

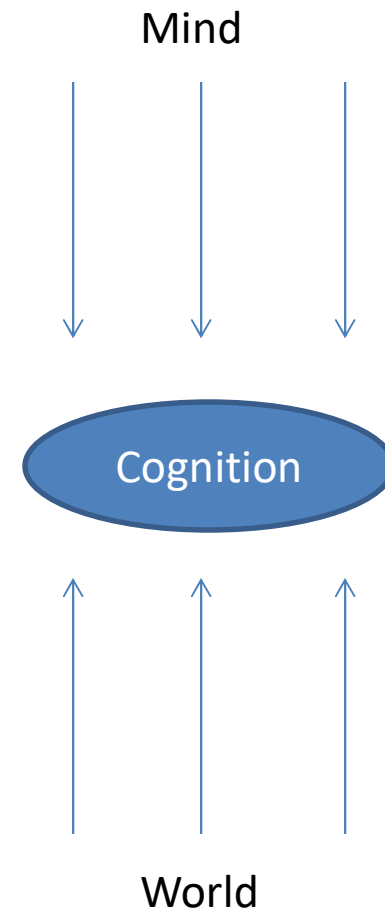
# Association

Nisheeth

5<sup>th</sup> August 2024



Welcome to CS786 - a computational cognitive science course!



Cognitive Science investigates the data structures that the mind uses

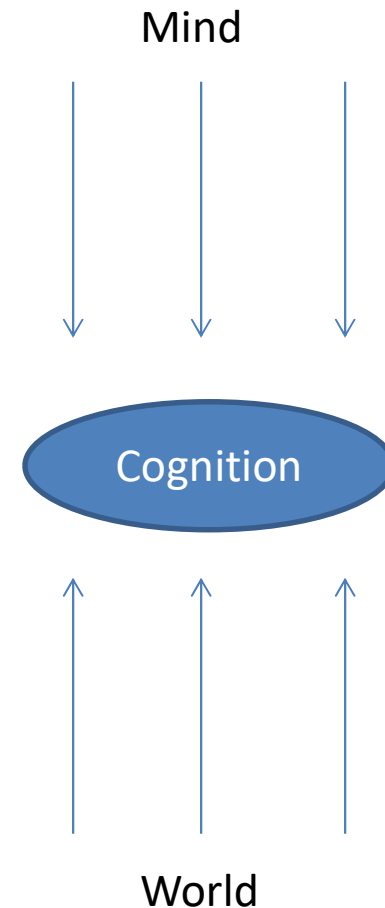
# Nature vs nurture



Developmental psychologists have found that even newborns come with a large bag of phenotypic and genetic experience

# Cognition and computation

- Cognition is fundamentally path-dependent
- Purely analytic approaches fare poorly with path-dependence
- Computation maps on to cognitive path-dependence well



# About me

- I'm Nisheeth
- I sit in ESB2-602
- Class timings are :
  - Monday 1535-1650
  - Tuesday 1400-1515
- All classes in RM101, except the ones I move online
- Office hours for this course will be by email appointment
  - Informal office hours right after the class everyday
- Email : nsrivast at iitk.ac.in

# Course evaluation policy

- 4 take home programming assignments (15% of course grade each)
  - Programming prep needed
    - ESC101
    - python
    - Courage
- 20% course credit for a 2000-word research paper, either improving upon a published model, or surveying modeling literature in an area
- 10% course credit from attendance
- 10% course credit for active participation in class discussions
  - Just engaging actively on the course forum will be adequate to get full marks for this component

# Course structure

- Broadly five segments
  - Association
  - Reinforcement
  - Accumulation
  - Embodiment
  - Learning
- Each segment will last about 5 lectures, bookended by a forum discussion and assignment
- Reading material will be assigned as web-links within each lecture
  - If you don't read, you won't be able to contribute in the discussions, which will draw upon these readings
  - Students are also encouraged to suggest their own readings; I will add them to the list if they seem relevant
  - Don't have to read all the material assigned, but the more you do, the more fun you will have in the panel discussions



# Course policies

- Add-drop deadline
  - Drops beyond that will require instructor and DUGC permission
  - My permission can be taken for granted
- Assuming good faith on your part (regular attendance and participation in evaluation and experiments), the lowest possible grade you will get is B

# Course philosophy

- This is a science course, not an engineering course
  - Emphasis is on following the chain of understanding where it leads
  - We will cover a lot of topics, sometimes unrelated to each other
- Assignments will often be challenging
- Collaboration in programming assignments is acceptable (with acknowledgement)
- There will be math
  - Don't let it scare you

