelon from reduced row echelon form – Polynomial interpolation - The inverse of a Matrix. - Linear Systems and inverses - LU- Factorization Method.

#### Unit III: (Sections 5.1,5-2,.5.3 of [2])

Division algorithm - Relation between roots and coefficients - Sum of the powers of the roots.

#### Unit IV: (section 5.4,5.5,5.6 ,5.7 of [2] )

Reciprocal equations - Transformation of equations: - Multiple roots - Nature of position of roots - Sturm's Theorem.

#### Unit V: ( 5.8,5.9,5.10 of [2])

Cardan's Method for solving Cubic equations – Ferrari's Method for solving biquadratic equations - New Newton's Method- Horner's Method

#### Text Books

1. Bernard Kolman Drid R. Hill, Introductory Linear Algebra, (8e), Pearson India (2011)
2. S. Arumugam and A Thangaand Isaac, Set Theory Number System and Theory of Equations, New Gamma publishing house(1997.).

#### References:

1. Theory of Equations, Hari Kishan, Atlantic Publishers, 2022
- 2.Theory of Equations, Lalji Prasad, New Revised Edition, 2016

## **II YEAR: SEMESTER - III**

### **MAJOR – 3: REAL ANALYSIS- I**

**4 CREDITS (60 HOURS)**

#### **UNIT I :**

Sets and elements — Operations on sets — Functions - Real valued functions- Equivalence— Countability— Real numbers—Least upper bound—Greatest lower bound.

#### **UNIT II :**

Definition of sequence and subsequence — Limit of a sequence —Convergent sequence — Bounded sequence Monotone sequence -Operationonconvergentsequence-Limitsuperiorandlimitinferior—Cauchy sequence

#### **UNIT III :**

Convergence and divergence- Series with non-negative terms -Alternating series—Conditional convergence and absolute convergence- Tests for absolute convergence-Series whose terms form a non- increasing sequence— Summation by parts.

#### **UNIT IV :**

Limit of a function on the real line - Metric spaces (Examples 4 and 5 under 4.2 to be omitted)-Limits in metric spaces.

#### **UNIT V :**

Functions continuous at a point on the real line. Reformulation —Functions continuous on a metric space - Open sets and closed sets –Discontinuous functions on R

#### **Prescribed Text**

Methods of Real Analysis, Treatment as in Richard R.Goldberg(1970)

Unit 1 :Chapter1

Unit 2,3: Chapter2andChapter3(upto3.8)

Unit 4 : Chapter4

Unit 5 :Chapter5

#### **Reference Books**

1. A First Course in Mathematical Analysis- D Somasundaram & B Choudhury-Narosa Publishing house, New Dehli
2. Introduction to Calculus and Analysis, Vol. I, Richard Courant and Fritz John, Springer 1999.
3. Introduction to Real Analysis, 4<sup>th</sup> Edition, Robert G.Bartle and Donald R.Sherbert,Wiley-2014.

## **MAJOR – 4: ELEMENTS OF DISCRETE MATHEMATICS** **4 CREDITS (60 HOURS)**

### **Course Objectives:**

1. Able to understand the concepts of sets and determine whether a relation is a function and identify the domain and range of a function.
2. Understand the ideas of the basis step and the inductive step in a proof by Mathematical induction and recurrence relations

	Course Outcome
<b>CO 1</b>	To understand the basic concepts of Permutations and combinatorics
<b>CO 2</b>	To familiarize the applications of Difference sequences and Catalan numbers.
<b>CO 3</b>	To understand the concepts and significance of lattices and Partition of numbers.

### **Unit I:**

The Integers – The Division algorithm – Divisibility – The Euclidean Algorithm – Prime numbers.

### **Unit II:**

Mathematical induction – Weak form and strong form – Recursively defined sequences – Solving recurrence relations – The characteristic polynomials – Solving recurrence relations – Generating functions – The principle of inclusion- Exclusion – The addition and multiplication rules.

### **Unit III:**

The pigeonhole principle–Permutations – Combinations –Repetitions – Derangements – The binomial theorem.

### **Unit IV:**

Catalan numbers – Difference sequences - stirling numbers of the first kind and second kind.

### **Unit -V:**

Partition of numbers – Ferrers diagram – A geometric application – Lattice Paths – Schroder numbers.

### **Text Books**

1. Edgar G. Goodaire, Michael M. Parmenter , Discrete Mathematics with Graph Theory (Third Edition), PHI Learning Private Ltd., New Delhi – 2011.
2. Richard A. Brualdi, Introductory Combinatorics, (Fourth Edition), Pearson Education 2004.

### **Reference Books**

1. Richard Johnson bauth, Discrete Mathematics – 5<sup>th</sup> Edition, Pearson Education Asia, New Delhi, 2002.
2. Ralph. R. Grimaldi - Discrete and Combinatorial Mathematics: An Applied Introduction – 4<sup>th</sup> Edition, Pearson Education Asia, Delhi, 2002
3. C.L. Lie, Elements of Discrete Mathematics — the Mc Graw-Hill, Inc. India 1985.
4. Bernard Kolman, Robert C. Busby, Sharan Cutler Ross, Discrete Mathematical Structure, 4<sup>th</sup> Edition print Pearson Education Pvt. Ltd., New Delhi 2003

**II - YEAR: SEMESTER - IV**

**MAJOR – 5 : REAL ANALYSIS-II – 4 CREDITS (60 HOURS)**

**UNIT I:**

More about open sets - Connected sets. Bounded sets and totally bounded sets - Complete metric spaces.

**UNIT II:**

Compact metric spaces Continuous functions on compact metric Spaces - Continuity of the inverse function - Uniform continuity.

**UNIT III:**

Sets of measure zero - Definition of the Riemann integral - Existence of the Riemann integral- Properties of the Riemann integral

**UNIT IV :**

Derivatives - Rolle's theorem - The Law of the Mean - Fundamental theorem of Calculus - Improper integrals.

**UNIT V:**

Hyperbolic function - The exponential function - The logarithmic function - Definition of  $x^a$  - The trigonometric function - Taylor Theorem -L'Hopital's rule.

**Prescribed Text**

Methods of Real Analysis, Treatment as in Richard R. Goldberg, (1970)

Unit 1: 6.1 to 6.4      Unit 2: 6.5 to 6.8      Unit 3: 7.1 to 7.4

Unit 4: 7.5 to 7.10      Unit 5: 8.1 to 8.7

**Reference Books**

1. First Course in Mathematical Analysis by Dr. Somasundaram& B Choudhury-  
Narosa Publishing House, New Delhi
2. Real Analysis- by Shanti Narayanan e-Learning Source

## **MAJOR – 6 : GROUP THEORY – 4 CREDITS (60 HOURS)**

### **Course Objectives:**

1. To understand groups and sub groups
2. To understand quotient groups- Homomorphism.

#### **Unit I**

(12 hours)

Introduction to Groups - Definition and Examples of Groups – Elementary Properties of Groups – Subgroups - Subgroup Tests - Examples of Subgroups.

#### **Unit II**

(12 hours)

Cyclic Groups - Properties of Cyclic Groups - Classification of Subgroups of Cyclic Groups - Permutation Groups - Cycle Notation - Properties of Permutations.

#### **Unit III**

(12 hours)

Isomorphisms - Cayley's Theorem - Properties of Isomorphisms – Automorphisms - Properties of Cosets - Lagrange's Theorem and Consequences.

#### **Unit IV**

(12 hours)

External Direct Products – Properties of External Direct Products - The Group of Units Modulo n as an External Direct Product - Normal Subgroups - Factor Groups - Applications of Factor Groups - Internal Direct Products.

#### **Unit V**

(12 hours)

Group Homomorphisms - Properties of Homomorphisms - The First Isomorphism Theorem - Fundamental Theorem of Finite Abelian Groups - The Isomorphism Classes of Abelian Groups.

### **Text Book:**

Joseph A. Gallian, Contemporary Abstract Algebra, 8<sup>th</sup> Edition, Cengage Learning India Private Limited Chapter 2 to Chapter 12

### **Reference books**

- 1 M. Artin: Algebra, Prentice-Hall of India, 1991.
2. I.N. Herstein: Topics in Algebra, Wiley Eastern Ltd., New Delhi, 1975.

**MAJOR – 7 : ELEMENTS OF DIFFERENTIAL EQUATIONS – 4 CREDITS**  
**(60 HOURS)**

**Course Objectives:**

1. To understand ordinary and first order partial differential equations and their applications
2. To enable students to understand solving the first and second order ODES and first order PDEs.

	<b>Course Outcome</b>
<b>CO 1</b>	To solve a system of first order ODEs
<b>CO 2</b>	To analyze the stability of a Dynamical System using Differential Equations and their solutions
<b>CO 3</b>	To Solve First Order Partial Differential Equations

**Unit I:**

Exact differential equations- Integrating factors – Linear differential equations- Bernoulli equation – Modeling: Electric circuits – Orthogonal trajectories of curves.

**Unit II:**

Homogeneous linear equations of second order – Second order homogeneous equations with constant coefficients – Case of complex roots- Complex exponential function – Differential operators – Modeling: Free oscillations – Euler-Cauchy equation – Existence and uniqueness theory – Wronskian.

**Unit III:**

Nonhomogeneous equations – Solution by undetermined coefficients – Solution by variation of parameters – Modeling of electric circuits – Higher order linear differential equations – Higher order homogeneous equations with constant coefficients.

**Unit IV:**

Introduction: vectors, matrices, eigenvalues – Introductory examples – Basic concepts and theory – Homogeneous systems with constant coefficients, phase plane, critical points – Criteria for critical points, Stability.

