STAT-511 2018 Spring

Lecture 7: Model Selection

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## 7.1 Criteria: AIC

Goal: Find the model that gives the best prediciton without assuming the any candidate model is correct.

**Setup:** Suppose  $x_i \stackrel{iid}{\sim} f_{\theta}$  and the candidate set is  $\mathcal{M} = \{M_j | j = 1, 2, ..., n\}$  where  $M_j = \{p_{\theta_j}(x); \theta_j \in \Theta_j\}$ . We wan to minimize the loss

$$\min_{j} KL(f_{\theta}||\hat{p_{\theta_{j}}}) = \int (f_{\theta} \log f_{\theta} - f_{\theta} \log \hat{p_{\theta_{j}}}) d\theta,$$

where  $\hat{p_{\theta_j}}$  is an estimate of  $p_{\theta_j}$   $(\hat{p_{\theta_j}} = p_{\hat{\theta_j}})$ . This is equivalent to

$$\min_{j} - \int f_{\theta} \log p \hat{\theta}_{j} d\theta.$$

A good estimator of  $\int f_{\theta} \log \hat{p_{\theta_i}} d\theta$  is

$$\bar{K}_j = \frac{1}{n} \sum_{i} \log p \hat{\theta}_j.$$

## 7.2 Criteria: BIC