Preventing Glitches and Short Circuits in

Cornell University

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Ross Tate

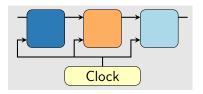
High-Level Self-Timed Chip Specifications

Brittany Nkounkou

Stephen Longfield

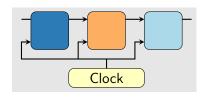
Preventing Glitches and Short Circuits in High-Level Self-Timed Chip Specifications

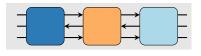




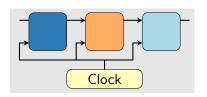
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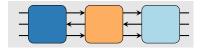
Self-Timed

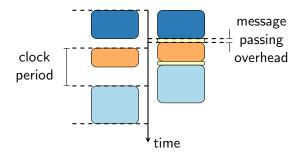




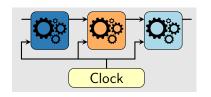
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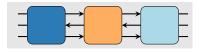


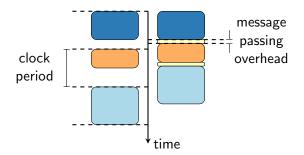




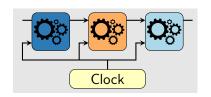
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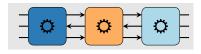


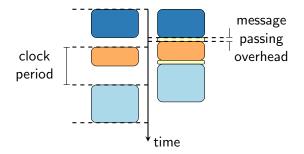




Self-Timed

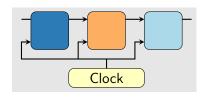


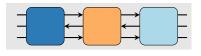




Clocked

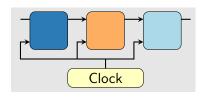
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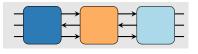


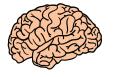


Clocked

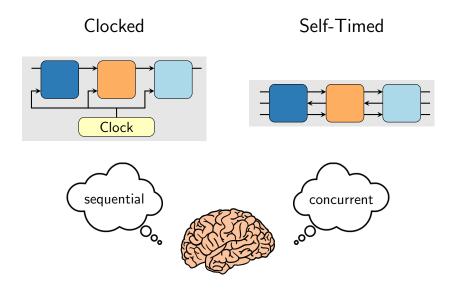
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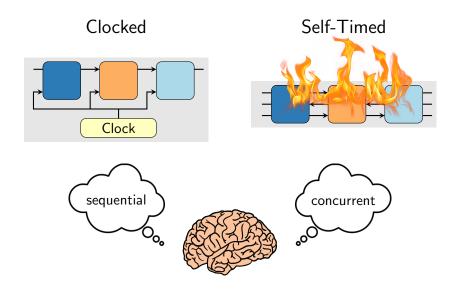


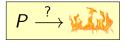




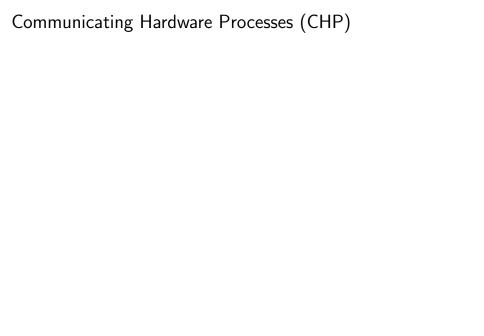
Clocked Self-Timed Clock sequential











Channel A

Channel A

Program P ::=

Channel A

Program P := A!

Channel A

Program $P := A! \mid A?$

Channel A

Program $P := A! \mid A? \mid P; P$

Channel A

Program $P ::= A! \mid A?$ $\mid P; P \mid P \parallel P$

Channel A

Program $P ::= A! \mid A?$ $\mid P; P \mid P \mid P \mid *P$

Channel A

 $\begin{array}{c} \mathsf{Program}\ P ::=\ A!\ |\ A? \\ |\ P;P\ |\ P\ |\ P\ |\ *P\ |\ \mathtt{skip} \end{array}$

Channel A

Program $P ::= A! \mid A?$ $\mid P; P \mid P \mid P \mid *P \mid \text{skip} \mid \dots$

Channel A

Program $P ::= A! \mid A?$ $\mid P; P \mid P \mid P \mid *P \mid \text{skip} \mid \dots$

 $P; P' \parallel Q; Q'$

Channel A

```
P; P' \parallel Q; Q
```

Channel A

 $P; A!; P' \parallel Q; A?; Q'$

Channel A

 $P; A!; P' \parallel Q; A?; Q' \longrightarrow \dots$

Channel A

Program $P ::= A! \mid A?$ $\mid P; P \mid P \mid P \mid *P \mid \text{skip} \mid \dots$

 $P; A!; P' \parallel Q; A?; Q' \longrightarrow \ldots \longrightarrow A!; P' \parallel A?; Q'$

Channel A

Program $P ::= A! \mid A?$ $\mid P; P \mid P \mid P \mid *P \mid \text{skip} \mid \dots$

P; A!; $P' \parallel Q$; A?; $Q' \longrightarrow \ldots \longrightarrow A$!; $P' \parallel A$?; $Q' \longrightarrow P' \parallel Q'$

