

Input:

$$\frac{dy}{dx} = \frac{2y}{x}$$

Output:

```
Input initial values of x and y: 1 1
Input x at which y is required: 2
Input step-size h: 0.1
Value of y at x=2 is 3.81818
PS C:\Users\Roshan\Desktop\Roshan NM\unit 4> █
```

Input:

$$\frac{dy}{dx} = 3x + \frac{y}{2}$$

Output:

```
Input initial values of x and y: 0 1
Input x at which y is required: 1
Input step-size h: 0.1
Value of y at x=1 is 3.17563
PS C:\Users\Roshan\Desktop\Roshan NM\unit 4> █
```

Input:

$$\frac{dy}{dx} = \frac{2y}{x}$$

Output:

```
Enter initial values of,  
x: 1  
y: 1  
Input x at which y is required: 1  
Input step-size h: 0.4  
  
Value of y at A = 1 is 1  
PS C:\Users\Roshan\Desktop\Roshan NM\unit 4> █
```

Input:

$$\frac{dy}{dx} = 2xy$$

Output:

```
Enter initial values of,  
x: 0  
y: 1  
Input x at which y is required: 1  
Input step-size h: 0.2  
  
Value of y at A = 1 is 2.68138  
PS C:\Users\Roshan\Desktop\Roshan NM\unit 4> █
```

Input:

$$y' = y \cos$$

Output:

```
Input initial values of x and y: 0 1
Input x at which y is required: 0.5
Input step-size h: 0.25

1      0.25 1.28069
2      0.5 1.61513
Value of y at x = 0.5 is 1.61513
PS C:\Users\Roshan\Desktop\Roshan NM\unit 4> █
```

Input:

$$y' = x+y$$

Output:

```
Input initial values of x and y: 0 1
Input x at which y is required: 0.5
Input step-size h: 0.25

1      0.25 1.31803
2      0.5 1.7974
Value of y at x = 0.5 is 1.7974
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```

Input:

$$\frac{dy_1}{dx} = x + y_1 + y_2, \quad \frac{dy_2}{dx} = 1 + y_1 + y_2$$

Output:

```
Enter the initial point x: 0

Enter the value of y1(x): 1

Enter the value of y2(x): -1

Enter the step length(h): 0.1

Enter the point x at which y(x) is required: 0.2

Calculation of y1(0.2) and y2(0.2):

x          y1(x)          y2(x)
0           1             -1
0.1         1.01          -0.895
0.2         1.04315       -0.77685

Do you want to approximate at another point?(y/n): n
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```

Input:

$$\frac{dy_1}{dx} = y_1 y_2 + x^2 + 1, \quad \frac{dy_2}{dx} = y_2 + x y_1 + y_1$$

Output:

```
Enter the initial point x: 0

Enter the value of y1(x): 0

Enter the value of y2(x): 0

Enter the step length(h): 0.1

Enter the point x at which y(x) is required: 0.2

Calculation of y1(0.2) and y2(0.2):

x          y1(x)          y2(x)
0           0             0
0.1         0.105         0.0055
0.2         0.222208      0.025393

Do you want to approximate at another point?(y/n): n
PS C:\Users\Roshan\Desktop\Roshan NM\unit 4>
```

Input:

$$\frac{d^2y}{dx^2} + 2\frac{dy}{dx} - 3y = 6x$$

Output:

```
Enter the initial point x: 0
Enter the value of y(x): 0
Enter the value of y'(x): 1
Enter the step length (h): 0.1

Enter the point x at which y(x) is required: 0.2

The approximate value of y(0.2) is 0.1722.

Do you want to approximate at another point? (y/n): n
PS C:\Users\Roshan\Desktop\Roshan NM\unit 4> █
```

Input:

$$\frac{d^2y}{dx^2} + 4\frac{dy}{dx} + 5y = 8x$$

Output:

```
Enter the initial point x: 0
Enter the value of y(x): 0
Enter the value of y'(x): 1
Enter the step length (h): 0.1

Enter the point x at which y(x) is required: 0.4

The approximate value of y(0.4) is 0.228393.

Do you want to approximate at another point? (y/n): n
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```

Input:

$$\frac{d^2y}{dx^2} = 2x^2y + 1$$

Output:

```
Enter the first boundary conditions x and y(x): 0 1
Enter the second boundary conditions x and y(x): 1 1
Enter the step length: 0.5
Enter the first guess of y'(0): 1.3

Enter the second guess of y'(0): 1.8

Enter the point x at which y(x) is required: 1

The approximate value of y(1) is 0.445312.
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```

Input:

$$\frac{d^2y}{dx^2} = 4x^3y + 2$$

Output:

```
Enter the first boundary conditions x and y(x): 0 1
Enter the second boundary conditions x and y(x): 1 1
Enter the step length: 0.5
Enter the first guess of y'(0): 1

Enter the second guess of y'(0): 0

Enter the point x at which y(x) is required: 0.5

The approximate value of y(0.5) is 0.25.
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```