

2528. Maximize the Minimum Powered City

Solved 

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You are given a **0-indexed** integer array `stations` of length `n`, where `stations[i]` represents the number of power stations in the i^{th} city.

Each power station can provide power to every city in a fixed **range**. In other words, if the range is denoted by `r`, then a power station at city `i` can provide power to all cities `j` such that $|i - j| \leq r$ and $0 \leq i, j \leq n - 1$.

- Note that $|x|$ denotes **absolute** value. For example, $|7 - 5| = 2$ and $|3 - 10| = 7$.

The **power** of a city is the total number of power stations it is being provided power from.

The government has sanctioned building `k` more power stations, each of which can be built in any city, and have the same range as the pre-existing ones.

Given the two integers `r` and `k`, return the **maximum possible minimum power** of a city, if the additional power stations are built optimally.

Note that you can build the `k` power stations in multiple cities.

Example 1:

Input: `stations = [1,2,4,5,0]`, `r = 1`, `k = 2`

Output: 5

Explanation:

One of the optimal ways is to install both the power stations at city 1. So `stations` will become `[1,4,4,5,0]`.

- City 0 is provided by $1 + 4 = 5$ power stations.
- City 1 is provided by $1 + 4 + 4 = 9$ power stations.
- City 2 is provided by $4 + 4 + 5 = 13$ power stations.
- City 3 is provided by $5 + 4 = 9$ power stations.
- City 4 is provided by $5 + 0 = 5$ power stations.

So the minimum power of a city is 5.

Since it is not possible to obtain a larger power, we return 5.

Example 2:

Input: `stations = [4,4,4,4]`, `r = 0`, `k = 3`

Output: 4

Explanation:

It can be proved that we cannot make the minimum power of a city greater than 4.

Constraints:

- `n == stations.length`
- `1 <= n <= 105`
- `0 <= stations[i] <= 105`
- `0 <= r <= n - 1`
- `0 <= k <= 109`

Python:

class Solution:

def maxPower(self, stations: List[int], r: int, k: int) -> int:

n = len(stations)

left, right = 0, k + sum(stations)

while left <= right:

 x = (left + right) // 2

 use = 0

 # v is the stations after adding

 v = stations.copy()

 # s means the power of city i

 # at first, it record the sum of v[0,r)

 s = sum(stations[0: r])

 for i in range(n):

 # add to t if needed

 t = n - 1 if n - 1 < i + r else i + r

 # update s

 # find a city should be added

 if i + r < n: s += v[i+r]

 # find a city should be removed

 if i - r > 0: s -= v[i-r-1]

 # missing power stations

 diff = x - s if x - s > 0 else 0

 v[t] += diff

 s += diff

 use += diff

 if use <= k:

 left = x + 1

 else:

```
    right = x - 1
    return right
```

JavaScript:

```
/**
 * @param {number[]} stations
 * @param {number} r
 * @param {number} k
 * @return {number}
 */
var maxPower = function (stations, r, k) {
    const n = stations.length;
    const cnt = new Array(n + 1).fill(0);

    for (let i = 0; i < n; i++) {
        const left = Math.max(0, i - r);
        const right = Math.min(n, i + r + 1);
        cnt[left] += stations[i];
        cnt[right] -= stations[i];
    }

    const check = (val) => {
        const diff = [...cnt];
        let sum = 0;
        let remaining = k;

        for (let i = 0; i < n; i++) {
            sum += diff[i];
            if (sum < val) {
                const add = val - sum;
                if (remaining < add) {
                    return false;
                }
                remaining -= add;
                const end = Math.min(n, i + 2 * r + 1);
                diff[end] -= add;
                sum += add;
            }
        }
        return true;
    };

    let lo = Math.min(...stations);
    let hi = stations.reduce((a, b) => a + b, 0) + k;
```

```

let res = 0;

while (lo <= hi) {
    const mid = Math.floor(lo + (hi - lo) / 2);
    if (check(mid)) {
        res = mid;
        lo = mid + 1;
    } else {
        hi = mid - 1;
    }
}
return res;
};

```

Java:

```

class Solution {
    public long maxPower(int[] stations, int r, int k) {
        int n = stations.length;
        long left = 0, right = k;
        for (int x: stations)
            right += x;
        // v is the stations after adding
        long []v = new long[n];
        while (left <= right) {
            long x = (left + right) / 2;
            for (int i = 0; i < n; ++i)
                v[i] = stations[i];
            // s means the power of city i
            // at first, it record the sum of v[0,r)
            long s = 0, use = 0;
            for (int i = 0; i < r; ++i)
                s += v[i];
            for (int i = 0; i < n; ++i) {
                // add to t if needed
                int t = Math.min(n - 1, i + r);
                // update s
                // find a city should be added
                if (i + r < n) s += v[i + r];
                // find a city should be removed
                if (i - r > 0) s -= v[i - r - 1];
                // missing power stations
                long diff = Math.max(0, x - s);
                v[t] += diff;
                s += diff;
            }
        }
    }
}

```

```
        use += diff;
    }
    if (use <= k) left = x + 1;
    else right = x - 1;
}
return right;
}
}
```