Channel A

Program
$$P ::= A! \mid A?$$

 $\mid P; P \mid P \mid P \mid *P \mid \text{skip} \mid \dots$

$$P; A!; P' \parallel Q; A?; Q' \longrightarrow \ldots \longrightarrow A!; P' \parallel A?; Q' \longrightarrow P' \parallel Q'$$

ideal: A!; $P \parallel A?$; $Q \longrightarrow P \parallel Q$

Channel A

Program
$$P ::= A! \mid A?$$

 $\mid P; P \mid P \mid P \mid *P \mid \text{skip} \mid \dots$

$$P; A!; P' \parallel Q; A?; Q' \longrightarrow \ldots \longrightarrow A!; P' \parallel A?; Q' \longrightarrow P' \parallel Q'$$

ideal:
$$A!$$
; $P \parallel A?$; $Q \longrightarrow P \parallel Q$

$$(A! \parallel A?) \parallel (A! \parallel A?)$$

Channel A

Program
$$P ::= A! \mid A?$$

 $\mid P; P \mid P \mid P \mid *P \mid \text{skip} \mid \dots$

$$P; A!; P' \parallel Q; A?; Q' \longrightarrow \ldots \longrightarrow A!; P' \parallel A?; Q' \longrightarrow P' \parallel Q'$$

ideal:
$$A!$$
; $P \parallel A?$; $Q \longrightarrow P \parallel Q$

$$(A! \parallel A?) \parallel (A! \parallel A?) \longrightarrow$$

Channel A

Program $P ::= A! \mid A?$ $\mid P; P \mid P \mid P \mid *P \mid \text{skip} \mid \dots$

```
Channel A:=\langle \bar{A},\hat{A}\rangle Program P::=A!\mid A? \mid P;P\mid P\parallel P\mid *P\mid \mathrm{skip}\mid \dots
```

```
Channel A:=\langle \bar{A},\hat{A}\rangle

Program P::=A!\mid A?

\mid P;P\mid P\parallel P\mid *P\mid {\rm skip}\mid \dots
```

```
ar{A} ar{A} ar{A}
```

```
Channel A := \langle \bar{A}, \hat{A} \rangle

Program P ::= A! \mid A? \mid P; P \mid P \mid P \mid P \mid \text{skip} \mid \dots
```

```
ar{A} \xrightarrow{\longrightarrow} \hat{A}
```

```
Channel A := \langle \bar{A}, \hat{A} \rangle

Program P ::= A! \mid A? \mid P; P \mid P \mid P \mid P \mid \text{skip} \mid \dots
```

```
ar{A} \Longrightarrow \hat{A}
```

```
Channel A := \langle \bar{A}, \hat{A} \rangle

Program P ::= A! \mid A? \mid P; P \mid P \mid P \mid P \mid \text{skip} \mid \dots
```

```
\bar{A} \hat{A} \hat{A}
```

```
Channel A:=\langle \bar{A},\hat{A}\rangle

Program P::=A!\mid A?

\mid P;P\mid P\parallel P\mid *P\mid {\rm skip}\mid \dots
```

```
\bar{A} \hat{A} \hat{A}
```

```
Channel A := \langle \bar{A}, \hat{A} \rangle

Program P ::= A! \mid A? \mid P; P \mid P \mid P \mid P \mid \text{skip} \mid \dots
```



```
Channel A := \langle \bar{A}, \hat{A} \rangle

Program P ::= A! \mid A? \mid A_i \mid P; P \mid P \mid P \mid *P \mid \text{skip} \mid \dots
```

```
\hat{A} \hat{A} \hat{A}
```

```
Channel A := \langle \bar{A}, \hat{A} \rangle

Program P := A! \mid A? \mid A_i \mid A_i \mid A_i \mid P; P \mid P \mid P \mid P \mid Skip \mid \dots
```

```
\hat{A} \hat{A}
```

```
Channel A := \langle \bar{A}, \hat{A} \rangle

Program P ::= A! \mid A? \mid A_i \mid A_i \mid A_i \mid P; P \mid P \mid P \mid P \mid Skip \mid \dots
```



ideal:

```
Channel A := \langle \bar{A}, \hat{A} \rangle

Program P := A! \mid A? \mid A_i \mid A_i \mid A_i \mid P; P \mid P \mid P \mid P \mid Skip \mid \dots
```



ideal: $A! \parallel A?$

Channel $A := \langle \bar{A}, \hat{A} \rangle$ Program $P := A! \mid A? \mid A_i \mid A_i \mid A_i \mid P; P \mid P \mid P \mid P \mid Skip \mid \dots$



ideal: $A! \parallel A? \longrightarrow A_i \parallel A?$

Channel
$$A := \langle \bar{A}, \hat{A} \rangle$$

Program $P := A! \mid A? \mid A_i \mid A_i \mid A_i \mid P; P \mid P \mid P \mid P \mid Skip \mid \dots$

$$\vec{A}$$
 \hat{A} \hat{A}

ideal: $A! \parallel A? \longrightarrow A_i \parallel A? \longrightarrow A_i \parallel A_i$

Channel
$$A := \langle \bar{A}, \hat{A} \rangle$$

Program $P := A! \mid A? \mid A_i \mid A_i \mid A_i \mid P; P \mid P \mid P \mid P \mid Skip \mid \dots$

$$\vec{A}$$
 \vec{A} \vec{A}

ideal: $A! \parallel A? \longrightarrow A_i \parallel A? \longrightarrow A_i \parallel A_i \longrightarrow \text{skip} \parallel A_i$

```
Channel A := \langle \bar{A}, \hat{A} \rangle

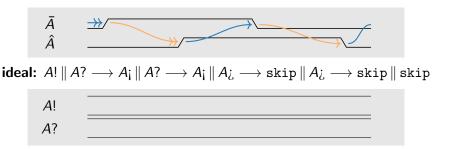
Program P := A! \mid A? \mid A_i \mid A_i \mid A_i \mid A_i \mid P; P \mid P \mid P \mid P \mid Skip \mid \dots
```

$$\bar{A}$$
 \hat{A} \hat{A}

 $\textbf{ideal:} \ A! \parallel A? \longrightarrow A_i \parallel A? \longrightarrow A_i \parallel A_i \longrightarrow \mathtt{skip} \parallel A_i \longrightarrow \mathtt{skip} \parallel \mathtt{skip}$

