



Linear Algebra

Laboratory Activity No. 8

System of Linear Equations

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I. Objectives

This laboratory activity aims to implement the principles and techniques of solving linear equations using the various linear algebra techniques and to solve a system of equations using Python programming.

II. Methods

The practices of the activity include working around with the system of linear equations using Python programming. This activity implies and teaches the various algebra techniques in solving linear equations. Moreover, the deliverables of the activity are to provide an equation and solve it using the NumPy functions. Lastly, it was achieved by creating a scenario and represent it in a matrix then solve using Python programming and NumPy function.

III. Results

The results from solving a system of linear equations from the scenario created using the linear equation and the `np.linalg.solve()` function from NumPy are presented in this section.

$$A = \begin{cases} 6a + 4b + 3c = 30000 \\ 2a + 2b + 3c = 18000 \\ 4a + 2b + 1c = 15000 \end{cases}$$

Figure 1 System of linear equation

Figure 1 shows the system of linear equation formed from the created scenario which is the “I and my brother have a collection of anime figurines and I created a list for our current figurines and the one that is still currently in a pre-ordered state. In total, we currently have 6 nendoroids, 4 Figma, and 3 pop up parade. This cost us a total of 30,000. Meanwhile, the current figurines we pre-ordered that will be released in the future are 2 nendoroids, 2 figma, and 3 pop up parade, for a total of 18,000. I am still waiting for the other re-release of the figures I failed to acquire. Those are 4 nendoroids, 2 Figma, and 1 pop up parade which will be about 15,000.” This was presented in matrix form afterward to solve it using Python programming.

```

: #1
  ## quantitiesprices = cost
  quantities = np.array([
    [6,4,3],
    [2,2,3],
    [4,2,1]
  ])
  cost = np.array([
    [30000],
    [18000],
    [15000]
  ])

: prices = np.linalg.inv(quantities) @ cost

print('The price of nendoroids is: PHP {:.2f}'.format(float(prices[0])))
print('The price of figma: PHP {:.2f}'.format(float(prices[1])))
print('The price of pop up parade: PHP {:.2f}'.format(float(prices[2])))

The price of nendoroids is: PHP 1500.00
The price of figma: PHP 3000.00
The price of pop up parade: PHP 3000.00

```

Figure 2 The code and output

Figure 2 shows the code created for solving a linear equation using the inverse equation or the inverse function with a dot product from the NumPy library. The results show the prices of each figurine from the given equations.

```

#2
using_solve = np.linalg.solve(quantities, cost)
using_solve

array([[1500.],
       [3000.],
       [3000.]])

```

Figure 3 Using np.linalg.solve ()

Figure 3 shows the results from solving a system of the linear equation using the np.linalg.solve() function from NumPy. In comparison with the result from solving it with an inverse equation or inverse function with a dot product, it can be observed that both of the results are identical. The function np.linalg.solve() according to [1], “computes the “exact” solution, x , of the well-determined, full rank, linear equation $ax = b$.” This is the reason why the answers are the same.

IV. Conclusion

This laboratory familiarized me with the principles and techniques of solving linear equations using the various linear algebra techniques and to solve a system of equations using Python programming and NumPy library. I learned how this can be implemented through the practical examples provided in the discussion. Learning all of this in this laboratory are my precious achievement. Lastly, I realized through this laboratory that the essence of the system of linear equations is that it can represent data or elements in life which can help us to make our life easier. This is evident in the practical examples presented in this laboratory and solving linear equations help in producing technologies like the one that is used today in the medical field which is CT imaging [2]. According to [3], linear algebra is fundamental in robotics because it was used for robot modeling, control, and optimization. An equation or a mathematical model represents how the arm of a robot moves and every joint of this can be described using a matrix and a proper matrix operation here can result in another equation that might describe a specific position of the arm of the robot [4]. To conclude, a system of linear equations can be used to model the kinematics of a robot arm.

References

- [1]"numpy.linalg.solve — NumPy v1.19 Manual", *Numpy.org*, 2020. [Online]. Available: <https://numpy.org/doc/stable/reference/generated/numpy.linalg.solve.html>. [Accessed: 13- Dec- 2020].
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Appendix

This is the GitHub Repository <https://github.com/RovilSurioJr/Laboratory-8>