

3623. Count Number of Trapezoids I

Solved

Medium

Topics

Companies

Hint

You are given a 2D integer array `points`, where `points[i] = [xi, yi]` represents the coordinates of the i^{th} point on the Cartesian plane.

A **horizontal trapezoid** is a convex quadrilateral with **at least one pair** of horizontal sides (i.e. parallel to the x-axis). Two lines are parallel if and only if they have the same slope.

Return the *number of unique horizontal trapezoids* that can be formed by choosing any four distinct points from `points`.

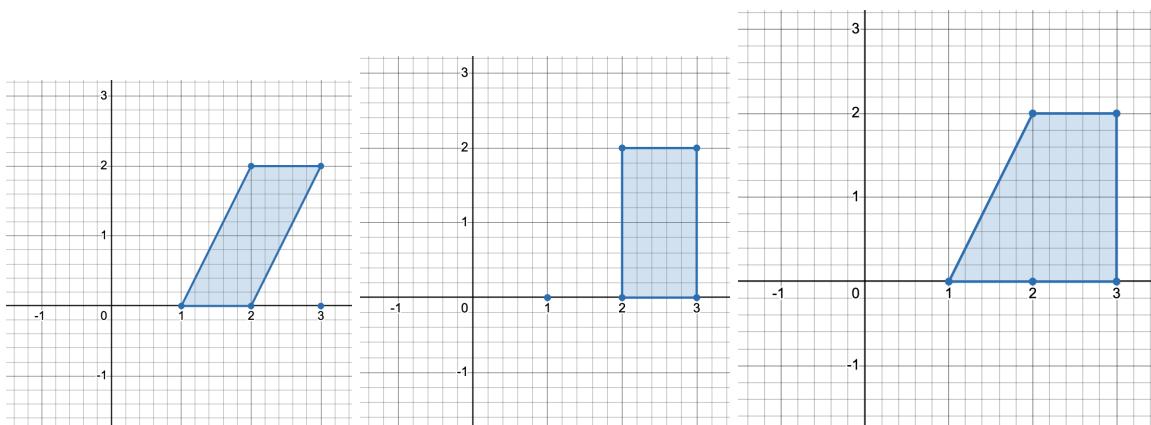
Since the answer may be very large, return it **modulo** $10^9 + 7$.

Example 1:

Input: `points = [[1,0],[2,0],[3,0],[2,2],[3,2]]`

Output: 3

Explanation:



There are three distinct ways to pick four points that form a horizontal trapezoid:

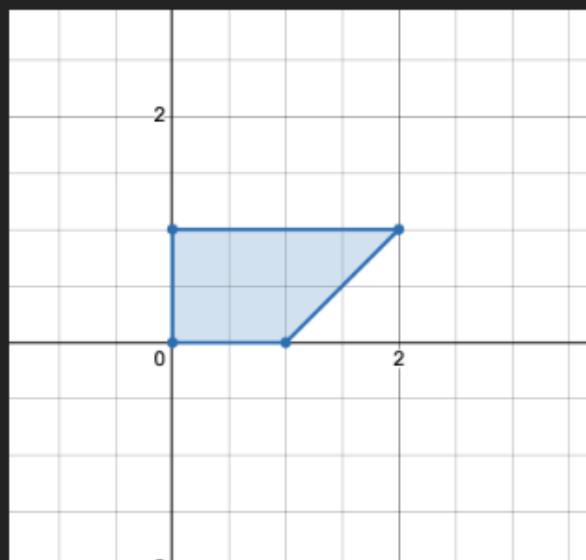
- Using points $[1, 0]$, $[2, 0]$, $[3, 2]$, and $[2, 2]$.
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Example 2:

Input: points = $[[0, 0], [1, 0], [0, 1], [2, 1]]$

Output: 1

Explanation:



There is only one horizontal trapezoid that can be formed.

Constraints:

- $4 \leq \text{points.length} \leq 10^5$
- $-10^8 \leq x_i, y_i \leq 10^8$
- All points are pairwise distinct.

Python:

```
class Solution:  
    def countTrapezoids(self, points: List[List[int]]) -> int:  
        MOD = 1000000007  
        groups = defaultdict(int)  
        for _, y in points:  
            groups[y] += 1  
        res = total = 0  
        for y, count in groups.items():  
            lines = count * (count - 1) // 2  
            res = (res + total * lines) % MOD  
            total = (total + lines) % MOD  
        return res
```

JavaScript:

```
/**  
 * @param {number[][]} points  
 * @return {number}  
 */  
var countTrapezoids = function(points) {  
    const MOD = 1000000007n;  
    const cnt = new Map();  
    for (const p of points) {  
        const y = p[1];  
        cnt.set(y, (cnt.get(y) || 0n) + 1n);  
    }  
    const seg = [];  
    for (const k of cnt.values()) {  
        if (k >= 2n) seg.push(k * (k - 1n) / 2n);  
    }  
}
```

```

let sum = 0n, ans = 0n;
for (const v of seg) {
    ans = (ans + v * sum) % MOD;
    sum = (sum + v) % MOD;
}
return Number(ans);
};

```

Java:

```

class Solution {
    public int countTrapezoids(int[][] points) {
        int n = points.length, MOD = 1000000007;
        Arrays.sort(points, Comparator.comparingInt(a -> a[1]));
        long res = 0, total = 0;
        for (int i = 0, j; i < n; i = j){
            j = i + 1;
            while (j < n && points[i][1] == points[j][1]){
                j++;
            }
            long count = j - i;
            long lines = count * (count - 1) / 2;
            res = (res + total * lines) % MOD;
            total = (total + lines) % MOD;
        }
        return (int)res;
    }
}

```