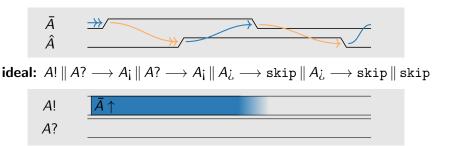
Channel
$$A := \langle \bar{A}, \hat{A} \rangle$$

Program $P ::= A! \mid A? \mid A_i \mid A_i \mid A_i \mid P; P \mid P \mid P \mid P \mid Skip \mid \dots$



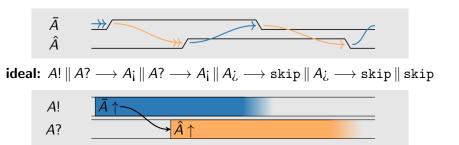
Channel
$$A := \langle \bar{A}, \hat{A} \rangle$$

Program $P ::= A! \mid A? \mid A_i \mid A_i \mid A_i \mid P; P \mid P \mid P \mid P \mid Skip \mid \dots$



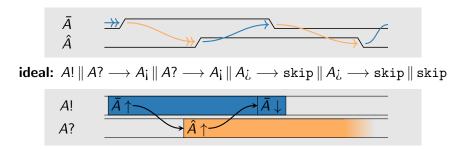
Channel
$$A := \langle \bar{A}, \hat{A} \rangle$$

Program $P ::= A! \mid A? \mid A_i \mid A_i \mid A_i \mid P; P \mid P \mid P \mid P \mid Skip \mid \dots$



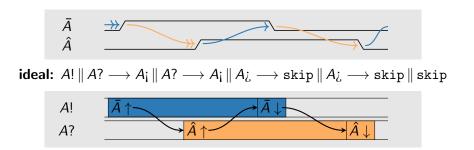
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Program $P := A! \mid A? \mid A_i \mid A_i \mid A_i \mid P; P \mid P \mid P \mid P \mid \text{skip} \mid \dots$



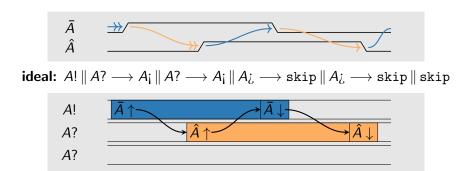
Channel
$$A := \langle \bar{A}, \hat{A} \rangle$$

Program $P := A! \mid A? \mid A_i \mid A_i \mid A_i \mid P; P \mid P \mid P \mid P \mid \text{skip} \mid \dots$



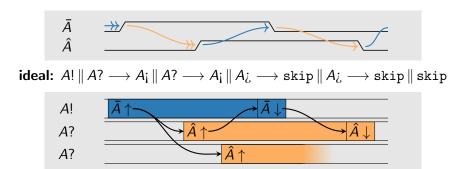
Channel
$$A := \langle \bar{A}, \hat{A} \rangle$$

Program $P ::= A! \mid A? \mid A_i \mid A_i \mid A_i \mid P; P \mid P \mid P \mid P \mid Skip \mid \dots$



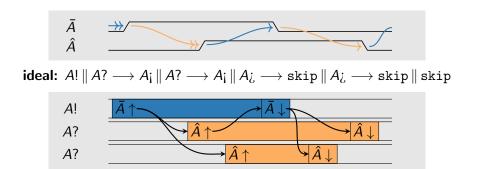
Channel
$$A := \langle \bar{A}, \hat{A} \rangle$$

Program $P := A! \mid A? \mid A_i \mid A_i \mid A_i \mid A_i \mid P; P \mid P \mid P \mid P \mid Skip \mid \dots$



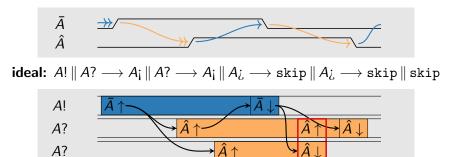
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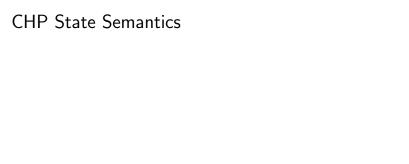


Channel
$$A := \langle \bar{A}, \hat{A} \rangle$$

Program $P := A! \mid A? \mid A_i \mid A_i \mid A_i \mid P; P \mid P \mid P \mid P \mid Skip \mid \dots$







$$\langle P, \sigma \rangle \longrightarrow_{s} \langle P', \sigma' \rangle$$
 or **error**

$$\langle P, \sigma \rangle \longrightarrow_{s} \langle P', \sigma' \rangle$$
 or **error**

$$\langle P, \sigma \rangle \longrightarrow_{s} \langle P', \sigma' \rangle$$
 or error

 σ is a mapping from each \bar{A} and \hat{A} to a Natural Number

 $\langle A!, \sigma \rangle \longrightarrow_{s}$

$$\langle P, \sigma \rangle \longrightarrow_s \langle P', \sigma' \rangle$$
 or **error**

$$\frac{\sigma(\hat{A}) = 0}{\langle A!, \sigma \rangle \longrightarrow_{s}}$$

$$\langle P, \sigma \rangle \longrightarrow_{s} \langle P', \sigma' \rangle$$
 or **error**

$$\frac{\sigma(\hat{A}) = 0 \qquad \sigma(\bar{A}) = n}{\langle A!, \sigma \rangle \longrightarrow_{s}}$$

$$\langle P, \sigma \rangle \longrightarrow_{s} \langle P', \sigma' \rangle$$
 or error

