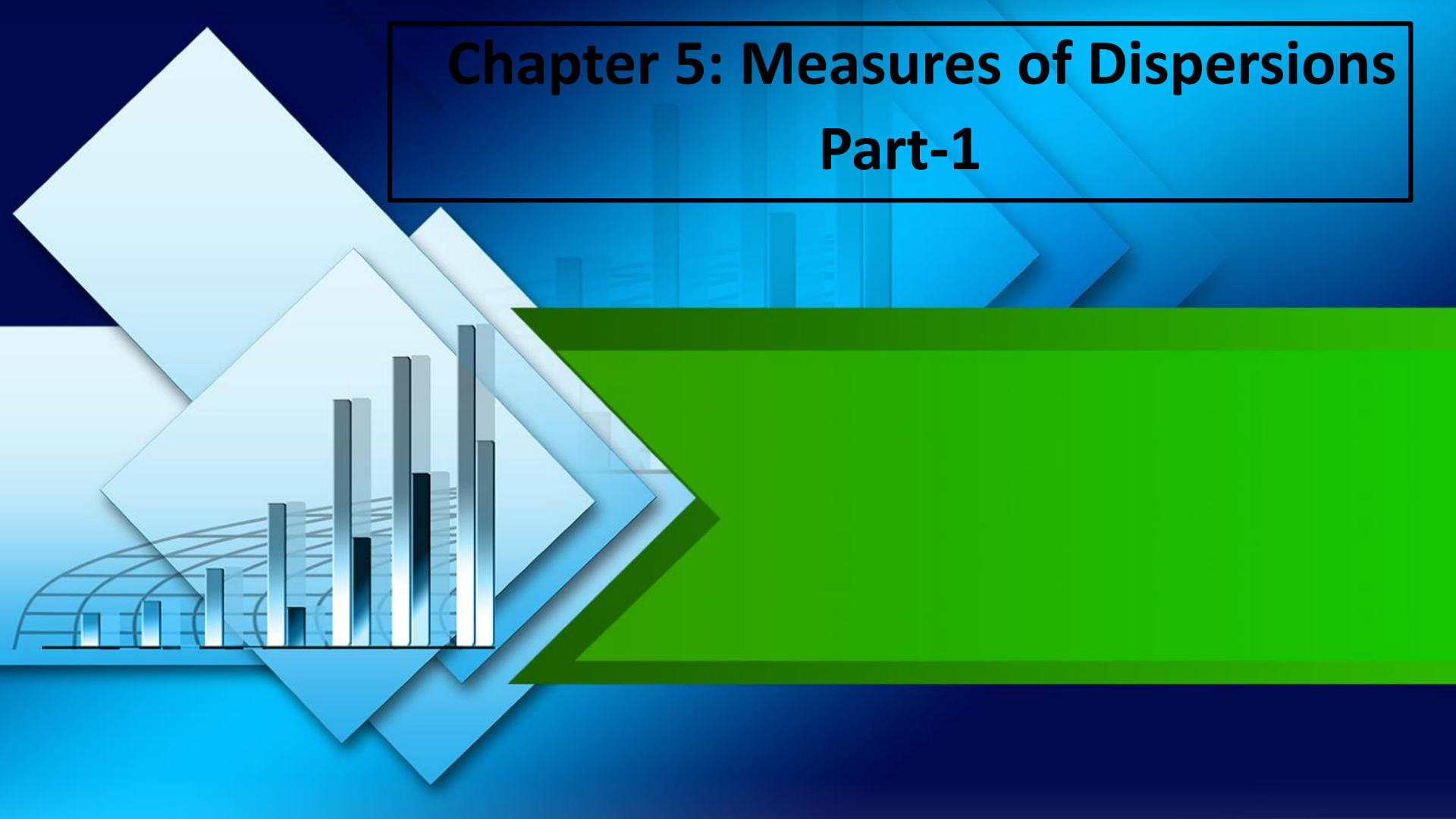


Chapter 5: Measures of Dispersions

Part-1





Learning Outcomes

After Completing the chapter ,you will able to know :

- ☐ How to measure spreadness of data values by calculating dispersion.
- ☐ Different types of measures of Dispersion with their application and limitations.



