

# ACSL

2013 - 2014

American Computer Science League

Contest #1

## Intermediate Division Solutions

### 1. Recursive Functions

$$\begin{aligned} f(12) &= 2 * f(9) - 3 = 2 * 49 - 3 = 95 \\ f(9) &= 2 * f(6) - 3 = 2 * 26 - 3 = 49 \\ f(6) &= f(8) + 1 = 25 + 1 = 26 \\ f(8) &= 2 * f(5) - 3 = 2 * 14 - 3 = 25 \\ f(5) &= f(7) + 1 = 13 + 1 = 14 \\ f(7) &= 2 * f(4) - 3 = 2 * 8 - 3 = 13 \\ f(4) &= 4 + 4 = 8 \quad \text{Now substitute backwards.} \end{aligned}$$

1. 95

### 2. Recursive Functions

$$\begin{aligned} f(10,2) &= f(8,4) + 2 = 38 + 2 = 40 \\ f(8,4) &= f(6,6) + 2 = 36 + 2 = 38 \\ f(6,6) &= f(7,5) - 1 = 37 - 1 = 36 \\ f(7,5) &= f(5,7) + 2 = 35 + 2 = 37 \\ f(5,7) &= 5 * 7 = 35 \end{aligned}$$

Now substitute backwards.

2. 40

### 3. Computer Number Systems

$$\begin{aligned} 110111_2 &= 55 & \text{Sum} &= 55 + 63 + 58 + 84 = 260 \\ 63_{10} &= 63 & \text{Average} &= 65 = 101_8 \\ 3A_{16} &= 58 \\ 124_8 &= 84 \end{aligned}$$

3.  $101_8$  or 101

### 4. Computer Number Systems

$$\begin{aligned} 178_{16} &= 101111000 & 5 \text{ 1's} \\ 567_8 &= 101110111 & 7 \text{ 1's} \\ 101110110_2 &= 101110110 & 6 \text{ 1's} \\ 565_8 &= 101110101 & 6 \text{ 1's} \\ 377_{10} &= 101111001 & 6 \text{ 1's} \end{aligned}$$

4.  $567_8$

### 5. What Does This Program Do?

The table contains the values of a, b, c, d and e after each line.

a	b	c	d	e
10	5	20	1	2
10	5	20	1	2
10	5	20	25	2
10	20	20	25	2
10	8	20	25	2
10	8	20	5	2

$$\text{So } c / (b + e) - d^2 + a / e = 20 / (8 + 2) - 5^2 + 10/2 = -18$$

5. -18