

Assumed Values:

Quantity	Value	Units
Strength	3.78	ksi
Thrust per motor	10	lbs
Dist. to 1 st Motor	12	in
Dist. to 2 nd Motor	30	in

Moment of Inertia of a square about its diagonal:

$$I_x = I_y = \frac{a^4}{12}$$

<https://byjus.com/jee/moment-of-inertia-of-a-square/>

Flexure Formula:

$$\sigma = -\frac{My}{I}$$

<http://www.engineeringcorecourses.com/solidmechanics1/C4-bending/C4.2-flexure-formula/theory/>

Solution Steps:

$$M = 10[lb] * 12[in] + 10[lb] * 30[in] = 420[in * lb_f]$$

$$y = \sqrt{2} * a$$

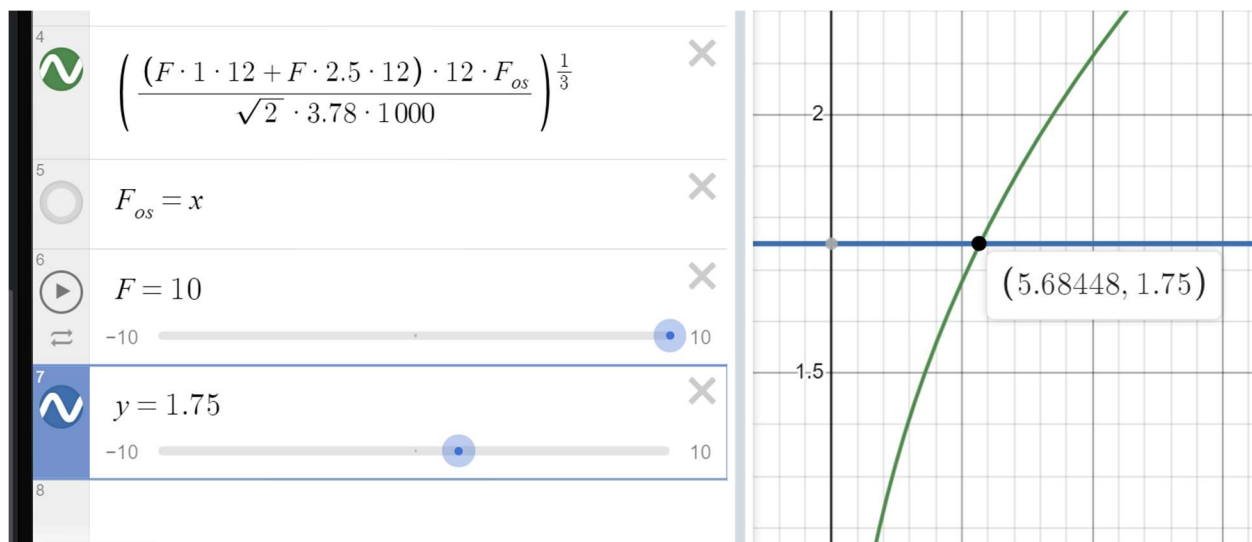
$$a = \sqrt[3]{\frac{12 * M * F_{os}}{\sqrt{2} * \sigma}} [in] = 0.9806 * \sqrt[3]{F_{os}} [in]$$

$$F_{os} = \left(\frac{a}{0.9806}\right)^3$$

F_os of common square dowel sizes (referenced from Lowes website)

Square edge length [in]	F_os
0.7500	0.4475
1.0000	1.0607
1.2500	2.0716
1.7500	5.6845
2.0000	8.4853

Choice: 1.25in (which is currently out of stock, will likely end up using 1.75)



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$$\left(\frac{(F \cdot 1 \cdot 12 + F \cdot 2.5 \cdot 12) \cdot 12}{\sqrt{2} \cdot 3.78 \cdot 1000} \right)^{\frac{1}{3}} \cdot F_{os}^{\frac{1}{3}}$$



$$= 0.980560917811$$

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$$F_{os} = 1$$



-10



10

6



$$F = 10$$



-10



10

7



$$y = 1.75$$



-10



10

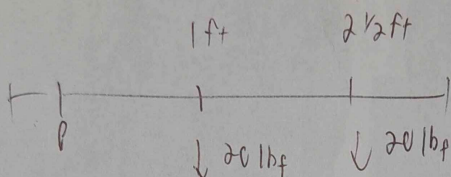
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$$\left(\frac{1.75}{0.980560917811} \right)^3$$



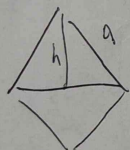
$$= 5.68447560813$$

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$$M_p = 20 + 50 \text{ lbf} = 70 \text{ ft} \cdot \text{lbf} = 840 \text{ in} \cdot \text{lbf}$$

$$\sigma = \frac{M_y}{I} = 0.3 \text{ ksi} \quad \frac{\text{lb}}{\text{in}^2}$$



$$I = \frac{M_y}{\sigma} = \frac{840 \text{ [in} \cdot \text{lbf]}}{0.3 \text{ [klb/in}^2\text{]}} \cdot h$$

$$a = h\sqrt{2}$$

$$h = \frac{a}{\sqrt{2}}$$

$$I_x = I_y = \frac{a^4}{12} \quad \text{or} \quad \frac{a^4}{12} \cdot \left(\frac{\sqrt{2}}{a} \right) = \frac{840}{0.3 \cdot 1000} \text{ [in}^3\text{]}$$

$$a = \sqrt[3]{\frac{840 \cdot 12}{\sqrt{2} \cdot 0.3 \cdot 1000}} \text{ [in]}$$