Contents

From this lecture, you are going to learn...

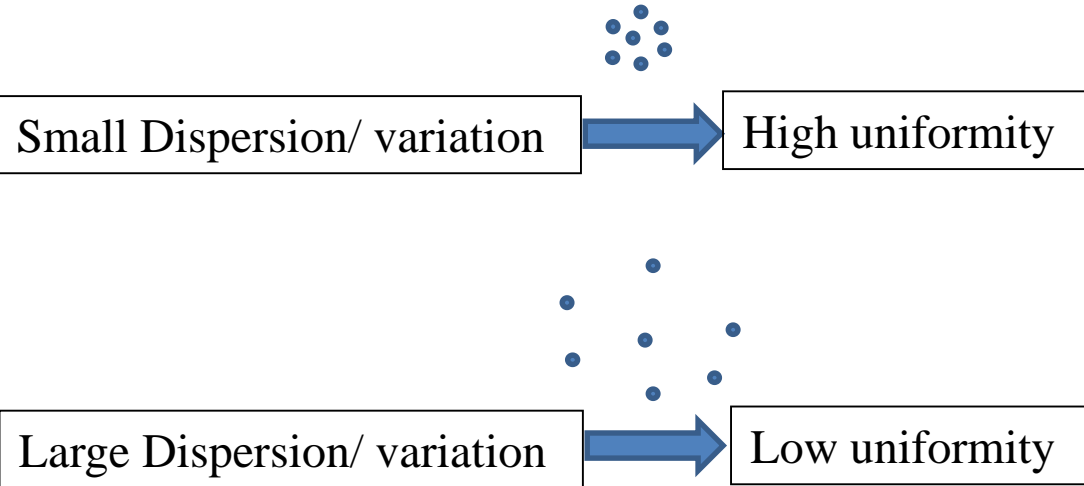
- What is dispersion?
- Discussion on Range, Mean deviation, Population variance and standard deviation.
- Examples, Uses and limitations

What is measures of Dispersion?

Dispersion measures the spread or variability of a set of observations among themselves or about some central values.

Example: **Group-1**
Marks of 4 students out of 100.
50, 49, 51, 50.
Mean = 50

Example: **Group-2**
Marks of 4 students out of 100.
100, 100, 0, 0.
Mean = 50



Types of measures of dispersion

Measures of Dispersion

Absolute measures

1. Range
2. Mean Deviation
3. Variance
4. Standard deviation($\sqrt{\text{Variance}}$)
5. Quartile deviation

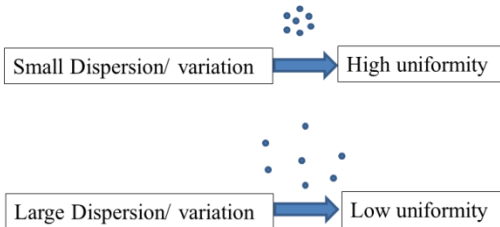
Relative measures

1. Coefficient of Range
2. Coefficient of Mean Deviation
3. Coefficient of Variation(c.v.)
4. Coefficient of Quartile deviation

Purpose of Studying Dispersion

Example: **Group-1**
Marks of 4 students out of 100.
50, 49, 51, 50.
Mean = 50

Example: **Group-2**
Marks of 4 students out of 100.
100, 100, 0, 0.
Mean = 50



Purposes of measures of dispersions:

- To measure the spread of the data set.
- To determine the reliability of an average.
- To compare two or more data sets according to their variability.



1. Range: Simplest measure of dispersion is the range.

$$\text{Range} = \text{Largest value} - \text{Smallest value}$$

Example: suppose the marks of 8 students in a class are: 65, 20, 55, 80, 42, 35, 77, 68.
Calculate Range.