**Unit V:**

Non-linear first order PDEs : Compatible systems- Solutions of Quasi-linear equations-Charpit's method- Special Types of Charpits Method, -Integral surfaces through a given The Cauchy problem for Quasi Linear case and nonlinear first order PDEs

**Text Book**

Erwin Kreyszig, Advanced Engineering Mathematics, 8<sup>th</sup> Edition, John Wiley & Sons, 1999.

Unit-I: Sections 1.5-1.8;

Unit-II: Sections 2.1-2.7;

Unit-III: Sections 2.8-2.10, 2.13, 2.14;

Unit-IV: Sections 3.0-3.4;

K. Shankara Rao, Introduction to Partial Differential Equations, PHI Publications, 3<sup>rd</sup> Edition. 2011. – Chapter 1

**Reference Books**

1. George F. Simmons, Differential Equations, Tata McGraw-Hill, New Delhi, 1972.
2. Boyce and Di Prima, Differential Equations and Boundary Value Problems, Wiley, 10<sup>th</sup> edition 2012.

3. Earl A. Coddington, An Introduction to Ordinary Differential Equations, Prentice Hall of India Private Ltd, 1991.

### **III – YEAR: SEMESTER - V**

### **MAJOR – 8 : PROGRAMMING USING SCILAB– PRACTICAL - 4 CREDITS (60 HOURS)**

#### **UNIT I:**

Overview of Scilab - How to get started with Scilab - Getting help from Scilab demonstrations and macros – The Console – The Editor – Batch Processing Creating Real Variables - Elementary mathematical functions – Booleans – Complex Numbers – Integrers – Floating Points – Strings – Dynamic Variables

#### **UNIT II:**

Matrices – Create Matrices of Real Variables – Accessing Elements of Matirces - Matrices are dynamic – Elementwise Operations Conjugate transpose and non-conjugate transpose - Multiplication of two vectors Comparing two real matrices - Issues with floating point integers - More on elementary functions - Higherlevel linear algebra features

#### **UNIT III:**

Looping and branching - The if , select , for and while statements The break and continue statements Functions - Function libraries - Managing output arguments Levels in the call stack - The return statement - Debugging functions with pause

#### **UNIT IV:**

Plotting - 2D plot - Contour plots - Titles, axes and legends - Export

#### **UNIT V:**

Solving Ordinary Differential Equations using Scilab

#### **Prescribed Text**

Introduction to Scilab- Michael Baudin From Scilab Consortium, 2010Chapters 1to 8 (Book Freely Downloadable in Internet)

1. Plotting Using Scilab –An open Source Document–[www.openeering.com](http://www.openeering.com)

#### **Reference Books**

1. Modeling and Simulation in Scilab,Stephen L. Campbell, Jean-PhilippeChancelierand Ramine Nikoukhah
2. An Introduction to Scilab from a Matlab User's Point of View by Eike Rietsch

## **MAJOR – 9 : RING THEORY – 4 CREDITS (60 HOURS)**

- Unit I** (12 hours)  
Introduction to Rings - Motivation and Definition of Rings – Examples of Rings – Properties of Rings – Subrings - Definition and Examples of Integral Domains – Fields - Characteristic of a Ring.
- Unit II** (12 hours)  
Ideals - Factor Rings - Prime Ideals and Maximal Ideals - Definition and Examples of Ring Homomorphisms - Properties of Ring Homomorphisms - The Field of Quotients.
- Unit III** (12 hours)  
Polynomial Rings - The Division Algorithm and Consequences - Principal ideal domain - Factorization of Polynomials - Reducibility Tests - Irreducibility Tests.
- Unit IV** (12 hours)  
Unique Factorization in  $\mathbb{Z}[x]$  - Weird Dice: An Application of Unique Factorization - Divisibility in Integral Domains – Irreducibles and Primes.
- Unit V** (12 hours)  
Historical Discussion of Fermat's Last Theorem - Unique Factorization Domains - Euclidean Domains.

### **Text Book:**

Joseph A. Gallian, Contemporary Abstract Algebra, 8<sup>th</sup> Edition, Cengage Learning India Private Limited  
Chapter 12 to Chapter 18

### **Reference books**

- 1 M. Artin: Algebra, Prentice-Hall of India, 1991.
2. I.N.Herstein: Topics in Algebra, Wiley Eastern Ltd., New Delhi, 1975.
3. David S. Dummit and Richard M. Foote, Abstract Algebra (Third Edition), John Wiley and sons, 2004

## **MAJOR – 10 : COMPLEX ANALYSIS – I – 4 CREDITS (60 HOURS)**

### **UNIT I:**

Complex numbers-Definitions-Algebraic properties–Cartesian co-ordinates - Triangular inequality - Polar Form - Powers and roots -Region in the complex plane.

### **UNIT II:**

Analytic functions - Functions of a complex variable -Mapping -Limit - Theorems on limits - Continuity - Derivatives -Differentiation formula-Cauchy Riemann equations-Sufficient conditions.

### **UNIT III:**

Cauchy Riemann equations in polar form - Analytic functions -Harmonic functions.

### **UNIT IV:**

Elementary functions - Exponential function – Trigonometric functions and their--Hyperbolic functions– Logarithmic function – Branches - properties of logarithms - Complex exponents -Inverse trigonometric & hyperbolic functions.

### **UNIT V:**

Mapping by elementary functions - The linear function  $1/z$  – Linear fractional transformation function  $w=\exp(z)$ ,  $W=\sin z$ ,  $W=\cos z$ ,  $z^{1/2}$ -Successive transformation  $W=z+1/z$ .

### **Prescribed Text:**

Complex Variables and Applications, James Ward Brown and Ruel V Churchill, McGraw-Hill, International Edition (2009)

UNIT I-chapter 1UNIT II -chapter 2UNIT III -chapter 2UNIT IV -chapter 3UNIT V -chapter 4

### **Reference Books**

1. Functions of a Complex Variable by B. S. Tyagi – Kedar Nath Ram Nath Publishers(P)Ltd.
2. Complex Analysis by P. Duraipandian and Kayalal Pachaiappa –S.Chand & Co.
3. S.Ponnusamy, Foundations of Complex Analysis, (2<sup>nd</sup> Edition), Narosa, 2011. V. Karunakaran, Complex Analysis, (2<sup>nd</sup> Edition), Narosa 2005

### **III – YEAR : SEMESTER – VI**

#### **MAJOR – 11: GRAPH THEORY – 4 CREDITS (60 HOURS)**

##### **Course Objectives:**

1. To introduce the notion of graphs and the basic terminologies in graphs
2. To learn the concept of spanning trees, Cayley's formula and to introduce the concept of connectivity and edge connectivity of graphs

##### **Unit I:**

Graphs – Subgraphs – Isomorphism of graphs – Degrees of Vertices – Paths and Connectedness – Automorphism of a Simple Graph – Trees – Centers and Centroid.

##### **Unit II:**

Counting the Number of Spanning Trees – Cayley's Formula– Vertex Cuts and Edge Cuts – Connectivity and Edge-connectivity.

##### **Unit III:**

Vertex Independent sets and Vertex Coverings – Edge-Independent Sets – Matchings and Factors – MAugmenting Paths – Matchings in Bipartite Graphs – Halls Theorem on Bipartite graphs – Tutte's 1-Factor Theorem (without proof).

##### **Unit IV:**

Eulerian graphs – Necessary and sufficient condition for Eulerian graphs – Hamiltonian graphs – Dirac theorem –Closure of a graph.

##### **Unit V:**

Vertex Coloring – Chromatic Number –Critical Graphs – Brooks' Theorem – Edge Colorings of Graphs – Vizing's Theorem (without proof) – Planar and Nonplanar Graphs – Euler's Formula and its Consequences.

##### **Text Book:-**

##### **1. R. Balakrishnan and K. Ranganathan, A Textbook of Graph Theory (Universitext), Second Edition, Springer New York 2012.**

Chapter 1: 1.1-1.6 Chapter 3: 3.1-3.3 Chapter 4: 4.1-4.5 Chapter 5: 5.1-5.5

Chapter 6: 6.1-6.3 Chapter 7: 7.1,7.2,7.3.1, 7.6.2 Chapter 8: 8.1-8.3.

##### **Reference Books:-**

1. Bondy, J.A and Murthy, U.S.R, Graph Theory with Applications, Macmillan Press Ltd, New Delhi – (1976).Douglas B. West, Introduction to Graph Theory, Second Edition, PHI Learning Private Ltd, New Delhi-2011.
2. G. Chartrand, Linda Lesniak and Ping Zhang, Graphs and Digraphs, Fifth Edition, CRC press 2011.

## **MAJOR – 12 : INTRODUCTION TO LINEAR ALGEBRA – 4 CREDITS (60 HOURS)**

### **Course Objectives:**

1. To understand vector spaces by its definition and examples.
2. To know how to represent a linear transformation by a matrix

	<b>Course Outcome</b>
<b>CO 1</b>	To learn elementary operations on Matrices and how to apply them to find the solutions of a system of equations
<b>CO 2</b>	To learn the properties of determinant of matrices
<b>CO 3</b>	To know about inner products and orthogonalization

### **Unit I:**

Abstract Algebra Concepts – Groups- Subgroups- Fields- examples Vector space- Subspace-linear combinations and systems of linear equations- Linear dependence and linear independence- Basis and dimension.

### **Unit II:**

Linear Transformations- Null spaces- Range spaces- Dimension theorem- Matrix representation of linear transformation- composition of linear transformations and Matrix multiplication- Invertability and Isomorphism- The change of coordinate matrix.