$$\frac{\sigma(\hat{A}) = 0 \quad \sigma(\bar{A}) = n}{\langle A!, \sigma \rangle \longrightarrow_{s} \langle A_{i}, \sigma[\bar{A} \mapsto n+1] \rangle}$$

$$\langle P, \sigma \rangle \longrightarrow_{s} \langle P', \sigma' \rangle$$
 or **error**

$$\frac{\sigma(\hat{A}) = 0 \quad \sigma(\bar{A}) = n}{\langle A!, \sigma \rangle \longrightarrow_{s} \langle A_{i}, \sigma[\bar{A} \mapsto n+1] \rangle}$$

$$\langle A_i, \sigma \rangle \longrightarrow_s$$

$$\langle P, \sigma \rangle \longrightarrow_{s} \langle P', \sigma' \rangle$$
 or **error**

$$\frac{\sigma(\hat{A}) = 0 \quad \sigma(\bar{A}) = n}{\langle A!, \sigma \rangle \longrightarrow_{s} \langle A_{i}, \sigma[\bar{A} \mapsto n+1] \rangle}$$

$$\frac{\sigma(\hat{A}) > 0}{\langle A_{\mathbf{i}}, \sigma \rangle \longrightarrow_{\mathbf{s}}}$$

$$\langle P, \sigma \rangle \longrightarrow_{s} \langle P', \sigma' \rangle$$
 or **error**

$$\frac{\sigma(\hat{A}) = 0 \quad \sigma(\bar{A}) = n}{\langle A!, \sigma \rangle \longrightarrow_{s} \langle A_i, \sigma[\bar{A} \mapsto n+1] \rangle}$$

$$\sigma(\hat{A}) > 0$$
 $\sigma(\bar{A}) = 1$ $\langle A_{i}, \sigma \rangle \longrightarrow_{s}$

$$\langle P, \sigma \rangle \longrightarrow_s \langle P', \sigma' \rangle$$
 or **error**

$$\frac{\sigma(\hat{A}) = 0 \quad \sigma(\bar{A}) = n}{\langle A!, \sigma \rangle \longrightarrow_{s} \langle A_{i}, \sigma[\bar{A} \mapsto n+1] \rangle}$$

$$rac{\sigma(\hat{A}) > 0 \quad \sigma(\bar{A}) = 1}{\langle A_{\mathsf{i}}, \sigma
angle \longrightarrow_{s} \langle \mathtt{skip}, \sigma[\bar{A} \mapsto 0]
angle}$$

CHP State Semantics

$$\langle P, \sigma \rangle \longrightarrow_{s} \langle P', \sigma' \rangle$$
 or **error**

 σ is a mapping from each \bar{A} and \hat{A} to a Natural Number

$$\frac{\sigma(\hat{A}) = 0 \quad \sigma(\bar{A}) = n}{\langle A!, \sigma \rangle \longrightarrow_{s} \langle A_{i}, \sigma[\bar{A} \mapsto n+1] \rangle}$$

$$rac{\sigma(\hat{A}) > 0 \quad \sigma(ar{A}) = 1}{\langle A_{ar{i}}, \sigma
angle \longrightarrow_s \langle ext{skip}, \sigma[ar{A} \mapsto 0]
angle}$$

$$\frac{\sigma(\hat{A}) > 0 \qquad \sigma(\bar{A}) > 1}{\langle A_{\mathbf{i}}, \sigma \rangle \longrightarrow_{s} \mathbf{error}}$$

CHP State Semantics

 $\langle A_i, \sigma \rangle \longrightarrow_{\epsilon} error$

$$\langle P, \sigma \rangle \longrightarrow_{s} \langle P', \sigma' \rangle$$
 or **error**

 σ is a mapping from each \bar{A} and \hat{A} to a Natural Number

$$\langle A_{\dot{c}}, \sigma \rangle \longrightarrow_{s} \text{error}$$

CHP State Semantics

$$\langle P, \sigma \rangle \longrightarrow_{s} \langle P', \sigma' \rangle$$
 or **error**

 σ is a mapping from each \bar{A} and \hat{A} to a Natural Number

$$\frac{\sigma(\hat{A}) = 0 \quad \sigma(\bar{A}) = n}{\langle A!, \sigma \rangle \longrightarrow_{s} \langle A_{i}, \sigma[\bar{A} \mapsto n+1] \rangle} \qquad \frac{\sigma(\bar{A}) > 0 \quad \sigma(\hat{A}) = n}{\langle A?, \sigma \rangle \longrightarrow_{s} \langle A_{i}, \sigma[\hat{A} \mapsto n+1] \rangle}$$

$$\frac{\sigma(\hat{A}) > 0 \quad \sigma(\bar{A}) = 1}{\langle A_{i}, \sigma \rangle \longrightarrow_{s} \langle \text{skip}, \sigma[\bar{A} \mapsto 0] \rangle} \qquad \frac{\sigma(\bar{A}) = 0 \quad \sigma(\hat{A}) = 1}{\langle A_{i}, \sigma \rangle \longrightarrow_{s} \langle \text{skip}, \sigma[\hat{A} \mapsto 0] \rangle}$$

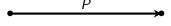
$$\frac{\sigma(\hat{A}) > 0 \quad \sigma(\bar{A}) > 1}{\langle A_{i}, \sigma \rangle \longrightarrow_{s} \text{error}} \qquad \frac{\sigma(\bar{A}) = 0 \quad \sigma(\hat{A}) > 1}{\langle A_{i}, \sigma \rangle \longrightarrow_{s} \text{error}}$$

. . .

