

Answer 2 -

Basic idea -

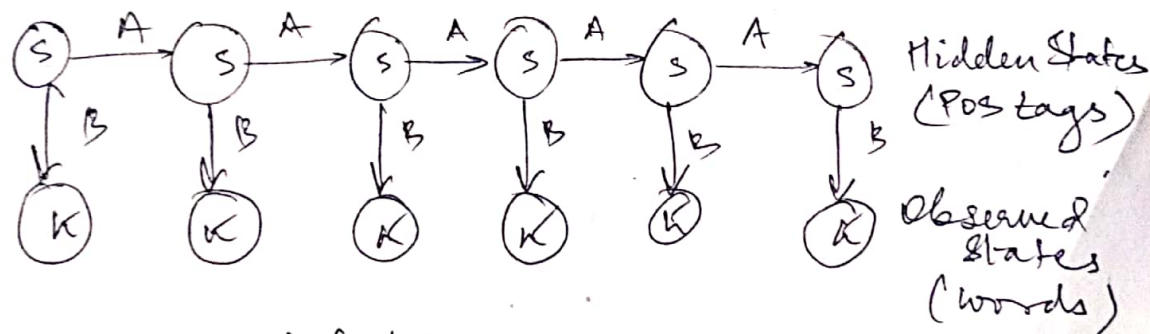
$$P(t|w) = \frac{P(w|t) \times P(t)}{P(w)}$$

$$P(w_1, w_2, \dots, w_n) = P(w_1) \prod_{i=2}^n P(w_i | w_1, \dots, w_{i-1})$$

For 2 assumption length \rightarrow

$$P(w_1, w_2, \dots, w_n) \approx P(w_1) \cdot P(w_2 | w_1) \prod_{i=2}^{n-1} P(w_{i+1} | w_i, w_{i-1})$$

$$P(w_i | w_{i-2}, w_{i-1}) = \frac{\text{count}(w_{i-2}, w_{i-1}, w_i)}{\text{count}(w_{i-2}, w_{i-1})}$$



Transition probability \rightarrow

For every transition $S_j \rightarrow S_k$, transition probability $P(S_k | S_j)$ is present.

Emission Probability \rightarrow

For every state S_k and every word w_i , we have an emission probability $P(w_i | S_k)$ (implementing $P(w_i | t_i)$)

The probabilities are calculated using log probabilities and optimized data structures such as dictionary are used for every tag set.

The columns contain both w_{i-1}, w_{i-2} for w_i calculation and hence shows trigram model through dependencies on previous two words.

Start and stop symbols - '*' and 'STOP' are added and then the starting probabilities are calculated, the transition - prior probabilities are also taken into account.

Also \rightarrow

$$p(x_1, x_2, \dots, x_n, y_1, y_2, \dots, y_{n+1}) \\ = \prod_{i=1}^{n+1} q(y_i | y_{i-2}, y_{i-1}) \cdot \prod_{i=1}^n e(x_i | y_i)$$

K = set of possible tags. $K_{-1} = K_0 = \{*\}$
and $K_k = K$ for $k = 1, 2, \dots, n$

Initialization $\rightarrow \pi(0, *, *) = 1$

Algorithm \rightarrow

- For $k = 1, \dots, n$

- For $u \in K_{k-1}, v \in K_k,$

$$\pi(k, u, v) = \max_{w \in K_{k-2}} (\pi(k-1, w, u) \\ \times q(v | w, u) \\ \times e(x_k | v))$$

- Return $\max_{u \in K_{n-1}, v \in K_n} (\pi(n, u, v) \\ \times q(\text{STOP} | u, v))$

Basic Viterbi