### **Unit III:**

Elementary matrix Operations and elementary matrices- The rank of a matrix and matrix inverses- systems of linear equations- Theory and computation

### **Unit IV:**

Determinants of order 2 and order n- properties of determinants- Important facts about determinants- Eigen values and Eigen vectors- Diagonalizability- Invariant spaces and Cayley-Hamilton theorem.

### **Unit V:**

Inner products and norms- The Gram-Schmidt orthogonalisation process and orthogonal complements.

### **Text Book**

Stephen H. Friedberg, Arnold J. Insel and Lawrence E. Spence, Linear Algebra, 4<sup>th</sup> Edition, Prentice Hall of India Pvt. Ltd., 2006

Unit I: 1.2 to 1.6      Unit II: 2.1 to 2.5      Unit III: 3.1 to 3.4

Unit IV: 4.1 to 4.4 and 5.1 to 5.2, 5.4      Unit V: 6.1, 6.2

### **Reference Books**

1. S. Kumaresan, Linear Algebra Geometric Approach, Prentice Hall of India Pvt. Ltd., 2000.
2. I. N. Herstein, Topics in Algebra, 2<sup>nd</sup> Edition, John Wiley & Sons, 2003.
3. David C. Lay, Linear Algebra and Applications (2<sup>nd</sup> Edition), Addison Wesley, 1997.
4. John B. Fraleigh, A First Course in Abstract algebra, (7<sup>th</sup> Edition), Pearson 2013.

## **MAJOR – 13: COMPLEX ANALYSIS-II– 4 CREDITS (60 HOURS)**

### **UNIT I:**

Contour integrals- Examples - The Cauchy-Goursat theorem -A preliminary lemma- Proof of Cauchy-Goursat's theorem -Simply and multiple connected domains.

### **UNIT II:**

The Cauchy integral formula -Derivatives of analytic functions-Morera's theorem - Maximum moduli of functions- Liouville's The fundamental theorem of algebra.

### **UNIT III:**

Convergence of sequences and series - Taylor series -Observations and examples-Laurent Series (statement only).

### **UNIT IV:**

Singularities- Definitions and The residue theorem - The principal part of a function- Residues and poles – zeros and poles of order m.

### **UNIT V:**

Type 1:  $\int_{-\infty}^{\infty} \frac{p(x)}{q(x)} dx$ , Type 2:  $\int_{-\infty}^{\infty} \frac{p(x)}{q(x)} \sin ax dx$  (or)  $\int_{-\infty}^{\infty} \frac{p(x)}{q(x)} \cos ax dx$

Type 3:  $\int_0^{2\pi} F(\sin \theta, \cos \theta) d\theta$ , Where p(x) and q(x) are real polynomials with no factor in common, and q(x) has no real zeros.

### **Prescribed Text**

Complex Variables and Applications, James Ward Brown and Ruel V Churchill, McGraw-Hill, International Edition(1990)

Unit I : Chapter 4:Section 34-38 Unit II:

Chapter 4 Section 39-43

Unit III:Chapter 5:Section 44-48 Unit

IV:Chapter 6:Section 53-57

UnitV:Chapter 6:Section 58-60

### **Reference Books**

1. Functions of a Complex variable by B. S. Tyagi – KedarNath RamNath Publishers(P)Ltd.
2. Complex Analysis by P. Duraipandian and Kayalal Pachaiappa –S.Chand&Co.
3. S. Ponnusamy, Foundations of Complex analysis, (2<sup>nd</sup> Edition), Narosa,2011.  
V. Karunakaran,Complex Analysis,(2<sup>nd</sup>Edition),Narosa2005

**MAJOR – 14: NUMERICAL METHODS USING SCILAB-PRACTICAL – 4 CREDITS (60Hrs)****UNIT I:**

Numerical solution of algebraic and transcendental equations – Bolzano's bisection method - Successive approximation method – Regula falsi method – Newton-Raphson method.

**UNIT II:**

Numerical solution of simultaneous linear algebraic equations – Gauss elimination method - Gauss Jordan elimination method – Gauss Seidel iteration method.

**UNIT III:**

Finite difference operator - Interpolation – Newton-Gregory forward and backward interpolation – Newton's divided difference formula – Lagrange's interpolation formula for uneven intervals – Gauss interpolation formula – Numerical differentiation – Numerical Integration – Trapezoidal rule – Simpson's 1/3rd rule.

**UNIT IV:**

Numerical solutions of Ordinary differential equations of first and second order – Simultaneous equations – Taylor series method – Picard's method.

**UNIT V:**

Euler's method – Improved Euler's Method - Modified Euler's Method – Runge-Kutta method of second and fourth order – Milne's predictor-corrector method.

**Text book**

Numerical Methods in Science and Engineering,  
M.K.Venkataraman,National Publication Co,Chennai(2001)  
Unit1: Chapter 3 and 4  
Unit2: Chapter 5  
Unit3: Chapter 6 and 9  
Unit4:Chapter11(Relevantportions)Unit5:Chapter11(Relevantportions)

**Reference Books**

Computer-Oriented Numerical Methods by V.Rajaram–PHI(P)Ltd.

























Differential Equations.

- <sup>1</sup> K. Shankara Rao, Introduction to Partial Differential Equations, PHI Publications, Edition: 2011.  
<sup>2</sup> T. Amarnath, An Elementary Course in Partial Differential Equations, Narosa Publishing House, 2010.

## **Books for Reference**

- 1 I. N. Sneddon, Elements of Partial Differential Equations, McGraw Hill, International Edition, 1986.
  - 2 F. John, Partial Differential Equations, Springer Verlag, 1975.
  - 3 Lawrence C. Evans, Partial Differential Equations, Graduate Studies in Mathematics, 1998.

**MINOR STREAM - I**  
**MINOR – 1 : STATISTICS-I – 4 CREDITS (60 HOURS)**

**Course Objectives**

- \* To introduce the basic concepts of probability and statistics, including sample spaces, events, probability rules, random variables, and probability distributions.
- \* To develop an understanding of the mathematical foundations of probability and statistics, such as expectation, variance, and covariance.
- \* To apply probability and statistics to solve problems in a variety of contexts, such as business, engineering, and science.

**Unit I:** (Chapter 3 – 3.1, 3.2, 3.3, 3.4, 3.5, 3.8, 3.9, 3.10, 3.11, 3.12, 3.13)

Theory of Probability - I – Mathematical and Statistical Probability, Axiomatic approach to Probability – Some theorems on probability– Simple problems

**Unit II:** (Chapter 4 – 4.1, 4.2, 4.3)

Theory of Probability – II : Extended axiom of addition and axiom of continuity – Bayes' theorem – Geometric probability - Simple problems.

**Unit III:** (Chapter 5 – 5.1, 5.2, 5.3, 5.4, 5.5)

Distribution function – Discrete random variable – Continuous random variable – Two dimensional random variable – Simple problems.

**Unit IV:** (Chapter 6 - 6.1, 6.2, 6.3, 6.4, 6.5, 6.6 )

Mathematical Expectation : Mathematical expectation or expected value of a random variable – expected value of function of a random variable – Properties of expectation – Properties of variance – Covariance – Simple problems.

**Unit V:** (Chapter 8 – 8.1, 8.2, 8.3, 8.4, 8.5, 8.7)

Special Discrete Probability Distributions : Discrete uniform distribution – Bernoulli distribution – Binomial distribution – Poisson distribution – Geometric distribution -

**Text Book:** S.C. Gupta & V.K. Kapoor , Fundamentals of Mathematical Statistics- Sultan Chand and Sons,12th Edition ,2022

**Reference Books:**

1. S.P. Gupta, Statistical methods- Sultan Chand and Sons, 45th Edition 2017
2. R.S.N.Pillai & V. Bagavathi, Statistics –S.Chand & company LTD, Reprint 2014

## **MINOR -2 : STATISTICS-II – 4 CREDITS (60 HOURS)**

### **Course Objectives**

- To introduce the normal distribution and its properties.
- To develop an understanding of the special continuous probability distributions.
- To introduce the concept of correlation and its measurement.
- To develop an understanding of the linear and curvilinear regression models.
- To introduce the concepts of theory of attributes and its applications.

### **Unit I:** (Chapter 9 – 9.1, 9.2, 9.2.1, 9.2.2, 9.2.3, 9.2.5, 9.2.6, 9.2.7)

Normal Distribution: Limiting form of binomial distribution – Characteristics – Mode – Median – Moment Generating function – Cumulant Generating Function – Moments of Normal distribution

### **Unit – II:** (Chapter 9 – 9.3, 9.3.1, 9.3.2, 9.3.3, 9.3.4, 9.4, 9.5, 9.5.1, 9.5.2, 9.5.3)

Special Continuous Probability Distributions: Rectangular Distribution - Triangular distribution – Gamma Distribution – simple problems.

### **Unit III:** (Chapter 10 – 10.1, 10.2, 10.3, 10.4, 10.5, 10.6, 10.7)

Correlation: Meaning of correlation – scatter diagram – Karl pearson's coefficient of correlation – Calculation of the correlation coefficient for a bivariate frequency distribution – Probable error of correlation coefficient – Rank correlation – Simple problems.

### **Unit IV:** (Chapter 11 – 11.4)

Linear and Curvilinear Regression : Linear regression – Curvilinear regression - Regression curves – simple problems

### **Unit V:** (Chapter 13 – 13.13.7)

Theory of Attributes: Notations – Dichotomy – Classes and Class frequencies – Consistency of data – Independence of attributes – Association of attributes - Simple problems.