Solution:

$$R = X_{\max} - X_{\min}$$

$$R = 80 - 20 = 60$$

Limitation:

Range cannot tell us anything about the character of the distribution within two extreme observations

Example of Range

Average run of Batsman A = 36.73

The variation of the run of Batsman A = $86 - 10 = 76$



20	35	22	55	60
10	17	32	64	86
14	32	50	24	30

Average run of Batsman B = 43.4

The variation of the run of Batsman B = $370 - 0 = 370$



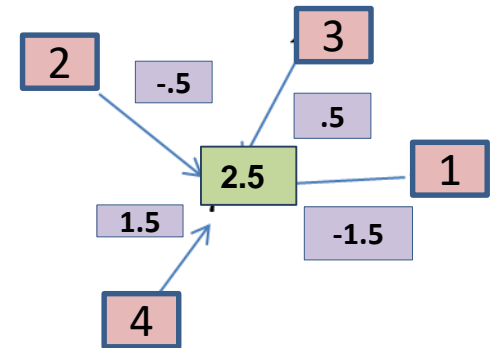
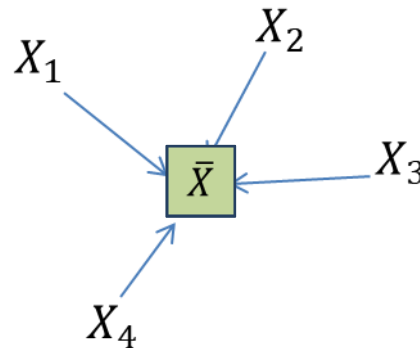
0	0	0	2	0
15	5	370	250	
0	3	5	0	1

Mean deviation

Mean Deviation: The average of the absolute values of the deviations from the average of the data.

Mean deviation is obtained by calculating the absolute deviations of each observation from mean and then averaging these deviations by taking arithmetic mean.

Formula:
$$M.D. = \frac{\sum_{i=1}^n |X_i - \bar{X}|}{n}$$
$$= \frac{|X_1 - \bar{X}| + |X_2 - \bar{X}| + \dots + |X_n - \bar{X}|}{n}$$



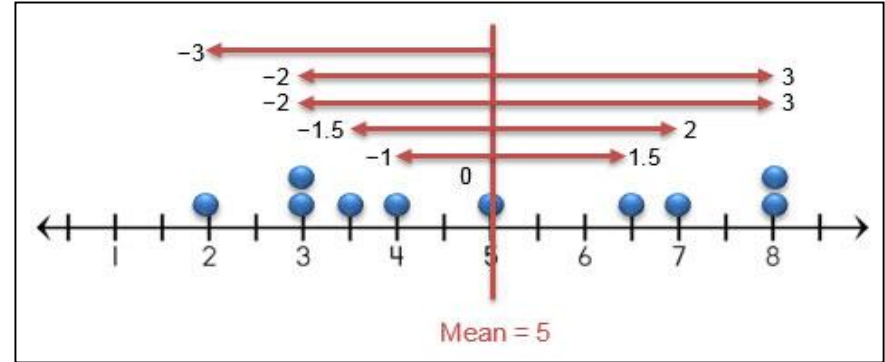
Example of Mean deviation

Example:

Find the Mean Deviation of data values are 2, 3, 3, 3.5, 4, 5, 6.5, 7, 8, 8.

