

## Summary

This unit introduced  $n$ -grams as a fundamental concepts of computational and theoretical linguistics alike.

- A negative  $n$ -gram grammar is a set of  $n$ -grams.
  - A string is well-formed iff it does not contain any forbidden  $n$ -grams.
  - An  $n$ -gram grammar is fixed if all  $n$ -grams have the same length, and mixed otherwise.
- Every negative  $n$ -gram grammar has an equivalent positive  $n$ -gram grammar, and the other way round.
- Positive grammars must be fixed.
- Multiple grammars can be combined into a single grammar.
  - Negative grammars: union of sets
  - Positive grammars: intersection of sets
- Whereas an  $n$ -gram grammar is a set, a bag-of-words model is a multiset.
  - The multiset counts for each word type its number of word tokens.
  - Multiset sum and scalar multiplication can be used to combine and modify counts.
- Due to Zipf's law, a small number of words make up the majority of each text.
- The function  $\text{del}_s$  removes all stop words.
- Mathematically, this is the same as constructing phonological tiers.
- Tiers make it possible to handle long-distance dependencies in an elegant fashion with much smaller grammars.

## Some additional terminology

We now have two types of  $n$ -gram grammars: those that regulate strings, and those that regulate tiers. The former are commonly referred to as **strictly local** (SL) grammars, whereas the latter are **tier-based strictly local** (TSL). A TSL grammar consists of both an SL grammar  $G$  and a set  $T$  of tier symbols. A string  $s$  is well-formed with respect to the TSL grammar iff  $\text{del}_{+T}(s)$  is well-formed with respect to  $G$ .

By default SL and TSL grammars are negative, but positive counterparts can be defined as usual.