**Text Book:** S.C. Gupta & V.K. Kapoor , Fundamentals of Mathematical Statistics- Sultan Chand and Sons,11th Edition ,2014

### **Reference Books:**

1. S.P. Gupta, Statistical methods- Sultan Chand and Sons, 45th Edition 2017
2. R.S.N.Pillai & V. Bagavathi, Statistics –S.Chand & company LTD, Reprint 2014

## **MINOR -3: STATISTICS-III – 4 CREDITS (60 HOURS)**

### **Course Objectives**

- To introduce the concepts of sampling distribution and estimation.
- To develop an understanding of the different types of sampling methods and their errors.
- To learn how to construct and interpret confidence intervals for population means and proportions.
- To learn how to test hypotheses about population means and proportions using large and small sample theory.
- To introduce the concepts of experimental design and its applications.

### **Unit I:** (Chapter 2 – 2.1, 2.2, 2.3, 2.4, 2.5, 2.6, 2.7, 2.8)

Sampling Distribution and Estimation: Introduction – types of sampling methods – sampling and non sampling errors – sampling distribution of mean , difference between two means, proportion, difference between two proportions – Central limit theorem – simple problems

### **Unit II:** (Chapter 2 – 2.9, 2.10, 2.11, 2.12, 2.13, 2.14, 2.16)

Sampling Distribution and Estimation: Estimation – confidence interval for the population mean for large samples (when  $\sigma$  is known) , for small samples (when  $\sigma$  is unknown) – for the difference between two population means for large samples (when  $\sigma$  is known) , for the difference between two population means for small samples (when  $\sigma$  is unknown) – confidence interval for the difference between two population proportions for large samples – determining the sample size(using confidence interval)

### **Unit III:** (Chapter 3 – 3.1, 3.2, 3.3, 3.4, 3.5, 3.6)

Tests of Hypothesis: test of significance for large sampling theory – Testing of hypothesis about a population proportion – about the difference between two proportions – about population mean – about difference between two means – difference between two standard deviations

### **Unit IV:** (Chapter 3 – 3.7, 3.8, 3.9, 3.10, 3.11)

Tests of Hypothesis: Test of significance for small sampling theory – about the mean population – about the difference between two means(Using t – test) – Paired t – test for difference of means – testing of hypothesis for equality of two variances

### **Unit V:** (Chapter 3 – 3.12, 3.13, 3.14, 3.15, 3.16, 3.17, 3.18, 3.19)

Tests of Hypothesis: Chi- square distribution -  $\chi^2$  Test of Goodness of Fit -  $\chi^2$  test of independence of attributes -  $\chi^2$  test for population variance – designs of experiments – Completely Randomized (CRD) or One-way Classification – Randomised block design (RBD) or Two way classification – Latin square design (LSD)

**Text Book:** K. Subramani & A. Santha, Statistics for Management, Second Edition 2011

### **Reference Books:**

1. S.C. Gupta & V.K. Kapoor , Fundamentals of Mathematical Statistics- Sultan Chand and Sons,11th Edition ,2014
2. R.S.N.Pillai & V. Bagavathi, Statistics –S.Chand & company LTD, Reprint 201

## **MINOR -4 : STATISTICS-IV – 4 CREDITS (60 HOURS)**

### **Course Objectives**

- To introduce the F-test and its applications.
- To develop an understanding of the Analysis of Variance (ANOVA) technique and its applications.
- To introduce the concepts of statistical quality control and total quality management.
- To develop an understanding of the methods of measuring fertility and mortality, and to learn how to construct life tables.
- To introduce the concepts of time series analysis and index numbers, and to learn how to construct and interpret these measures.

### **Unit I: (Chapter 5)**

F – Test and Analysis of variance: The F- test or the Variance ratio test – Applications of F-test – Analysis of Variance(ANOVA) – Assumptions in ANOVA – Technique of ANOVA – ANOVA in Two – way classification model

### **Unit II: (Chapter 7)**

Statistical Quality Control: Control charts - X chart – R chart – Control chart for C – Control chart for P – Advantages and limitations of Statistical quality control – Total quality management – Acceptance sampling

### **Unit III: (Chapter 16)**

Vital Statistics: Introduction – Uses – Methods – Measurement of Fertility – Reproduction rates – Measurement of Mortality – Life tables

### **Unit IV: (Chapter 5 – 5.2, 5.3, 5.4, 5.5, 5.6)**

Time Series Analysis: Time Series analysis – Secular Trend – Measurement of Seasonal variations – Cyclical variations – irregular variations

### **Unit V: (Chapter 5 – 5.7, 5.8, 5.9, 5.10)**

Index Numbers: Characteristics – Uses – Methods of Constructing index numbers – Tests of consistency and adequacy – Cost of living index

### **Text book:**

1. Dr. S.P. Gupta, Statistical methods, Sultan Chand & Sons, 46<sup>th</sup> Edition, 2021 (Unit I, II, III)
2. K. Subramani & A. Santha, Statistics for Management, Second Edition 2011. (Unit IV, V)

### **Reference Books:**

1. S.C. Gupta & V.K. Kapoor , Fundamentals of Mathematical Statistics- Sultan Chand and Sons,11th Edition ,2014
2. R.S.N.Pillai & V. Bagavathi, Statistics –S.Chand & company LTD, Reprint 2014

## **MINOR – 5 : OPERATIONS RESEARCH – I – 4 CREDITS (60 HOURS)**

### **Objectives:**

1. To introduce the field of operations research, which has many applications in management techniques.
2. To help students find the optimum solution to business and management problems.

### **Unit I:**

Operations Research –An overview: Introduction – Origin and development of O.R. – Nature and features of O.R. – Applications of Operations Research - Linear programming problem: Mathematical formulation - production allocation problem, product mix problem, product allocation problem only- Graphical solution method - General LPP - Canonical and Standard forms only.

### **Unit II:**

Linear programming problem- Simplex Method : Introduction – The computational procedure –The Simplex Algorithm – Use of Artificial variables -Two Phase method – Big- M method.

### **Unit III:**

Transportation problem: Definition- Formulation and solution of transportation problem - Initial Basic Feasible solution - Test for optimality - degeneracy in transportation problem - Modi method.

### **Unit IV:**

Assignment problem: Introduction - Mathematical formulation of the problem – solution methods of Assignment problems - Special cases in Assignment problems: Maximization case only.

### **Unit V:**

Network Scheduling by PERT/ CPM:- Introduction - Network and basic components - logical sequences - Rules of Network constructions - Concurrent Activities - Critical path Analysis.

**Text Book:**“ Operations Research” by Kanti Swarup, P.K.Gupta and Man Mohan, Sultan Chand & Sons Educational Publishers, New Delhi, 16th Edition 2014.

**Reference Book:** 1. Hamdy A., Taha, Operations Research, Pearson publisher, 9th Edition,2012

## **MINOR -6 : OPERATIONS RESEARCH – II – 4 CREDITS (60 HOURS)**

### **Objectives:**

1. To introduce the various techniques of Operations Research. 2. To make students solve real time problems in Business and management.

### **UNIT – I :**

Sequencing Problem: Introduction –Problem of sequencing – Basic terms used in sequencing –Processing n jobs through two machines –Processing n jobs through k machines.

### **UNIT – II :**

Games and Strategies : Two person zero sum games - Some basic terms - the maximin - minimax principle - Games without saddle points - Mixed strategies - graphic solution of  $2 \times n$  and  $m \times 2$  games – Dominance property .

### **UNIT- III :**

Replacement Problems : Introduction – Replacement policy when value of money does not change with time – Replacement policy when value of money changes with time – Replacement of equipment that fails suddenly - Group replacement policy .

### **UNIT IV :**

Inventory Control : Costs associated with inventories – Factors affecting inventory control - An inventory control problem – The concept of EOQ – Deterministic inventory with no shortages – Deterministic inventory problem with shortages – problems of EOQ with price breaks.

### **UNIT V :**

Queueing Theory – Elements of a queueing system – Classification of queueing models – Definition of transient and steady states – Poisson Queueing Systems – Model I{ (M/M/1):(∞/FIFO)} – Model III {(M/M/1) : (N/FIFO)} – Model V {(M/M/C):(∞/FIFO)}.

