American Computer Science League

Contest #1

Intermediate Division

1. Recursive Functions

Find f(12) given:

$$f(x) = \begin{cases} 2 * f(x-3) - 3 & \text{if } x > 6 \\ f(x+2) + 1 & \text{if } 4 < x \le 6 \\ x + 4 & \text{if } x \le 4 \end{cases}$$

2. Recursive Functions

Find f(10,2) given:

$$f(x,y) = \begin{cases} f(x-2, y+2) + 2 & \text{if } x > y \\ f(x+1, y-1) - 1 & \text{if } x = y \\ xy & \text{if } x < y \end{cases}$$

3. Computer Number Systems

Find the average of the following. Express the answer in octal.

4. Computer Number Systems

Which of the following has the most 1's in its binary representation?

$$178_{16}$$
 567_8 101110110_2 565_8 377_{10}

5. What Does This Program Do?

What is printed when this program is run?

$$\begin{array}{l} a = 10: b = 5: c = 20: d = 1: e = 2 \\ \text{if } a + b > c \ / \ e \ \text{then } b = a - b \ \text{else } c = c \ * \ e \\ \text{if } a \ / \ b = c \ / \ b \ \text{then } a = b + 2 \ * \ e \ \text{else } d = b \ ^ 2 \\ \text{if } (a > b) \ \text{and } (c > d) \ \text{then } e = d \ / \ b \ \text{else } b = a + c \ / \ e \\ \text{if } (a + c > d \ * \ e) \ \text{or } (b \ / \ c = b \ / \ (2 \ * \ a)) \ \text{then } b = a - e \\ \text{else } c = b - c \\ \text{if } (a < b) \ \text{or } (c < d) \ \text{and } (b + e = a) \ \text{then } d = d - c \ \text{else } c = c \ / \ a \\ \text{print } c \ / \ (b + e) - d \ ^ 2 + a \ / \ e \\ \text{end} \end{array}$$