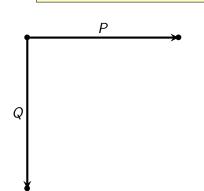
$\langle P, \sigma_0 \rangle \xrightarrow{?}_s^* \text{error}$

$\langle P \parallel Q \parallel R, \sigma_0 \rangle \stackrel{?}{\longrightarrow}_s^* \text{ error }$

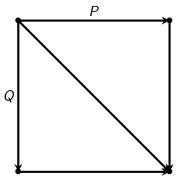
$$\langle P \parallel Q \parallel R, \sigma_0 \rangle \xrightarrow{?}_s^* \text{error}$$



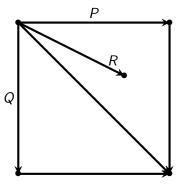
$$\langle P \parallel Q \parallel R, \sigma_0 \rangle \stackrel{?}{\longrightarrow}_s^* \text{ error}$$



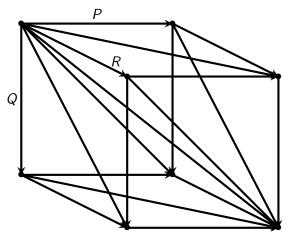
$\langle P \parallel Q \parallel R, \sigma_0 \rangle \stackrel{?}{\longrightarrow}_s^* \text{ error}$



$\langle P \parallel Q \parallel R, \sigma_0 \rangle \stackrel{?}{\longrightarrow}_s^* \text{error}$



$\langle P \parallel Q \parallel R, \sigma_0 \rangle \stackrel{?}{\longrightarrow}_s^* \text{ error}$



$\langle P \parallel Q \parallel R, \sigma_0 \rangle \stackrel{?}{\longrightarrow}_s^* \text{ error }$

$\langle P \parallel Q \parallel R, \sigma_0 \rangle \xrightarrow{?}_s^* \text{error}$

$$\langle P \parallel Q \parallel R, \sigma_0 \rangle \stackrel{?}{\longrightarrow}_s^* \text{ error }$$

$$\langle P \parallel Q \parallel R, \sigma_0 \rangle \xrightarrow{?}_s^* \text{error}$$

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2

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$$\langle P \parallel Q \parallel R, \sigma_0 \rangle \stackrel{?}{\longrightarrow}_s^* \text{error}$$

D

 \mathcal{Q}

R

$$\langle P \parallel Q \parallel R, \sigma_0 \rangle \stackrel{?}{\longrightarrow}_s^* \text{ error}$$

$$\langle P, \sigma \rangle \longrightarrow_{s} \dots$$

$$\langle Q, \sigma \rangle \longrightarrow_{s} \dots$$

$$\langle R, \sigma \rangle \longrightarrow_{s} \dots$$

$$\langle P \parallel Q \parallel R, \sigma_0 \rangle \stackrel{?}{\longrightarrow}_s^* \text{error}$$

$$\langle P, \sigma \rangle \longrightarrow_{s} \dots$$

$$\langle Q, \sigma \rangle \longrightarrow_{s} \dots$$

$$\langle R, \sigma \rangle \longrightarrow_{s} \dots$$

$$P \xrightarrow{L} P'$$

 $P \xrightarrow{L} P'$

Label L

$$P \xrightarrow{L} P'$$
 Label $L ::= idle$

$$P \xrightarrow{L} P'$$
 Label $L ::= idle \mid S$

$$P \xrightarrow{L} P'$$
 Label $L ::= idle \mid S \mid L \parallel L$

$$P \xrightarrow{L} P'$$
 Label $L ::= idle \mid S \mid L \parallel L \mid \dots$

$$P \xrightarrow{L} P'$$
Label $L ::= idle \mid S \mid L \parallel L \mid \dots$
Step $S ::= M_!^A \mid M_?^A$

$$P \xrightarrow{L} P'$$
Label $L ::= idle \mid S \mid L \parallel L \mid \dots$
Step $S ::= M_!^A \mid M_?^A$
Move $M ::= start \mid use \mid finish$

```
P \xrightarrow{L} P'
Label L ::= idle \mid S \mid L \mid L \mid ...
Step S ::= M_!^A \mid M_!^A
Move M ::= start \mid use \mid finish
\xrightarrow{A! \xrightarrow{start_!^A} A_!}
```

```
P \xrightarrow{L} P'
       Label L ::= idle | S | L || L | \dots
       Step S ::= M_1^A \mid M_2^A
     Move M ::= start | use | finish
   A! \xrightarrow{\mathsf{start}_!^A} A_i
A_i \xrightarrow{\text{finish}_1^A} \text{skip}
```

```
P \xrightarrow{L} P'
                                 Label L := idle \mid S \mid L \parallel L \mid \dots
                                  Step S ::= M_1^A | M_2^A
                                Move M ::= start | use | finish
A! \xrightarrow{\mathsf{idle}} A! \qquad A! \xrightarrow{\mathsf{start}_!^A} A_i
                          A_i \xrightarrow{\text{finish}_i^A} \text{skip}
```

$$P \xrightarrow{L} P'$$

$$Label L ::= idle | S | L || L | ...$$

$$Step S ::= M_!^A | M_!^A$$

$$Move M ::= start | use | finish$$

$$A! \xrightarrow{idle} A! \qquad A! \xrightarrow{start_!^A} A_i$$

$$A! \xrightarrow{use_!^A} A_i \qquad A_i \xrightarrow{finish_!^A} skip$$

$$P \xrightarrow{L} P'$$

$$Label \ L ::= idle \ | \ S \ | \ L \ | \ L \ | \ L \ | \$$

$$Step \ S ::= M_!^A \ | \ M_!^A$$

$$Move \ M ::= start \ | \ use \ | \ finish$$

$$\frac{.}{A! \xrightarrow{idle} A!} \xrightarrow{A!} A! \xrightarrow{A! \xrightarrow{start_!^A} A_!} A_! \xrightarrow{A! \xrightarrow{use_!^A} A_!} A? \xrightarrow{\frac{idle}{A!} A?} A? \xrightarrow{A : \xrightarrow{finish_!^A} skip} A;$$