### **Text Books:**

1. Kanti Swarup, P.K. Gupta and Man Mohan, Operations Research, 16th edition, Sultan Chand and Sons, Reprint 2014.

Unit I : Chapter 12- sec 12.1 to 12.5 pp.327 – 338

Unit II : Chapter 17- sec 17.1 to 17.7 pp.443 – 464

Unit III : Chapter 18 – sec 18:1, 18:2.1,18:2.2,18:3 pp.478 – 492

Unit IV : Chapter 19 – sec 19.6 to 19.12 pp. 510 – 538

Unit V : Chapter 21 – sec 21:3, 21:7, 21:8, 21:9, pp.589,590,596 to 604, 608 to 610, 613to 618

### **Reference Books**

1. Resource Management Techniques(Operations Research) by V. Sundaresan, K. S. Ganapathy Subramanian, K. Ganesan – A. R. Publications
2. Operations Research: An Introduction, 9th edition, Hamdy A.Taha, Pearson, 2010

## **MINOR-7 CALCULUS OF VARIATIONS -(4 CREDITS-60 HOURS )**

### **Course Objectives**

1. To learn about functionals and solving related variational problems by Euler's equation
2. To understand and solve the variational problems involving functionals depending on higher order derivatives

<b>Course Outcome</b>	
<b>CO 1</b>	To study about the general variational of a functional and the Weierstrass Erdmann conditions
<b>CO 2</b>	To study and understand about canonical form of Euler equations and other transformations, Noether's Theorem, and conservation laws
<b>CO 3</b>	To learn about the second variation and Legendre conditions of a functional

### **Unit I:**

Functionals- some simple variational The variation of a functional- A necessary condition for an extremum- The simplest variational problem-Euler's. The case of several variables, simple variable end point problem- The variational derivative- Invariance of Euler's equation.[Chapter-1]

### **Unit II:**

The fixed end point problem for  $n$ -unknown functions - Variational problem in parametric form- Functionals depending on higher order derivatives- Variational problems with subsidiary conditions. [Chapter-2]

### **Unit III:**

The general variational of a functional- derivation of the basic formula- End points lying on two given curves or surfaces- Broken extremals- The Weierstrass-Erdmann conditions. [Chapter-3]

### **Unit IV:**

The canonical form of Euler equations- First integrals of the Euler equations- The Legendre transformation- Canonical transformations- Noether's Theorem- The principle of least action- Conservation laws- The Hamilton-Jacobi equation- Jacobi theorem.[Chapter-4]

### **Unit V:**

The second variation of a functional- The formula for the second variation, Legendre conditions- Sufficient conditions for a weak extremum. [Chapter-5]

### **Textbook:**

I.M. Gelfand and S.V. Fomin, Calculus of Variations, Dover Publications, 2000.

### **Reference Books:**

1. A.S. Gupta, Calculus of Variations with Applications, Prentice-Hall of India, 2008.
2. M.L. Krasnov, G.I. Makarenko and A.I. Kiselev, Problems and Exercises in the Calculus of Variations, Mir Publishers, Moscow 1975.



## **MINOR STREAM II**

### **MINOR -1: MATHEMATICS OF FINANCE – 4 CREDITS (60 HOURS)**

#### **UNIT I :**

Ratio, Proportion, and Percentage: Ratio: Definition – Continued Ratio – inverse Ratio. Proportion – Continued Proportion – Direct Proportion – Inverse Proportion – Variation – Inverse Variation – Joint Variation – Percentage: Meaning and computation of percentage. Interest: Simple interest – compound interest (reducing balance and flat interest rate) – equated monthly instalments (EMI) – Problems.

#### **UNIT II :**

Matrices and Determinates (up-to order 3 only): Multivariable data - Definition of a Matrix; Types of matrices; Algebra of matrices; Determinates – Ad-joint of a matrix – Inverse of a matrix via ad-joint matrix – homogeneous system – Solution of non- homogeneous system of linear equations (not more than three variables) – Conditions for existence and uniqueness of solution – Solution using inverse of the coefficient matrix – Problems.

#### **UNIT III :**

Functions: (To identify and define the relationships that exist among the business variables) Definition of function, constants, variables, continuous real variable, domain or interval – Types of functions – one valued function – Explicit function – Algebraic functions – Polynomial functions – Absolute value function – Inverse function – Rational and irrational function – Monotone function – Even and odd function – Supply/demand function – Cost function – Total revenue function – Profit function – Production function – Utility function – Consumption function.

**(Problems: 80%, Theory: 20%)**

#### **Text Books**

1. Kappor, V.K., Business Mathematics, Sultan Chand & Sons, New Delhi

#### **Books for References:**

1. Agarwal, B.M., Basic Mathematics & Statistics, Sultan Chand & Sons, New Delhi
2. Rajagopalan, S. & Sattanathan., R., Business mathematics, McGraw-Hill, New Delhi
3. Bari, Business Mathematics, New Literature Publishing Company, Mumbai.
4. Bhardwaj, R. S. (2019). Business Mathematics and Statistics. New Delhi: Scholar Tech Press.
5. Richard, I. L., Masood, H. S., David, S. R., & Rastogi, S. (2017). Statistics for Management. New Jersey: Pearson Education.
6. Thukral, J. K. (2017). Business Mathematics and Statistics. New Delhi: Maximax Publications.
7. Vohra, N. D. (2014). Business Mathematics and Statistics. New Delhi: Tata McGraw Hill Education India.

## **MINOR – 2: BUSINESS STATISTICS– 4 CREDITS (60 HOURS)**

### **UNIT I:**

Statistics-Definition-Functions, Scope and Limitations of statistics - Statistical Enquiry Stages in conducting a statistical survey-Primary data Vs secondary data-Sources of secondary data - Classification, Tabulation and Presentation of data- Diagrams.

### **UNIT II:**

#### Univariate Analysis

- (a) Measures of Central Tendency – Average – Meaning - Characteristics of a typical average - Computation of Mean, Median, Mode, Geometric Mean, Harmonic Mean, and Weighted Arithmetic Mean- Merits and Limitations of each.
- (b) Measures of Dispersion: Dispersion - Meaning - Properties of a good measure of dispersion - Absolute versus relative measure of dispersion - Computation of Range, Quartile Deviation, Mean Deviation, Standard Deviation, and Coefficient of Variation- Merits and Limitations of each.
- (c) Skewness – Meaning - Variation versus Skewness - Measures of Skewness- Karl and Co-efficient of Skewness.

### **UNIT III:**

#### Bi-variate Analysis

- (a) Simple and Linear Correlation Analysis: Meaning – Definition - Types of Correlation Methods of Studying Correlation - Correlation) and Properties.
- (b) Simple and Linear Regression Analysis: Definition - Correlation, Regression, Regression lines, and Regression Equations. Regression coefficient- Computation of correlation coefficient from regression co-coefficient.

### **UNIT IV:**

Index Numbers: Definition - Characteristics of Index numbers – Uses - Types of index numbers - Construction of Price Index numbers - Unweighted Index numbers -Weighted Index numbers - Tests of adequacy of Index number - formulae. Chain - basis index number base shifting, splicing, and deflating problems in constructing index numbers; Consumer price index.

### **UNIT V:**

Analysis of Time Series: Introduction Uses - Components of time series - Measurement of trend- graphical method, semi-average method, moving average and method of least square (including linear, second degree, Parabolic and exponential trend) - Computational of seasonal, indices by simple average, Ratio - trend, ratio - to - moving average and link relative methods.

#### **Text Books**

1. J. K. Sharma, Business Statistics, Vikas Publishing House (P), Ltd., New Delhi.
2. R.S.N. Pillai and Bagavathi, Business Statistics, S. Chand & Co., New Delhi.

#### **Books for References**

1. S.P. Gupta & M.P Gupta, Statistical Methods, Sultan Chand & Co, New Delhi
2. K. Alagar, Business Statistics, Tata McGraw Hill Publications, New Delhi
3. Arora & Arora., Statistics for Management, S.Chand & Co, New Delhi

## **MINOR -3 : NUMERICAL ANALYSIS – 4 CREDITS (60 HOURS)**

### **UNIT I:**

Numerical solution of algebraic and transcendental equations – Bolzano's bisection method - Successive approximation method – Regula falsi method – Newton-Raphson method.

### **UNIT II:**

Numerical solution of simultaneous linear algebraic equations – Gauss elimination method - Gauss Jordan elimination method – Gauss Seidel iteration method.

### **UNIT III:**

Finite difference operator - Interpolation – Newton-Gregory forward and backward interpolation – Newton's divided difference formula – Lagrange's interpolation formula for uneven intervals – Gauss interpolation formula – Numerical differentiation – Numerical Integration – Trapezoidal rule – Simpson's 1/3rd rule.

### **UNIT IV:**

Numerical solutions of Ordinary differential equations of first and second order – Simultaneous equations – Taylor series method – Picard's method.

### **UNIT V:**

Euler's method – Improved Euler's Method - Modified Euler's Method – Runge-Kutta method of second and fourth order – Milne's predictor corrector method.

#### **Text book**

Numerical Methods in Science and Engineering,  
M.K.Venkataraman,NationalPublicationCo,Chennai(2001)  
Unit1: Chapter 3 and 4  
Unit2: Chapter 5  
Unit3: Chapter 6 and 9  
Unit4:Chapter11(Relevantportions)Unit5:Chapter11(Relevantportions)

#### **Reference Books**

Computer-Oriented Numerical Methods by V. Rajaram–PHI(P)Ltd. e-LearningSource

## **MINOR -4: OPTIMIZATION TECHNIQUES – I – 4 CREDITS (60 HOURS)**

### **Objectives:**

1. To introduce the field of operations research, which has many applications in management techniques.
2. To help students find the optimum solution to business and management problems.

### **Unit I:**

Operations Research –An overview: Introduction – Origin and development of O.R. – Nature and features of O.R. – Applications of Operations Research - Linear programming problem: Mathematical formulation - production allocation problem, product mix problem, product allocation problem only- Graphical solution method - General LPP - Canonical and Standard forms only.

### **Unit II:**

Linear programming problem- Simplex Method: Introduction – The computational procedure –The Simplex Algorithm – Use of Artificial variables -Two Phase method – Big- M method.

**Unit III:** Transportation problem: Definition- Formulation and solution of transportation problem - Initial Basic Feasible solution - Test for optimality - degeneracy in transportation problem - Modi method.

**Unit IV:** Assignment problem: Introduction - Mathematical formulation of the problem – solution methods of Assignment problems - Special cases in Assignment problems: Maximization case only.

### **Unit V:**

Network Scheduling by PERT/ CPM:- Introduction - Network and basic components - logical sequences - Rules of Network constructions - Concurrent Activities - Critical path Analysis.

