

# ACSL

2013 - 2014

American Computer Science League

All-Star

## Short Round Questions

### 1. Boolean Algebra

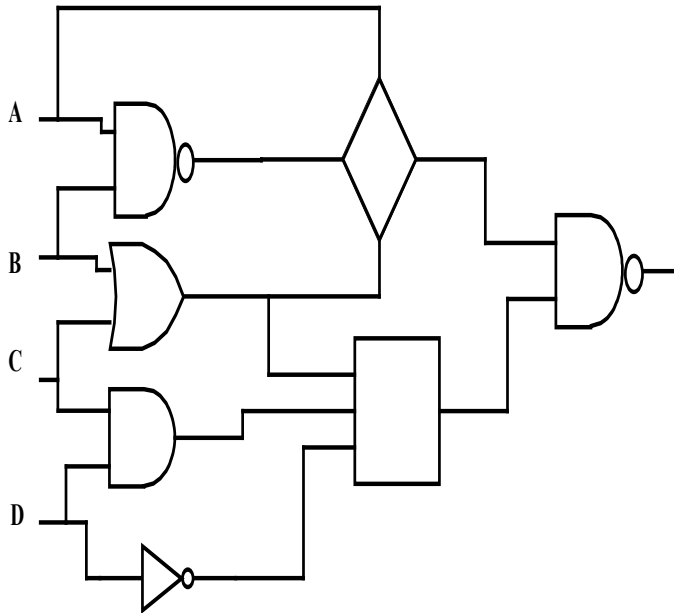
Simplify the following Boolean expression:

$$\overline{\overline{A(B+C) + BC}} \overline{\overline{AB + C + ABC}}$$

- A. 0
- B.  $\overline{AC} + \overline{B}$
- C.  $A + \overline{BC}$
- D. 1
- E. None of the above

### 2. Digital Electronics

Let  $\square$  be a gate with 3 inputs that is true if exactly 2 inputs are the same. Let  $\diamond$  be a gate with 3 inputs that is true if at least 1 input is true. How many ordered quadruples make the following circuit true?



- A. 0
- B. 2
- C. 4
- D. 8
- E. None of the above

### 3. Prefix-Infix-Postfix

Define:  $a \# b = (a+b)/2$

$a \% b = [a/b] = \text{greatest integer } \leq a/b$

$a \& = \sqrt{a} = \text{principal square root of } a$

Evaluate the following prefix expression: (all single digits)

$- + \% 9 2 * \& 9 \uparrow + / \# 9 7 4 \& 4 2 // * / * 9 \# 7 5 \% 7 2 8 \& + 9 7 \& 4$

- A. 21
- B. 52
- C. 34
- D. 56
- E. None of the above

#### 4. Computer Number Systems

Which term is next (expressed in octal) in the sequence below?

$11_2$     $11_8$     $11011_2$     $51_{16}$     $?_8$

- A. 213
- B. 243
- C. 323
- D. 363
- E. None of the above

#### 5. Bit-String Flicking

Which value(s) of X (five bits long) solve the following equation?

$$(\text{LCIRC} - 2 (01011 \text{ OR } X)) \text{ AND } (\text{RSHIFT} - 2 (10111 \text{ AND } X)) = (\text{RCIRC} - 2 (\text{LSHIFT} - 1 X))$$

- A. 11010, 10010
- B. 10101, 10001
- C. 11000, 00000
- D. 10100, 11100
- E. None of the above

#### 6. What Does This Program Do?

What is the output after this program is executed?

```
c = 99
for i = 2 to 99 step 2
    c = c - 1
next i
for j = 3 to 99 step 6
    if j/5 = int(j/5) then c = c - 1
next j
for k = 5 to 99 step 10
    if k = 5 then c = c - 1
    if (k/3 > int(k/3)) and (k < 5) then c = c - 1
next k
print c
end
```

