American Computer Science League

Contest #3

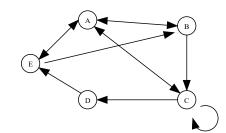
Junior Division

1. Graph Theory

Draw the directed graph containing the following vertices and edges. Vertices: {A, B, C, D} Edges: {AB, BB, BC, CD, DA, AD, AC}

2. Graph Theory

Write the adjacency matrix for the directed graph.



3. Boolean Algebra

Which ordered pairs make the following Boolean expression TRUE?

$$A(\overline{A}B + \overline{B})$$

4. Boolean Algebra

How many ordered triples make the following circuit TRUE?

$$\overline{A} + B\overline{C} + A(\overline{B} + C)$$

5. What Does This Program Do?

Given array A below, what is the final value of C after the program is run?

$$C = O$$

FOR
$$I = 1$$
 TO 4

FOR
$$J = 1$$
 TO 4

IF A(I,J)/4 = INT(A(I,J)/4) THEN A(I,J)=A(I,J)/4

IF A(I,J)/3 = INT(A(I,J)/3) THEN A(I,J)=A(I,J)/3

IF A(I,J)/10 = INT(A(I,J)/10) THEN A(I,J)=A(I,J)/10

IF A(I,J)/2 = INT(A(I,J)/2) THEN A(I,J)=A(I,J)/2

NEXT J

NEXT I

FOR I = 4 TO 1 STEP -1

FOR
$$J = 1$$
 TO 4

IF
$$A(I,J) = 1$$
 THEN $C = C + 1$

NEXT J

NEXT I

PRINT C

END

21	8	4	90	
48	44	1	27	
70	5	36	10	
16	40	81	24	

Note: A(1,1) = 16