**Text Book:** “Operations Research” by Kanti Swarup, P.K.Gupta and Man Mohan, Sultan Chand & Sons Educational Publishers, New Delhi, 16th Edition 2014.

1. Unit I : Chapter 1, 2 & 3 Sections 1.1 to 1.3, 1.10, 2.1 to 2.4, 3.2 to 3.5
2. Unit II : Chapter 4 Sections 4.1, 4.3, 4.4
3. Unit III : Chapter 10 Sections 10.1, 10.2, 10.5, 10.8, 10.9, 10.10, 10.12, 10.13
4. Unit IV : Chapter 11 Sections 11.1 to 11.4
5. Unit V : Chapter 25 Sections 25.1 to 25.6

### **Reference Book:**

1. Hamdy A., Taha, Operations Research, Pearson publisher, 9 th Edition,2012

## **MINOR -5: OPTIMIZATION TECHNIQUES – II – 4 CREDITS (60 HOURS)**

### **Objectives:**

1. To introduce the various techniques of Operations Research.
2. To make students solve real-time problems in Business and management.

### **UNIT – I :**

Sequencing Problem: Introduction –Problem of sequencing – Basic terms used in sequencing –Processing n jobs through two machines –Processing n jobs through k machines.

### **UNIT – II :**

Games and Strategies : Two-person zero-sum games - Some basic terms - the maximin - minimax principle - Games without saddle points - Mixed strategies - graphic solution of  $2 \times n$  and  $m \times 2$  games – Dominance property

### **UNIT- III :**

Replacement Problems: Introduction – Replacement policy when value of money does not change with time – Replacement policy when value of money changes with time – Replacement of equipment that fails suddenly - Group replacement policy.

### **UNIT IV :**

Inventory Control: Costs associated with inventories – Factors affecting inventory control - An inventory control problem – The concept of EOQ – Deterministic inventory with no shortages – Deterministic inventory problem with shortages – problems of EOQ with price breaks.

### **UNIT V :**

Queueing Theory – Elements of a queueing system – Classification of queueing models – Definition of transient and steady states – Poisson Queueing Systems – Model I {  $(M/M/1);(\infty/FIFO)$  } – Model III { $(M/M/1) : (N/FIFO)$ } – Model V { $(M/M/C);(\infty/FIFO)$ }.

### **Text Books:**

1. Kanti Swarup, P.K. Gupta and Man Mohan, Operations Research, 16th edition, Sultan Chand and Sons, Reprint 2014.  
Unit I : Chapter 12- sec 12.1 to 12.5 pp.327 – 338  
Unit II : Chapter 17- sec 17.1 to 17.7 pp.443 – 464  
Unit III : Chapter 18 – sec 18:1, 18:2.1,18:2.2,18:3 pp.478 – 492  
Unit IV : Chapter 19 – sec 19.6 to 19.12 pp. 510 – 538  
Unit V : Chapter 21 – sec 21:3, 21:7, 21:8, 21:9, pp.589,590,596 to 604, 608 to 610, 613to 618

### **Reference Books**

1. Resource Management Techniques(Operations Research) by V. Sundaresan, K. S. Ganapathy Subramanian, K. Ganesan – A. R. Publications
2. Operations Research: An Introduction, 9th edition, Hamdy A.Taha, Pearson, 2010

## **MINOR – 6 : APPLIED STATISTICS– 4 CREDITS (60 HOURS)**

### **Objectives:**

1. To learn the basics of statistics concepts
2. To learn how to solve correlation and regression problems
3. Ability to understand and represent data
4. Ability to analyse and interpret data.

### **UNIT I:**

Diagrammatic and Graphic Presentation: General Rules for Constructing Diagrams, Types of Diagrams, One-Dimensional or Bar Diagrams, Types of Bar Diagrams, Two-Dimensional Diagrams, Limitations of Pie Diagrams.

### **UNIT II:**

Measures of Central Value: Arithmetic Mean: Calculation of Simple Arithmetic Mean, Individual Observations, Calculation of Arithmetic Mean- Discrete Series, Calculation of Arithmetic Mean- Continuous Series, Merits and Limitations of Arithmetic Mean. Median: Calculation of Median-Individual Observations, Computation of Median-Discrete Series, Calculation of Median-Continuous Series, Merits and Limitations of Median Mode: Calculation of Mode-Individual Observations, Calculation of Mode-Discrete Series, Calculation of Mode-Continuous Series, Merits and Limitations of Mode.

### **UNIT III :**

Measures of Dispersion: Significance of Measuring Variation, Properties of a Good Measure of Variation, The Interquartile Range or the Quartile Deviation, Merits and Limitations, The Mean Deviation, Calculation of Mean Deviation, Calculation of Mean Deviation – Continuous Series, Merits and Limitations, The Standard Deviation, Difference Between Mean Deviation and Standard Deviation, Calculation of Standard Deviation, Merits and Limitations.

### **UNIT IV :**

Correlation Analysis: Types of Correlation, Scatter Diagram Method, Merits and Limitations of the Method, Karl Pearson's Coefficient of Correlation, Direct Method of Finding Out Correlation Coefficient, Origin is made and Problems, Rank Correlation Coefficient, Merits and Limitations of the Rank Method.

### **UNIT V :**

Regression Analysis: Uses of Regression Analysis, Difference Between Correlation and Regression Analysis, Regression Lines, Regression Equations, Regression Equation of Y on X, Regression Equation of X on Y and Problems

### **TEXTBOOK**

S.P.GUPTA, "Statistical Methods", Sultan Chand & Sons, Educational Publishers ,New Delhi,2016

### **REFERENCE BOOK:**

P.R. Vittal, "Mathematical Statistics", Margham Publications, 2016

## **MINOR STREAM – III**

### **MINOR -1 : MATRICES AND TRIGONOMETRY – 4 CREDITS (60 HOURS)**

#### **Unit 1:**

Matrices – rank of Matrices – Consistency of a system of linear non –non-homogeneous equations (statement only) – simple problems

#### **Unit 2:**

Characteristic roots of a square matrix – Evaluation of eigenvalues and Eigen vectors of a square matrix – Cayley Hamilton theorem (statement only) – simple problems – Orthogonal transformation of a symmetric matrix to diagonal form

#### **Unit 3:**

De Moivre's theorem and its applications – Direct and Inverse circular and hyperbolic functions.

#### **Unit 4:**

Logarithm of a complex quantity- Expansion of Trigonometrical functions

#### **Unit 5:**

Gregory's series- Summation of series.

#### **Text book:**

1. Dr. P.R. Vittal, Allied Mathematics, Margham Publications, 2018
2. Trigonometry, S. Narayanan and T.K. Manicavachagom Pillai, S. Viswanathan (Printers & Publishers) Pvt. Ltd, (1997)

## **MINOR -2: CALCULUS – 4 CREDITS (60 HOURS)**

### **UNIT I :**

$n^{\text{th}}$  derivative – Standard results – Trigonometrical transformation – Formation of equations involving derivatives – Leibnitz formula

### **UNIT II :**

Total differential coefficients – Euler's theorem – Partial derivatives of a function of two functions - Maxima and Minima of two variables – Lagrange's method of undetermined multipliers

### **UNIT- III :**

Circle, radius and centre of curvature – Cartesian formula for radius of curvature – envelope

### **UNIT- IV:**

Integration of rational algebraic functions – Integration of irrational algebraic functions - Properties of definite integrals

### **UNIT- V:**

Integration by parts – reduction formula, Bernoulli's formula - Evaluation of double integral (Cartesian form only) – Triple integral (Cartesian form only)

### **Textbook**

Calculus Volume — I, T. K. Manickavachagom Pillai, Printers and Publishers (May1992 Edition)

Unit 1: Chapter 3 – 1.1, 1.2, 1.3, 1.4, 1.5, 1.6, 2.1,

Unit 2: Chapter 8-1.3, 1.4, 1.5, 1.6, 1.7, 4, 4.1, 5,

Unit 3: Chapter 10 – 1.1, 1.2, 2.1, 2.2, 2.3, 2.4, 2.5

Calculus Volume II , S.Narayanan and T.K. Manickavasagam Pillai (2008)

Unit 4 : Chapter 1 : 7.3, 7.4, 7.5, 8, 11

Unit 5 : Chapter 1: 12,13,14, 15.1, and Chapter 5: 2, 4,

### **Reference books**

1. Integral Calculus, N. P. Bali, Laxmi Publications, Delhi, (1991)

2. 2. Calculus(2nd Edition), Lipman Bers and Frank Karal, Holt McDougal, 1976.

3. Thomas' Calculus 12th Edition, George B.Thomas, Maurice D.Weir and Joel Hass, Pearson Education, 2015.

## **MINOR -3 : VECTOR CALCULUS – 4 CREDITS (60 HOURS)**

### **Objective:**

To attain the basic knowledge on vector calculus.

### **UNIT I :**

Vector differentiation – Differentiation of vectors – Meaning of the derivative of position vector - Physical applications -- Vector differential operator - Gradient - Direction and magnitude of gradient – Simple problems.

### **UNIT II :**

Divergence and curl - Formula involving operator, operators involving twice – Simple problems.

### **UNIT III:**

Vector integration - Line integral – Surface integral – Volume integral – Simple problems.

### **UNIT IV :**

Gauss divergence theorem – Green's theorem (in space) (Statement only) – Simple problems using theorems.