$$A_! \xrightarrow{use_!^A} A_! \xrightarrow{A_!} A_! \xrightarrow{finish_!^A} skip \xrightarrow{A_! : use_!^A} A_! \xrightarrow{A_! : use_!^A} A_! \xrightarrow{A_! : use_!^A} skip$$

compliant(*L*) := traversable in hardware

$$\begin{array}{c}
P \xrightarrow{L} P' \\
\mathbf{compliant}(L) \\
\neg \mathbf{interferant}(L) \\
P \longrightarrow_{t} P'
\end{array}$$

$$\begin{array}{ccc} P \xrightarrow{L} P' & P \xrightarrow{L} P' \\ \textbf{compliant}(L) & \textbf{compliant}(L) \\ \hline \neg \textbf{interferant}(L) & \textbf{interferant}(L) \lor \dots \\ \hline P \longrightarrow_{t} P' & P \longrightarrow_{t} \textbf{error} \end{array}$$

$$\begin{array}{c}
P \xrightarrow{L} P' \\
\mathbf{compliant}(L) \\
\hline
\neg \mathbf{interferant}(L) \\
P \longrightarrow_{t} P'
\end{array}$$

$$P \xrightarrow{L} P'$$

$$\mathbf{compliant}(L)$$

$$\mathbf{interferant}(L) \lor \dots$$

$$P \longrightarrow_{t} \mathbf{error}$$

$$\begin{array}{ccc}
P \xrightarrow{L} P' & & P \xrightarrow{L} P' \\
 \text{compliant}(L) & & \text{compliant}(L) \\
 \hline
 P \longrightarrow_{t} P' & & \text{interferant}(L) \vee \dots \\
\hline
 P \longrightarrow_{t} \text{error}
\end{array}$$

$$A_i \parallel A_i \xrightarrow{\operatorname{use}_i^A \parallel \operatorname{finish}_i^A} A_i \parallel \operatorname{skip}$$

$$\begin{array}{ccc} P \xrightarrow{L} P' & P \xrightarrow{L} P' \\ \textbf{compliant}(L) & \textbf{compliant}(L) \\ \hline -\textbf{interferant}(L) & \textbf{interferant}(L) \lor \dots \\ \hline P \longrightarrow_{t} P' & P \longrightarrow_{t} \textbf{error} \end{array}$$

$$A_i \parallel A_i \xrightarrow{\operatorname{use}_i^A \parallel \operatorname{finish}_i^A} A_i \parallel \operatorname{skip} -\operatorname{compliant}(\operatorname{use}_i^A \parallel \operatorname{finish}_i^A)$$

$$\begin{array}{ccc}
P \xrightarrow{L} P' & & P \xrightarrow{L} P' \\
 \text{compliant}(L) & & \text{compliant}(L) \\
 \hline
 P \longrightarrow_{t} P' & & \text{interferant}(L) \vee \dots \\
\hline
 P \longrightarrow_{t} \text{error}
\end{array}$$

$$A_i \parallel A_i \xrightarrow{\operatorname{use}_i^A \parallel \operatorname{finish}_i^A} A_i \parallel \operatorname{skip}$$

$$\begin{array}{ccc}
P \xrightarrow{L} P' & & P \xrightarrow{L} P' \\
 \text{compliant}(L) & & \text{compliant}(L) \\
 \hline
 P \longrightarrow_{t} P' & & \text{interferant}(L) \vee \dots \\
\hline
 P \longrightarrow_{t} \text{error}
\end{array}$$

$$A_{i} \parallel A_{i} \xrightarrow{\text{finish}_{!}^{A} \parallel \text{use}_{?}^{A}} \text{skip} \parallel A_{i}$$

$$\begin{array}{ccc} P \xrightarrow{L} P' & P \xrightarrow{L} P' \\ \textbf{compliant}(L) & \textbf{compliant}(L) \\ \hline -\textbf{interferant}(L) & \textbf{interferant}(L) \lor \dots \\ \hline P \longrightarrow_{t} P' & P \longrightarrow_{t} \textbf{error} \end{array}$$

$$A_i \parallel A_i \xrightarrow{\text{finish}_1^A \parallel \text{use}_i^A} \text{skip} \parallel A_i \text{compliant}(\text{finish}_1^A \parallel \text{use}_i^A)$$

$$\begin{array}{ccc} P \xrightarrow{L} P' & P \xrightarrow{L} P' \\ \textbf{compliant}(L) & \textbf{compliant}(L) \\ \hline -\textbf{interferant}(L) & \textbf{interferant}(L) \lor \dots \\ \hline P \longrightarrow_{t} P' & P \longrightarrow_{t} \textbf{error} \end{array}$$

$$A_i \parallel A_i \xrightarrow{\text{finish}_1^A \parallel \text{use}_7^A} \text{skip} \parallel A_i \text{ compliant}(\text{finish}_1^A \parallel \text{use}_7^A)$$
 $\neg \text{interferant}(\text{finish}_1^A \parallel \text{use}_7^A)$

$$\begin{array}{ccc}
P \xrightarrow{L} P' & & P \xrightarrow{L} P' \\
 \text{compliant}(L) & & \text{compliant}(L) \\
 \hline
 P \longrightarrow_{t} P' & & \text{interferant}(L) \vee \dots \\
\hline
 P \longrightarrow_{t} \text{error}
\end{array}$$

$$A_{i} \parallel A_{i} \xrightarrow{\text{finish}_{!}^{A} \parallel \text{use}_{?}^{A}} \text{skip} \parallel A_{i}$$

