

**Recursion #1****Find each of the following.**

1) Find  $f(6)$ :  $f(x) = \begin{matrix} f(x-1) + x & \text{when } x > 1 \\ x - 2 & \text{when } x = 1 \end{matrix}$

2) Find  $f(5)$ :  $f(x) = \begin{matrix} f(x-1) + x & \text{when } x > 1 \\ x - 2 & \text{when } x \leq 1 \end{matrix}$

3) Find  $f(7)$ :  $f(x) = \begin{matrix} f(x+3) + 4 & \text{when } x \leq 12 \\ 3 & \text{when } x > 12 \end{matrix}$

4) Find  $f(2)$ :  $f(x) = \begin{matrix} f(x-1) + x & \text{when } x > 0 \\ 2 & \text{when } x = 0 \\ 5 & \text{when } x < 0 \end{matrix}$

5) Find  $f(6)$ :  $f(x) = \begin{matrix} f(f(x-2)) + 1 & \text{when } x > 1 \\ 2 & \text{when } x = 1 \\ 1 & \text{when } x = 0 \end{matrix}$

6) Find  $f(238)$ :  $f(x) = \begin{matrix} f(x-64) + 100 & \text{when } x \geq 64 \\ f(x-8) + 10 & \text{when } 8 \leq x < 64 \\ x & \text{when } x < 8 \end{matrix}$

7) Find  $f(f(f(2)))$ :  $f(x) = \begin{matrix} x - 1 & \text{when } x \geq 4 \\ 2x & \text{when } 0 \leq x < 4 \\ 1/x & \text{when } x < 0 \end{matrix}$

8) Find  $f(5)$ : *GIVEN:*  $p(x, y) = x * y$

$$f(n) = \begin{cases} 1 & n = 0 \\ p(n, f(n-1)) & \text{otherwise} \end{cases}$$

9) Find  $f(-4)$ :  
$$f(x) = \begin{cases} 2(f(x+2)) - f(x+1) + 1 & \text{when } x < 0 \\ 1 & \text{when } x = 0 \\ 0 & \text{when } x > 0 \end{cases}$$

10) Find  $f(12, 6)$ :  $f(x, y) = \begin{cases} f(x-y, y+1) + 2 & \text{when } x > y \\ x + y & \text{otherwise} \end{cases}$

11) Find  $f(6, 5)$ :  
$$f(x, y) = \begin{cases} 2 + f(x-3, y-1) & \text{when } x > y \text{ and } x > 0 \\ 1 + f(y, x) & \text{when } y \geq x \text{ and } x > 0 \\ 0 & \text{when } x \leq 0 \end{cases}$$

12) Find  $f(4, 1)$ :  $f(x, y) = \begin{cases} f(x, y+1) - 8 & \text{when } x \geq y \\ 4 & \text{when } x < y \end{cases}$

13) Find  $f(3, 5)$ :  $f(a, n) = \begin{cases} a & \text{when } n = 1 \\ a * f(a, n-1) & \text{when } n > 1 \end{cases}$

14) Find  $f(0, 2)$ :  
$$f(x, y) = \begin{cases} f(x+1, y) + 2 & \text{when } x < y \\ 10 & \text{when } x = y \\ 0 & \text{when } x > y \end{cases}$$