### **UNIT V :**

Stoke's theorem - Green's theorem (in plane) (Statement only) – Simple problems using theorems. #

### **Text Book:**

S. Narayanan and T.K. Manicavachagom Pillai, Vector Algebra and Analysis, S.Viswanathan Pvt. Ltd. (1995).

UNIT I Chapter 4 Sections 1 - 8

UNIT II Chapter 4 Sections 9 - 12

UNIT III Chapter 6 Sections 1 - 5

UNIT IV Chapter 6 Sections 6 - 8

UNIT V Chapter 6 Sections 9, 10

### **Books for Reference:**

1. M.L. Khanna, Vector Calculus, Jai Prakash Nath and Co., Eighth Edition (1986).

2. P.R. Vittal, Vector analysis, Analytical Geometry & sequences and series, Margham Publications, Chennai (2004).

## **MINOR -4 : INTRODUCTION TO DIFFERENTIAL EQUATIONS – 4 CREDITS (60 HOURS)**

Ordinary differential equations

### **Unit 1:**

Ordinary differential equations – linear equations and equations reducible to the linear form - Exact differential equations – Equations of the First, but of higher degree – Equations solvable for  $dy/dx$ , solvable for  $y$ , solvable for  $x$ , Clairaut's form and singular solutions – geometrical meaning of a differential equations – orthogonal trajectories.

### **Unit 2:**

Linear Differential equations with constant coefficients – Homogenous linear ordinary differential equation – linear differential simultaneous differential equations.

Partial differential equations

### **Unit 3:**

Formation of Partial differential equations – by elimination of arbitrary constants – by elimination of arbitrary functions – Defines of general, particular and complete solutions - Singular integral – Lagranges method of solving the linear equation  $Pp+Qq=R$

### **Unit 4 :**

Charpits method - Linear Partial Differential equation of second and higher order with constant coefficients.

### **Unit 5 :**

Boundary value problems method of separation of variable transverse vibrations of string – the one dimensional heat flow equations a Cartesian form.

#### **Text books**

1. T.K. Manicavachagom Pillay , Calculus , Volume – I, S. Viswanathan (Printers and Publishers) Pvt Ltd. (2004)
2. Dr. M.B.K. Moorthy & K. Senthilvadivu, Transforms and partial differential equations VRB Publishers, (2009).
3. Transforms and Partial differential equations by Dr. A. Singaravelu

#### **Reference Books**

1. Introductory course in Differential equations , D.A.Murray, Orient Longman (1967)
2. Engineering Mathematics , M.K.Venkataraman, National Publications , Chennai (2009) e-

## **MINOR -5 : FOURIER SERIES AND LAPLACE TRANSFORMS – 4 CREDITS (60 HOURS)**

### **UNIT 1:**

Dirichlet's condition general Fourier series Odd and Even Functions half range Sine series and Half range cosine series.

### **UNIT 2:**

Complex form of Fourier series Parseval's Identity.

### **UNIT 3:**

Transform of the equation by changing the dependent variables / the independent variables – Method of variations of parameters – ordinary simultaneous differential equations.

### **UNIT 4:**

Definition transform of 1 – transform of the function  $e$  ,  $\cos at$  ,  $\sin bt$  ,  $t$  , where n is a positive integer,  $\sinh at$  ,  $\cosh at$  - first shifting theorem – if the Laplace transform of a function  $f(t)$  is  $\Phi(s)$ , then the Laplace transform of  $e f(t)$  is  $\Phi(s + a)$  - Laplace transform of  $e \cos bt$  ,  $e \sin bt$  ,  $e t$  - Second shifting theorem – Transform of  $f(t)$  and  $f'(t)$  – inverse transform relating to the above standard forms.

### **UNIT 5:**

Application to solution of ordinary differential equation with constant coefficients – involving the above transforms.

### **Text books**

1. Dr. M.B.K. Moorthy & K. Senthil vadiu, Transforms and partial differential equations VRB Publishers (2009).
2. T.K. Manicavachagom Pillay , Calculus , Volume – I, S. Viswanathan (Printers and Publishers) Pvt Ltd. (2004)

### **Reference Books**

1. Introductory course in Differential equations , D.A.Murray, Orient Longman (1967)
2. Engineering Mathematics , M.K.Venkataraman, National Publications , Chennai (2009)

## **MINOR -6: NUMERICAL ANALYSIS – 4 CREDITS (60 HOURS)**

### **UNIT I:**

Numerical solution of algebraic and transcendental equations – Bolzano's bisection method - Successive approximation method – Regula falsi method – Newton-Raphson method.

### **UNIT II:**

Numerical solution of simultaneous linear algebraic equations – Gauss elimination method - Gauss Jordan elimination method – Gauss Seidel iteration method.

### **UNIT III:**

Finite difference operator - Interpolation – Newton-Gregory forward and backward interpolation – Newton's divided difference formula – Lagrange's interpolation formula for uneven intervals – Gauss interpolation formula – Numerical differentiation – Numerical Integration – Trapezoidal rule – Simpson's 1/3rd rule.

### **UNIT IV:**

Numerical solutions of Ordinary differential equations of first and second order – Simultaneous equations – Taylor series method – Picard's method.

### **UNIT V:**

Euler's method – Improved Euler's Method - Modified Euler's Method – Runge-Kutta method of second and fourth order – Milne's predictor corrector method.

### **Text book**

Numerical Method in Science and Engineering, M.K. Venkataraman, National Publication Co, Chennai(2001)

Unit1: Chapter 3 and 4

Unit2: Chapter 5

Unit3: Chapter 6 and 9

Unit4:Chapter11(Relevantportions)Unit5:Chapter11(Relevantportions)

### **Reference Books**

Computer oriented Numerical Methods by V.Rajaram–PHI(P)Ltd. e-Learning Source

## SKILL ENHANCEMENT COURSES

Title of the course		QUANTITATIVE APTITUDE (Practical)			Nature of the Course	SEC 1									
Credits	3	Semester	1	Type of course	Practical	No. of Hours of Teaching	45								
Internal Assessment Marks (IA)			50	End Semester Examination (ESA)		50	Duration of ESA 3 hrs								
Course Prerequisites if any		Students are expected to have basic knowledge of arithmetic operations, number systems, and an elementary understanding of algebraic expressions.													
<b>Course Outcomes</b>															
CO1	Understand the structure and properties of the number system and apply concepts of HCF, LCM, and decimal operations.														
CO2	Perform basic mathematical operations efficiently using simplification, root extraction, and average-related techniques.														
CO3	Solve real-life numerical problems involving age, numbers, and surds & indices with logical reasoning.														
CO4	Apply advanced arithmetic concepts like logarithms, percentage, and profit-loss to quantitative problems.														
CO5	Integrate multiple arithmetic concepts to solve problems on ratio, proportion, partnership, and chain rule.														
Unit No	<b>Course Content</b>						No. of Hours								
<b>Theory Component (30 Hours)</b>															
1	Fundamentals of Arithmetic: This unit focuses on the foundational principles of arithmetic, covering the Number System, including various types of numbers, their properties, and operations. It also explores the computation of the Highest Common Factor (H.C.F.) and the Least Common Multiple (L.C.M.) of numbers, along with Decimal Fractions.						5								
2	Basic Mathematical Operations: Unit 2 is dedicated to essential mathematical operations, including Simplification techniques, efficient methods for calculating Square Roots and Cube Roots, and a comprehensive understanding of Averages						5								
3	Problem Solving: Unit 3 enhances problem-solving skills by addressing a wide range of numerical problems, including Problems on Numbers, Problems on Ages, and Surds and Indices.						5								
4	Advanced Arithmetic: Unit 4 introduces more advanced arithmetic concepts, such as Logarithms, Percentage calculations, and the principles of Profit and Loss.						5								

<b>5</b>	Review and Application: Unit 5, provides an opportunity to review and apply the knowledge gained in previous units. It covers Ratio and Proportion, Partnership, and the Chain Rule for interconnected problem-solving.	<b>5</b>
<b>Exercise No</b>	<b>Practical Component - Internal Assessment marks (IA)-50</b>	<b>No. of Hours</b>
<b>1</b>	Exercise on Number System, HCF & LCM: Solve 10 problems involving classification of numbers (natural, whole, rational, etc.), and compute HCF and LCM for number pairs with proper steps.	
<b>2</b>	Simplification & Average Computation: Perform 10 simplification exercises (using BODMAS) and compute averages from given data sets (marks, temperatures, distances, etc.).	
<b>3</b>	Problems on Ages and Surds: Solve 5 real-life word problems on ages and 5 simplification problems involving surds and indices. Include full solution steps.	
<b>4</b>	Logarithms and Profit-Loss Calculations: Solve 5 logarithmic expressions using laws of logarithms and 5 business transaction problems related to profit and loss calculations.	
<b>5</b>	Ratio, Proportion & Partnership Problems: Complete 3 problems on ratios, 3 on proportions, and 4 on partnership investment and profit-sharing problems. Show all steps and justification.	<b>20</b>
<b>6</b>	Mini Assignment / Test – Cumulative Problem Set: A mixed exercise sheet of 10 problems covering concepts from all 5 units. Students must write the problem, solve, and reflect on the approach taken.	
<b>Prescribed Text</b>		
<b>1</b>	Quantitative Aptitude by R.S. Agarwal	
<b>2</b>	Quantitative Aptitude by Abhijit Guha	

\*The Course Instructor can customize the practical exercises and the number of exercises in the Practical Component

Title of the course		LOGICAL REASONING (Practical)			Nature of the Course	SEC 2	
Credits	3	Semester	2	Type of course	Practical	No. of Hours of Teaching	45
<b>Internal Assessment Marks (IA)</b>			50	<b>End Semester Examination (ESA)</b>		50	<b>Duration of ESA</b>
<b>Course Prerequisites, if any</b>		Students should have basic numerical ability and logical reasoning skills. Familiarity with patterns, sequences, and simple arithmetic operations is recommended.					