$$\begin{array}{ccc}
P \xrightarrow{L} P' & & P \xrightarrow{L} P' \\
 \text{compliant}(L) & & \text{compliant}(L) \\
 \hline
 P \longrightarrow_{t} P' & & \text{interferant}(L) \vee \dots \\
 \hline
 P \longrightarrow_{t} \text{error}
\end{array}$$

$$A \c \parallel A \c \stackrel{\mathsf{finish}_?^A \parallel \mathsf{use}_?^A}{\longrightarrow} \mathsf{skip} \parallel A \c \parallel A \c \parallel$$

$$\begin{array}{ccc}
P \xrightarrow{L} P' & P' \\
\text{compliant}(L) & \text{compliant}(L) \\
\hline
-\text{interferant}(L) & \text{interferant}(L) \lor \dots \\
\hline
P \longrightarrow_{t} P' & P \longrightarrow_{t} \text{error}
\end{array}$$

$$A_{\xi} \parallel A_{\xi} \xrightarrow{\text{finish}_{\gamma}^{A} \parallel \text{use}_{\gamma}^{A}} \text{skip} \parallel A_{\xi}$$

$$\textbf{compliant}(\text{finish}_{\gamma}^{A} \parallel \text{use}_{\gamma}^{A})$$

$$\begin{array}{ccc}
P \xrightarrow{L} P' & & P \xrightarrow{L} P' \\
 \text{compliant}(L) & & \text{compliant}(L) \\
 \hline
 P \longrightarrow_{t} P' & & P \longrightarrow_{t} \text{error}
\end{array}$$

$$A_{\dot{\xi}} \parallel A_{\dot{\xi}} \xrightarrow{\text{finish}_{?}^{A} \parallel \text{use}_{?}^{A}} \text{skip} \parallel A_{\dot{\xi}}$$

$$\text{compliant}(\text{finish}_{?}^{A} \parallel \text{use}_{?}^{A})$$

$$\text{interferant}(\text{finish}_{?}^{A} \parallel \text{use}_{?}^{A})$$

$$\begin{array}{c}
P \xrightarrow{L} P' \\
\mathbf{compliant}(L) \\
\neg \mathbf{interferant}(L) \\
P \longrightarrow_{t} P'
\end{array}$$

$$P \xrightarrow{L} P'$$

$$\mathbf{compliant}(L)$$

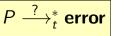
$$\mathbf{interferant}(L) \lor \dots$$

$$P \longrightarrow_{t} \mathbf{error}$$

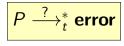
Semantics Equivalence



$$\langle P, \sigma_0 \rangle \longrightarrow_{\mathfrak{s}}^* \operatorname{error} \iff P \longrightarrow_t^* \operatorname{error}$$

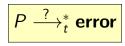








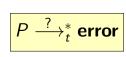
 ε_P





P ε_P

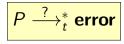
A!





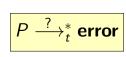
P ε_P

 $A! \qquad A! \xrightarrow{\mathsf{start}_!^A} A_i \xrightarrow{\mathsf{finish}_!^A} \mathsf{skip}$





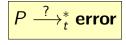
P	$arepsilon_{m{P}}$			
	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$			
A!	$A! \xrightarrow{q} A_i \xrightarrow{man} skip$			





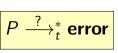
P ε_P

 $A! \qquad A! \xrightarrow{\mathsf{start}_!^A} A_i \xrightarrow{\mathsf{finish}_!^A} \mathsf{skip}$



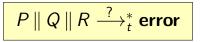


Р	$arepsilon_{m{P}}$		
<i>A</i> !	$A! \xrightarrow{start_!^A} A_i \xrightarrow{finish_!^A} skip$		
<i>A</i> ?	$A? \xrightarrow{start_?^A} A_{i:} \xrightarrow{finish_?^A} skip$		





Р	$arepsilon_{m{P}}$			
<i>A</i> !	$A! \xrightarrow{start_!^A} A_i \xrightarrow{finish_!^A} skip$			
<i>A</i> ?	$A? \xrightarrow{start_?^A} A_{\clip i} \xrightarrow{finish_?^A} skip$			
P; P	$\varepsilon_P \xrightarrow{idle} \varepsilon_{P'}$			
$P \parallel P'$	$\varepsilon_P imes \varepsilon_{P'}$			
*P	$\overbrace{\varsigma_{\mathcal{E}_{P}}}^{\text{idle}}$			



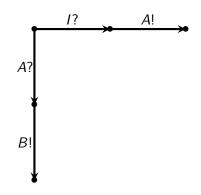


```
\varepsilon_P
                      A! \xrightarrow{\mathsf{start}_!^A} A_i \xrightarrow{\mathsf{finish}_!^A} \mathsf{skip}
A!
A? A? \xrightarrow{\text{start}_{?}^{A}} A_{i} \xrightarrow{\text{finish}_{?}^{A}} \text{skip}
                                  \varepsilon_P \xrightarrow{\mathsf{idle}} \varepsilon_{P'}
P; P
P \parallel P'
                                           \varepsilon_P \times \varepsilon_{P'}
*P
```

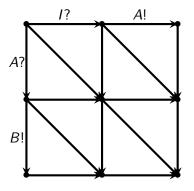
$$(I?;A!) \parallel (A?;B!) \parallel (B?;O!) \xrightarrow{?}_t^* \mathbf{error}$$

$$(I?;A!) \parallel (A?;B!) \parallel (B?;O!) \xrightarrow{?}_t^* \text{error}$$

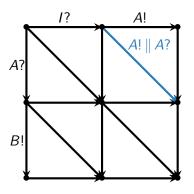
$$(I?;A!) \parallel (A?;B!) \parallel (B?;O!) \xrightarrow{?}_t^* \mathbf{error}$$



