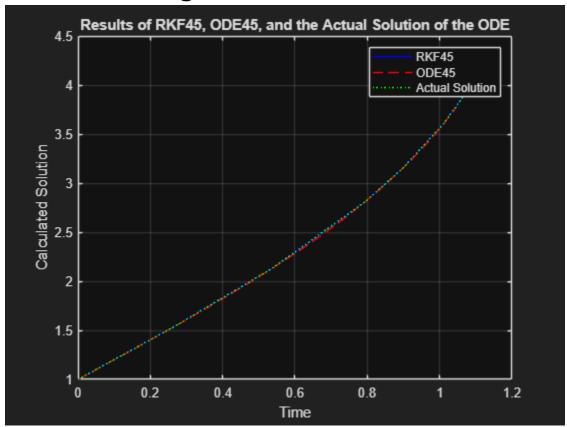
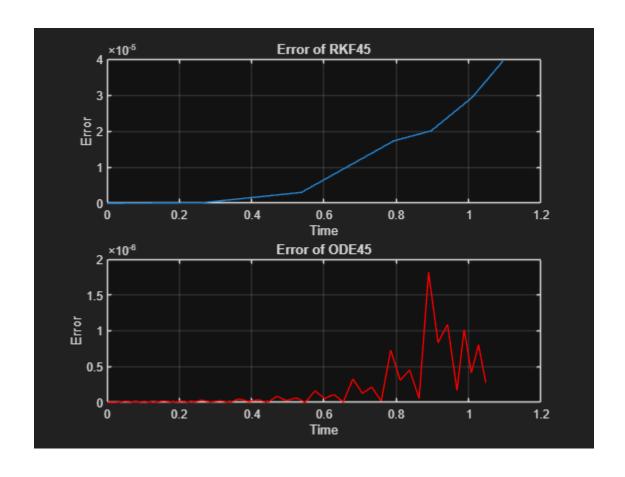
Table of Contents

	!
Workspace Prep	. .
PART 1: Using RKF45 to Solve an ODE	1
PART 2: Lorenz Equation	
1	
Lorenz Function	i
Runge-Kutta-Fehlberg Function	3

Workspace Prep

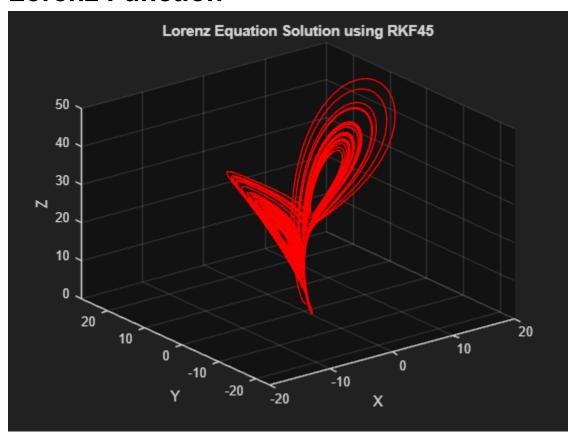
PART 1: Using RKF45 to Solve an ODE





PART 2: Lorenz Equation

Lorenz Function



Runge-Kutta-Fehlberg Function

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Table of Contents

	1
Workspace Prep	1
PART 1: Using RKF45 to Solve an ODE	1
PART 2: Lorenz Equation	2
Lorenz Function	3
Runge-Kutta-Fehlberg Function	
%Roshan Jaiswal-Ferri %Section - 03	
%Aero 300 Lab 7 - Runge-Kutta-Fehlberg Methods: 5/17/24	