### **Course Outcomes**

<b>CO1</b>	Analyse and complete various series patterns.
<b>CO2</b>	Apply analogical reasoning to identify and complete analogous pairs.
<b>CO3</b>	Classify objects and identify odd ones out based on given criteria.
<b>CO4</b>	Decode and encode messages using various coding techniques.
<b>CO5</b>	Solve puzzles and problems related to blood relations and directional sense.

Unit No	Course Content	No. of Hours
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### **Theory Component (30 Hours)**

1	Series Completion: This unit covers Number Series, Alphabet Series, and Alpha-Numeric Series. Students will learn to identify and complete various series patterns.	5
2	Analogy: Unit 2 explores Completing the Analogous Pair, Simple Analogy, Choosing the Analogous pair, Double Analogy, Word Analogy, and Number Analogy.	5
3	Classification / Odd One Out: This unit involves Word Classification, Number Classification, and Letter Classification, helping students identify patterns and outliers.	5
4	Coding – Decoding: Unit 4 introduces Letter Coding, Number Coding, Matrix Coding, Substitution, Deciphering Message Word Codes, and Jumbled Coding, enhancing code-based problem-solving skills.	5
5	Blood Relations: Unit 5 focuses on deciphering Jumbled up Descriptions and solving Relation Puzzles, including Direction Sense Tests.	5

<b>Exercise No</b>	<b>Practical Component - Internal Assessment marks (IA)-50</b>	<b>No. of Hours</b>
<b>1</b>	Solve 20 series completion problems (Number/Alphabet/Alpha-Numeric)	<b>20</b>
<b>2</b>	Complete 15 analogy patterns across 4 categories (Word/Number/Simple/Double)	
<b>3</b>	Classify 20 sets of objects/words/numbers and identify odd-one-out	
<b>4</b>	Decode 10 encrypted messages using 3 different coding techniques	
<b>5</b>	Solve 15 blood relation puzzles and 10 directional sense problems	
<b>6</b>	Conduct 5 number/ranking/time sequence tests with arithmetical validation	

**Prescribed Text**

<b>1</b>	"Verbal and Non-Verbal Reasoning" by R.S. Agarwal
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\*The Course Instructor can customize the practical exercises and the number of exercises in the Practical Component

Title of the course		LATEX (Practical)			Nature of the Course	SEC 3									
Credits	3	Semester	3	Type of course	Practical	No. of Hours of Teaching	45								
<b>Internal Assessment Marks (IA)</b>		50	<b>End Semester Examination (ESA)</b>		50	<b>Duration of ESA</b>	<b>3 hrs</b>								
<b>Course Prerequisites, if any</b>		<b>Nil</b>													
<b>Course Outcomes</b>															
<b>CO1</b>	Create basic LaTeX documents with appropriate formatting and structure as demonstrated in "Learning LaTeX."														
<b>CO2</b>	Proficiently typeset mathematical equations and expressions using LaTeX, following the examples and techniques presented in the book.														
<b>CO3</b>	Format and style LaTeX documents according to academic standards, drawing from the knowledge provided in "Learning LaTeX."														
<b>CO4</b>	Apply advanced LaTeX features, as covered in the book, to create complex mathematical documents and presentations.														
<b>CO5</b>	Use LaTeX for research, publications, and collaborative projects in mathematics, applying the principles and practices outlined in the book.														
Unit No	<b>Course Content</b>						<b>No. of Hours</b>								
<b>Theory Component (30 Hours)</b>															
1	Introduction to LaTeX: Motivation for Learning LaTeX, Running LaTeX, Resources for LaTeX						5								
2	Basic LaTeX: Sample Document and Key Concepts, Type Style in LaTeX, LaTeX Environments: Lists, Centering, Tables, Verbatim, Managing Vertical and Horizontal Spacing						5								
3	Typesetting Mathematics: Examples of Mathematical Typesetting, Equation Environments in LaTeX, Fonts, Hats, and Underlining in Mathematical Notation, Using Braces, Arrays, and Matrices, Creating Customized Commands, Theorem-like Environments in LaTeX, Miscellaneous Mathematical Notation and Styles						5								
4	Further Essential LaTeX: Document Classes and Document Structure, Titles for LaTeX Documents, Sectioning Commands, Miscellaneous Extras: Spacing, Accented Characters, Dashes, Hyphens, Quotation Marks, Troubleshooting LaTeX: Error Identification and Common Errors						5								
5	More About LaTeX: Introduction to LaTeX Packages, Inputting External Files, Inserting Pictures and Graphics, Creating Bibliographies, Generating an Index, Exploring the History of LaTeX, Exploring Online LaTeX Resources and Professional Societies.						5								

<b>Exercise No</b>	<b>Practical Component - Internal Assessment marks (IA)-50</b>	<b>No. of Hours</b>
1	<p>Introduction to LaTeX</p> <p>Task: Create a basic LaTeX document with a title, author, date, and a simple paragraph. Objective: Familiarize students with the LaTeX environment and basic commands</p>	
2	<p>Formatting Text</p> <p>Task: Create a document with different text styles (bold, italics, underline), lists (itemized, enumerated), and tables.</p> <p>Objective: Learn how to structure text and create lists and tables in LaTeX.</p>	
3	<p>Mathematical Typesetting</p> <p>Task: Typeset various mathematical expressions and equations using different equation environments.</p> <p>Objective: Gain proficiency in mathematical typesetting, including using subscripts, superscripts, and special characters.</p>	
4	<p>Advanced Mathematical Notation</p> <p>Task: Create a document with arrays, matrices, and customized commands for complex mathematical expressions.</p> <p>Objective: Understand advanced mathematical typesetting and customization of commands.</p>	
5	<p>Theorem-Like Environments</p> <p>Task: Create a document with theorem-like environments for definitions, theorems, proofs, and examples.</p> <p>Objective: Learn to structure mathematical documents with proper logical sections.</p>	20
6	<p>Document Structure and Sectioning</p> <p>Task: Create a well-structured document using different sectioning commands (e.g., sections, subsections, subsubsections) with a table of contents.</p> <p>Objective: Master the document structure and organization in LaTeX.</p>	
7	<p>Inserting Figures and Tables</p> <p>Task: Insert external images, create tables with captions, and adjust figure and table positions within the text.</p> <p>Objective: Learn how to include and format figures and tables within LaTeX documents.</p>	
8	<p>Bibliography Management</p> <p>Task: Create a bibliography section using BibTeX or LaTeX's built-in bibliography commands.</p> <p>Objective: Learn how to manage references and citations in academic documents.</p>	
9	Creating Presentations with Beamer	

	<p>Task: Create a simple presentation using the Beamer package, including slides with text, images, and bullet points.</p> <p>Objective: Introduce students to LaTeX-based presentations.</p>	
10	<p>Final Project</p> <p>Task: Create a comprehensive document or presentation incorporating all the learned skills, with a focus on research or academic content.</p> <p>Objective: Apply all the skills acquired throughout the course in a single cohesive project.</p>	

### **Prescribed Text**

**1** "Learning LaTeX" by David F. Griffiths and Desmond J. Higham

### **Books for Reference**

**2** The LaTeX Companion, 3rd edition (TTCT series) by Frank Mittelbach and Ulrike Fischer

\*The Course Instructor can customize the practical exercises and the number of exercises in the Practical Component

## **MULTIDISCIPLINARY COURSE(MLDC)**

## **Offered by the Department of Mathematics**

## Community Engagement

The Community Engagement Learning Project is a short course that offers students the chance to collaborate with a nonprofit or government organization through a group project chosen by the organization. Students will investigate the concept of community engagement, examine the role of the community sector in their local area, and analyze the operational context and tools the sector uses to deliver services, influence policies and programs, and share information with its clients. Additionally, the seminar program and hands-on collaboration with a local organization will enable students to develop a diverse range of skills.

## **Course Guidelines**

- The Community Engagement course is typically offered during the fourth semester.
  - The course is evaluated out of a maximum of 100 marks, with assessments based on a report, presentation, and viva voce.
  - Students may complete the course as a group, however, each team member must submit an individual report.
  - A faculty member, designated by the Head of the Department, will supervise the course.
  - An internal examiner will oversee the course evaluation.
  - The course is designed to encourage student interaction with the end users.
  - The chosen project should provide sufficient scope to apply and demonstrate the concepts learned during the course.
  - Internal marks (based on Internship report, work dairy, etc.): 50 marks.
  - External marks (based on presentation, viva voce, etc.): 50 marks

## **Summer Internship**

A summer internship is a short-term work placement, usually during the summer break, where students gain hands-on experience in their field. It allows them to apply classroom theories in a real-world environment, develop both technical and soft skills, and build professional networks. Interns work on projects that expose them to industry practices and workplace dynamics, providing valuable insights into their future careers.

## **Course Guidelines:**

- The Summer Internship course is typically offered during the fifth semester.
  - The course is evaluated out of a total of 100 marks, with assessments based on a report, presentation, and viva voce.
  - Students may work in groups; however, each member must submit an individual report.
  - A faculty member, designated by the Head of the Department, will supervise the course.
  - An internal examiner will be responsible for evaluating the course.
  - The course is designed to encourage meaningful interaction with the end user.
  - The selected internship project should provide ample opportunities to apply and demonstrate the concepts learned in the course.
  - Internal marks (based on Internship report, work dairy, etc.): 50 marks.
  - External marks (based on presentation, viva voce, etc.): 50 marks