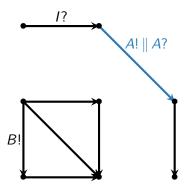
$$(I?;A!) \parallel (A?;B!) \parallel (B?;O!) \xrightarrow{?}_t^* \mathbf{error}$$



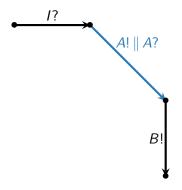
$$(I?;A!) \parallel (A?;B!) \parallel (B?;O!) \xrightarrow{?}_t^* error$$



$$(I?;A!) \parallel (A?;B!) \parallel (B?;O!) \xrightarrow{?}_t^* error$$

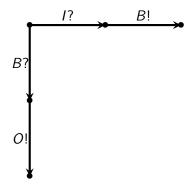


$$(I?;A!) \parallel (A?;B!) \parallel (B?;O!) \xrightarrow{?}_t^* \mathbf{error}$$

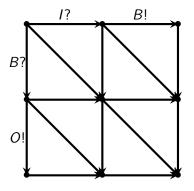


$$(I?;A!) \parallel (A?;B!) \parallel (B?;O!) \xrightarrow{?}_t^* \text{error}$$

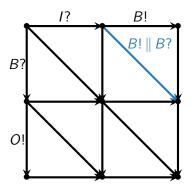
$$(I?;A!) \parallel (A?;B!) \parallel (B?;O!) \xrightarrow{?}_t^* \mathbf{error}$$



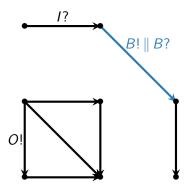
$$(I?;A!) \parallel (A?;B!) \parallel (B?;O!) \xrightarrow{?}_t^* error$$

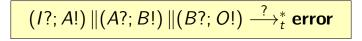


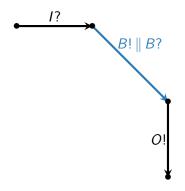
$$(I?;A!) \parallel (A?;B!) \parallel (B?;O!) \xrightarrow{?}_t^* \mathbf{error}$$



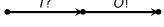
$$(I?;A!) \parallel (A?;B!) \parallel (B?;O!) \xrightarrow{?}_t^* \mathbf{error}$$



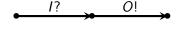




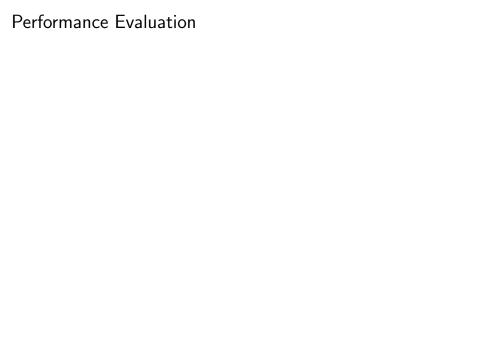
$$(I?;A!) \parallel (A?;B!) \parallel (B?;O!) \xrightarrow{?}_t^* \text{error}$$

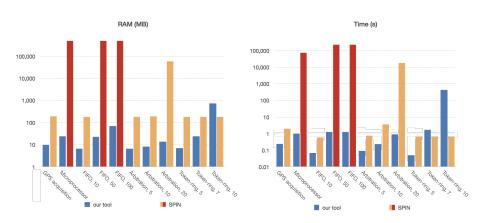


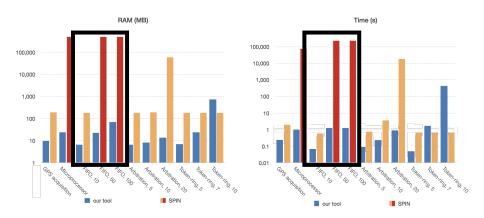
$$(I?;A!) \parallel (A?;B!) \parallel (B?;O!) \xrightarrow{?}_t^* error$$

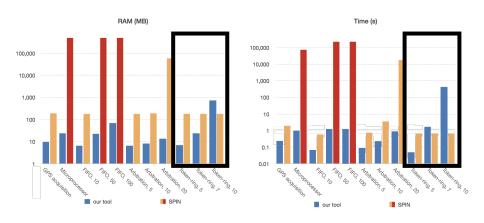


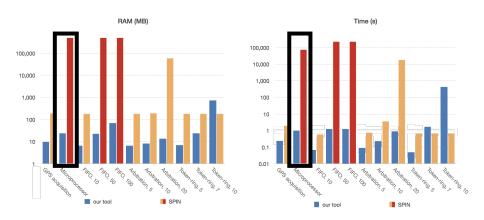
3 states vs. 27 states

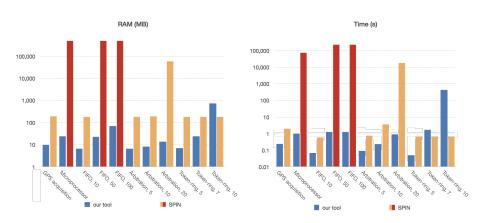












☑ CHP Trace Semantics

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 $\ \ \square$ Inferable Effect System

☑ CHP Trace Semantics

✓ Inferable Effect System

 $\hfill\Box$ include data in semantics proof of equivalence

☑ CHP Trace Semantics

✓ Inferable Effect System

☐ include data in semantics proof of equivalence

□ verify tool

- ☑ CHP Trace Semantics
- ✓ Inferable Effect System

- ☐ include data in semantics proof of equivalence
- □ verify tool
- \square explore other aspects of CHP design process

Thank you! Questions?