ASSIGNMENT 4 — KINEMATICS AND DYNAMICS

For all questions below, provide all programming code and plots in the report.

Kinematics

- 1. For a 1-link arm, assume $l=0.46(m), \theta=60^{\circ}, \dot{\theta}=2(rads/s), \ddot{\theta}=1(rads/s^2)$. Use Python (or other program) to calculate (3 marks):
 - a. Hand Position. 1 mark
 - b. Hand Velocity. 1 mark
 - c. Hand Acceleration. 1 mark
 - d. Note: make sure you work through taking the derivates by hand to find $J(\theta)$ and $\dot{J(\theta)}$
- 2. Using your calculations from 1a, 1b, and 1c, use inverse kinematics to retrieve (3 marks):
 - a. Joint Angle (deg). 1 mark
 - b. Angular Velocity (rad/s). 1 mark
 - c. Angular Acceleration (rad/s^2) . 1 mark
- 3. For a 2-link arm, assume $l_1 = 0.34$, $l_2 = 0.46$, $H_x = 0.36$, $H_y = 0.65$, $\dot{H}_x = -3.89$, $\dot{H}_y = 1.30$, $\ddot{H}_x = -7.79$, $\ddot{H}_y = -26.18$. Use Python (or other program) to calculate (**Graduate Only**) (4 marks):
 - a. Joint Angle (deq). 2 marks
 - b. Angular Velocity (rad/s). 1 marks
 - c. Angular Acceleration (rad/s^2) . 1 mark
 - d. Note: make sure you work through taking the derivates by hand to find $J(\theta)$ and $\dot{J(\theta)}$

Dynamics

- 4. For a 1-link arm (2 marks):
 - a. Derive the equations of motion by hand using Lagrange mechanics and show your work. 1 mark
 - b. Convert this second-order system into two, first-order ODEs and show your work. 1 mark.
- 5. For your derived 1-link arm model (4 marks):
 - a. Run a forward simulations using Euler integration and plot the states over time. Simulation time = 10 seconds, time step (h) = 0.0001s. Constants = $m(1.65kg), r(0.5m), g(9.81), \mathcal{I}(0.025)$; Initial Conditions = $\theta = 90$; $\dot{\theta} = 0$. 1 mark
 - b. Run a forward simulation using odeint (or ode45) and plot the states over time. Same constants and initial conditions as above, but with h = 0.001s. 1 mark
 - c. Plot the linear kinetic energy (T^{lin}) , rotational kinetic energy (T^{rot}) , potential energy (U), and the total energy (T+U) over time for the simulation above. 1 mark.
 - d. What do you notice with the energy terms? Why would this be? 1 mark.
- 6. For a 2-link arm (**Graduate Only**) (4 marks):
 - a. Run a forward simulation a two-link arm using odeint (or ode45), using the equations of motion defined in class, and plot the states over time. Sim time = 4 s, time step (h) = 0.001s.

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Constants = m_1(2.1), m_2(1.65), \mathcal{I}_1(0.025), \mathcal{I}_2(0.075), l_1(0.3384), l_2(0.4554), r_1(0.1692), r_2(0.2277), g(9.81), Q_1(0), Q_2(0)
Initial Conditions = \theta_1(180^\circ), \theta_2(1^\circ), \dot{\theta}_1(0^{\circ/s}), \dot{\theta}_2(0^{\circ/s}). 3 mark.
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b. Plot the kinetic energy (i.e., T, sum of the kinetic energy terms), potential energy (U, sum of the potential energy terms), and total energy (T+U) over time for the simulation above. 1 mark.