Workspace Prep

PART 1: Using RKF45 to Solve an ODE

```
%Given Parameter
t = [0, pi/3];
y0 = 1;
h = 0.01;
rtol = 1e-6;
%Given ODE
fun = @(t, y) (y - t - 1)^2 + 2;
%Solution to ODE (solution function)
solf = @(t) tan(t) + t + 1;
%Using rkf45
[t1, y1] = rkf45(fun, t, y0, h, rtol);
%Using ode45
options = odeset('RelTol', rtol, 'AbsTol', 1e-6);
[t2, y2] = ode45(fun, t, y0, options);
%rkf45 Error
for i = 1: length(t1)
    sol = solf(t1(i));
    rkfErr(i) = abs(y1(i) - sol); % Calculate the error for rkf45 at given
point
end
%ode45 Error
```

```
for i = 1: length(t2)
    sol = solf(t2(i));
    odeErr(i) = abs(y2(i) - sol); % Calculate the error for ode45 at given
end
%Plotting Results
figure('Name','Solution Plot')
plot(t1, y1, 'b');
hold on;
grid on;
plot(t2, y2, 'r--');
plot(t1, solf(t1), 'g:');
xlabel('Time');
ylabel('Calculated Solution');
legend('RKF45','ODE45','Actual Solution')
title('Results of RKF45, ODE45, and the Actual Solution of the ODE');
figure('Name','Error Comparison')
subplot(2,1,1)
plot(t1, rkfErr);
grid on;
xlabel('Time');
vlabel('Error');
title('Error of RKF45');
subplot(2,1,2)
plot(t2, odeErr, 'r');
grid on;
xlabel('Time');
vlabel('Error');
title('Error of ODE45');
```

PART 2: Lorenz Equation

```
%New Parameters
t = [0 50];
y0 = [1; 1; 1];
h = 0.01;
rTol = 1*10^-6;
%using rkf45
[t3, y3] = rkf45(@lorenz, t, y0, h, rTol);
%This is just to reorganize the data vector, long story short the output of %rkf45 is one column that is super long that contains all 3 columns (x y z)%data. In this super long column every-other-other starting from 1 is x,%every-other-other starting from 2 is y, and every-other-other starting
%from 3 is z. This code takes all the data and reorganizes it into%a new matrix that has 3 columns and assigns each data point to where its%proper column coordinate (x y z)
```

```
numRows = totalPts / 3;
y4 = zeros(numRows, 3);
for i = 1:numRows
        y4(i, 1) = y3((i-1)*3 + 1);
        y4(i, 2) = y3((i-1)*3 + 2);
        y4(i, 3) = y3((i-1)*3 + 3);
end

%Plotting Results
figure('Name', 'Lorenz Equation')
plot3(y4(:,1), y4(:,2), y4(:,3), 'r');
title('Lorenz Equation Solution using RKF45');
grid on;
xlabel('X');
ylabel('Y');
zlabel('Z');
```

Lorenz Function

Runge-Kutta-Fehlberg Function

```
function [t, y] = rkf45(fun, tspan, y0, h, rTol)
    f = fun;
   t0 = tspan(1);
   t2 = tspan(2);
    t = t0;
    y = y0;
    t1 = t;
   Wn1 = y;
   while t(end) < t2
        s1 = f(t1, Wn1);
        s2 = f(t1 + (1/4)*h, Wn1 + (1/4)*h*s1);
        s3 = f(t1 + (3/8)*h, Wn1 + (3/32)*h*s1 + (9/32)*h*s2);
        s4 = f(t1 + (12/13)*h, Wn1 + (1932/2197)*h*s1 - (7200/2197)*h*s2 +
(7296/2197) *h*s3);
        s5 = f(t1 + h, Wn1 + (439/216)*h*s1 - 8*h*s2 + (3680/513)*h*s3 -
(845/4104) *h*s4);
        s6 = f(t1 + (1/2)*h, Wn1 - (8/27)*h*s1 + 2*h*s2 - (3544/2565)*h*s3 +
(1859/4104)*h*s4 - (11/40)*h*s5);
        %4th and 5th order estimate
```

```
WNext = Wn1 + h*((25/216)*s1 + (1408/2565)*s3 + (2197/4104)*s4 -
(1/5)*s5);
        ZNext = Wn1 + h*((16/135)*s1 + (6656/12825)*s3 + (28561/56430)*s4 -
(9/50)*s5 + (2/55)*s6);
        %Error
        err = norm(ZNext - WNext);
        %Error test
        if err / abs(WNext) < rTol</pre>
            t = [t; t1 + h];
            y = [y; WNext];
            Wn1 = ZNext;
            t1 = t1 + h;
        end
        %Changing step size
        h = 0.8 * ((rTol/err)^(.2)) * h;
    end
end
```

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