1.
$$2x(1+\sqrt{x^2-y}) dx - \sqrt{x^2-y} dy = 0.$$

2.
$$y' - \frac{y}{x} = 3x^3$$
.

3.
$$xyy' = 4x^2 + y^2$$
.

4.
$$xy' + y = -xy^2$$
.

5.
$$xy' + y = \ln x + 1$$
, $y(2) = 1$.

6.
$$x^2y' + 3xy = \frac{1}{x}$$
, $y(1) = -1$.