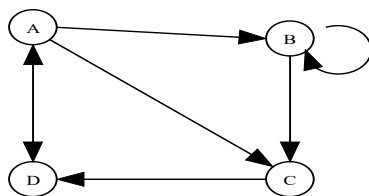


**Junior Division Solutions**

**1. Graph Theory**

1. As shown

**2. Graph Theory**

$$\begin{vmatrix} 0 & 1 & 1 & 0 & 1 \\ 1 & 0 & 1 & 0 & 0 \\ 1 & 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 \\ 1 & 1 & 0 & 0 & 0 \end{vmatrix}$$

2. As shown

**3. Boolean Algebra**

$$A(\overline{AB} + \overline{B}) = A\overline{A}B + A\overline{B} = 0 + A\overline{B} = A\overline{B}$$

$$A\overline{B} = 1 \rightarrow A = 1 \wedge \overline{B} = 1 \rightarrow A = 1 \wedge B = 0 \rightarrow (1, 0)$$

3. (1, 0)

**4. Boolean Algebra**  $X = \overline{A} + B\overline{C} + A(\overline{B} + C)$ 

$A$	$B$	$C$	$\overline{B}$	$\overline{C}$	$\overline{A}$	$B\overline{C}$	$\overline{B} + C$	$A(\overline{B} + C)$	$X$
0	0	0	1	1	1	0	1	0	1
0	0	1	1	0	1	0	1	0	1
0	1	0	0	1	1	1	0	0	1
0	1	1	0	0	1	0	1	0	1
1	0	0	1	1	0	0	1	1	1
1	0	1	1	0	0	0	1	1	1
1	1	0	0	1	0	1	0	0	1
1	1	1	0	0	0	0	1	1	1

4. 8

**5. What Does This Program Do?**

This program changes entries in the table that are divisible by 4, 3, 10 and 2. Then it counts the entries with a value of 1. The final table is:

7	1	1	3
2	11	1	9
7	5	3	1
2	1	27	1

5. 6