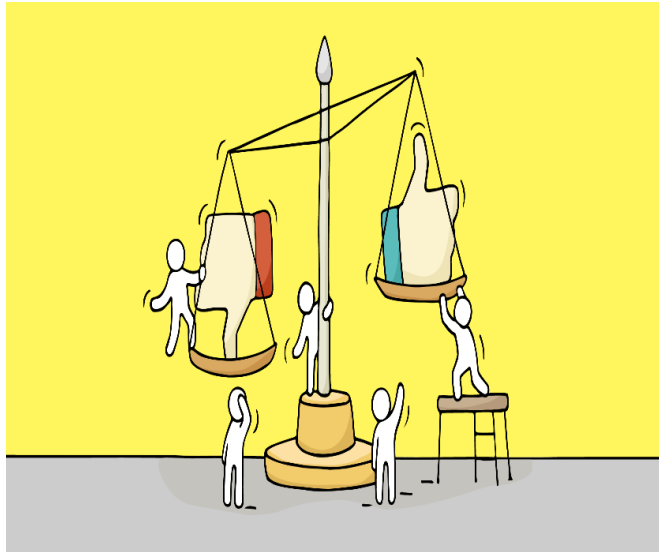
$$\text{Now, mean, } \bar{X} = \frac{2+3+3+3.5+4+5+6.5+7+8+8}{10} = 5$$

X_i	$X_i - \bar{X}$	$ X_i - \bar{X} $
2	-3	3
3	-2	2
3	-2	2
3.5	-1.5	1.5
4	-1	1
5	0	0
6.5	1.5	1.5
7	2	2
8	3	3
8	3	3
Total		$\sum_{i=1}^n X_i - \bar{X} = 19$



$$\therefore \text{M.D.} = \frac{\sum_{i=1}^n |X_i - \bar{X}|}{n} = \frac{19}{10} = 1.9.$$

Merits and limitations of Mean Deviation



Merits:

Less affected by the values of extreme observation.

limitations:

The greatest limitation of this method is that algebraic signs are ignored while taking the deviations of the items.

Population Variance and Standard Deviation

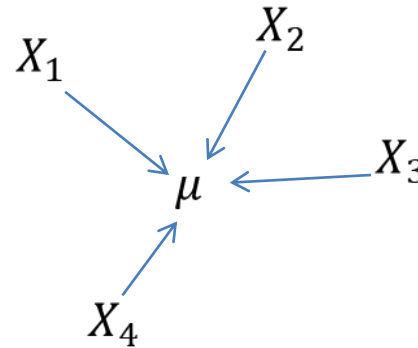
Population variance,

$$\sigma^2 = \frac{\sum_{i=1}^N (X_i - \mu)^2}{N}$$
$$= \frac{(X_1 - \mu)^2 + (X_2 - \mu)^2 + \dots + (X_N - \mu)^2}{N}$$

∴ Population Standard deviation,

$$\sigma = \sqrt{\frac{\sum_{i=1}^N (X_i - \mu)^2}{N}}$$
$$= \sqrt{\frac{(X_1 - \mu)^2 + (X_2 - \mu)^2 + \dots + (X_N - \mu)^2}{N}}$$

Where X_1, X_2, \dots, X_N are Population observation
 N = Population size.
 μ = Population mean





Example of Population Variance and Standard Deviation

Example: Calculate the population variance and standard deviation for the data set 1, 2, 2, 3, 4, 5.

Solution:

Population variance,

$$\sigma^2 = \frac{\sum_{i=1}^N (X_i - \mu)^2}{N}$$

$$\begin{aligned}\text{Where, Population Mean, } \mu &= \frac{\sum_{i=1}^N X_i}{N} \\ &= \frac{1+2+2+3+4+5}{6} \\ &= 2.83\end{aligned}$$

$$\therefore \sigma^2 = \frac{(1-2.83)^2 + (2-2.83)^2 + \dots + (5-2.83)^2}{6}$$

$$= \frac{10.84}{6} = 1.81$$

$$\therefore \text{Population standard deviation, } \sigma = \sqrt{1.81} = 1.35$$



Exercise of Population Variance and Standard Deviation

Exercise:

Set A: 18, 25, 10, 12.

Set B: 32, 30, 20, 10.

Find population standard deviation and compare the variability between these two data sets.

****Hints:** Find Standard deviation for both the data. Then the data set with lower standard deviation will have higher uniformity.



*Thank
you*