- A. 36
- B. 39
- C. 41
- D. 49
- E. None of the above

#### 7. Recursive Functions

Find  $f(13,1)$  given:

$$f(x, y) = \begin{cases} f(x-1, y+3) + 3 & \text{if } x > y \\ x + f(x+4, y-2) & \text{if } x = y \\ 2x + 3y & \text{if } x < y \end{cases}$$

- A. 75
- B. 91
- C. 88
- D. 94
- E. None of the above

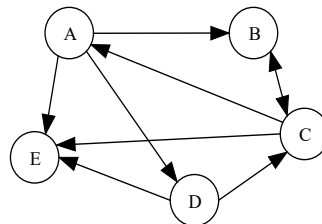
#### 8. Data Structures

Given a heap of depth six and with the bottom level completely filled, what is its internal path length?

- A. 384
- B. 642
- C. 896
- D. 1538
- E. None of the above

## 9. Graph Theory

Adding which directed edge to the original graph will increase the number of cycles from 4 by the smallest number?



- A. EB
- B. EA
- C. EC
- D. ED
- E. BA

## 10. LISP

(SETQ X '(1(2(34))(5(67)8(9(14))))))

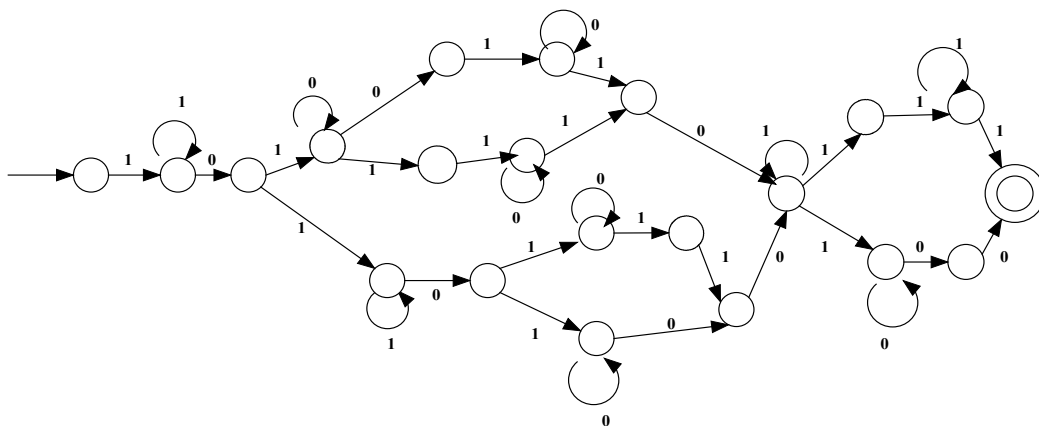
Evaluate the following expression:

(CAR (CAR (REVERSE (CDR (CDR X))))))

- A. (6 7)
- B. (5)
- C. (5 (6 7))
- D. (1 4)
- E. None of the above

## 11. FSA and Regular Expressions

Which of the strings below are represented by the following FSA?



- A. a, b, c, d
- B. a, c, d, e
- C. a, c, e, f
- D. a, c, d, f
- E. None of the above

- a. 1010100111
- b. 110101110100101
- c. 101001100101111111
- d. 1101101011011100
- e. 1010100011010
- f. 11010001000101111000000000

## 12. Assembly Language

After the following program is executed, what is printed? The data for the program is 1, -1, 2, -2, 3, -3, 4, -4, 5, -5, 0.

TOP	READ	N		SUB	=30
	BE	DONE		BE	ANS
	LOAD	N		BU	TOP
	MULT	N		PRINT	N
	MULT	=2		BU	TOP
	STORE	TEMP1		DONE	END
	LOAD	N			
	MULT	=4			
	STORE	TEMP2			
	LOAD	TEMP1			
	SUB	TEMP2			

- A. 5, -1
- B. -3, 2
- C. -3, 5
- D. 4, 5
- E. None of the above