# Association

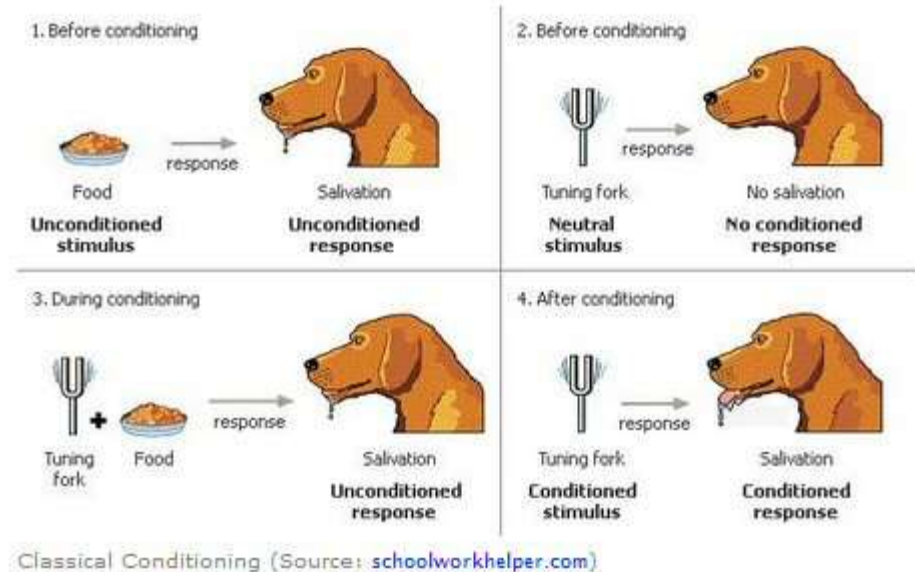
- A computer stores information randomly. A mind contains concepts associatively



© Ian Cuming/Ikon Images/Corbis

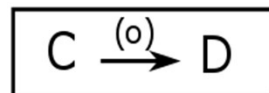
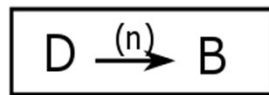
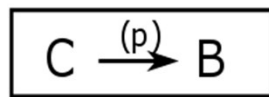
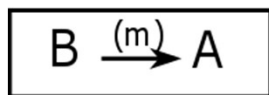
# What is relatedness?

- Co-occurrence → Among the first behavior invariants discovered
- Functionally unrelated concepts become related when they are presented together
- Pavlov's dogs learned to *associate* sound with food.



# Knowing concepts associatively

- *Related concepts* are activated concurrently



**File cabinet  
memory**

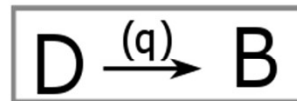
*Concepts:*

*A - spherical object, B - atom, C - proton, D - electron, E - planet, F - satellite*

*Links:*

*(m) - is a type of, (n) revolves within, (o) - is oppositely charged to, (p) - constituent of, (q) - revolves around*

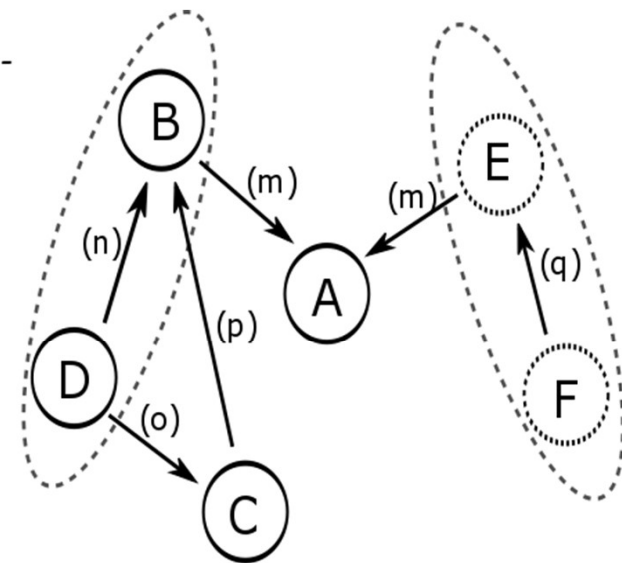
Test response



**Evaluation**

Wrong

Almost



**Associative  
memory**

Appearance of stimulus is closely followed by a particular behavior









CS: conditioned stimulus



US: unconditioned stimulus



# Real-Life Examples of Classical Conditioning

## Gustavson and Gustavson (1985) - Conditioned Taste Aversion

Coyotes killing sheep - problem to sheep farmers

Study conditioned coyotes not to eat the sheep

Sheep meat (CS) sprinkled with a chemical (UCS) that would produce a stomachache (UCR)

After coyotes ate the treated meat, they avoided the live sheep (CR)

This humane application of conditioned taste aversion might be used to control other predators as well



# Real-Life Examples of Classical Conditioning

Metalmikov & Chorine (1926, 1928) - Immune System

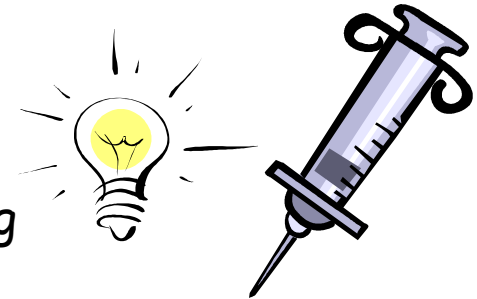
Injected Guinea Pigs with Foreign agents (non lethal)  
→ antibodies → boost their immune system

Then paired injections with Lights

Lights + Injections = better immunity

Lights alone = better immunity

Later Injected Cholera: animals with prior conditioning  
better survival vs controls with no conditioning



# Closer home ...



- The average person picks up their phone 80+ times a day
- More than 2k interactions per day

# Modeling classical conditioning

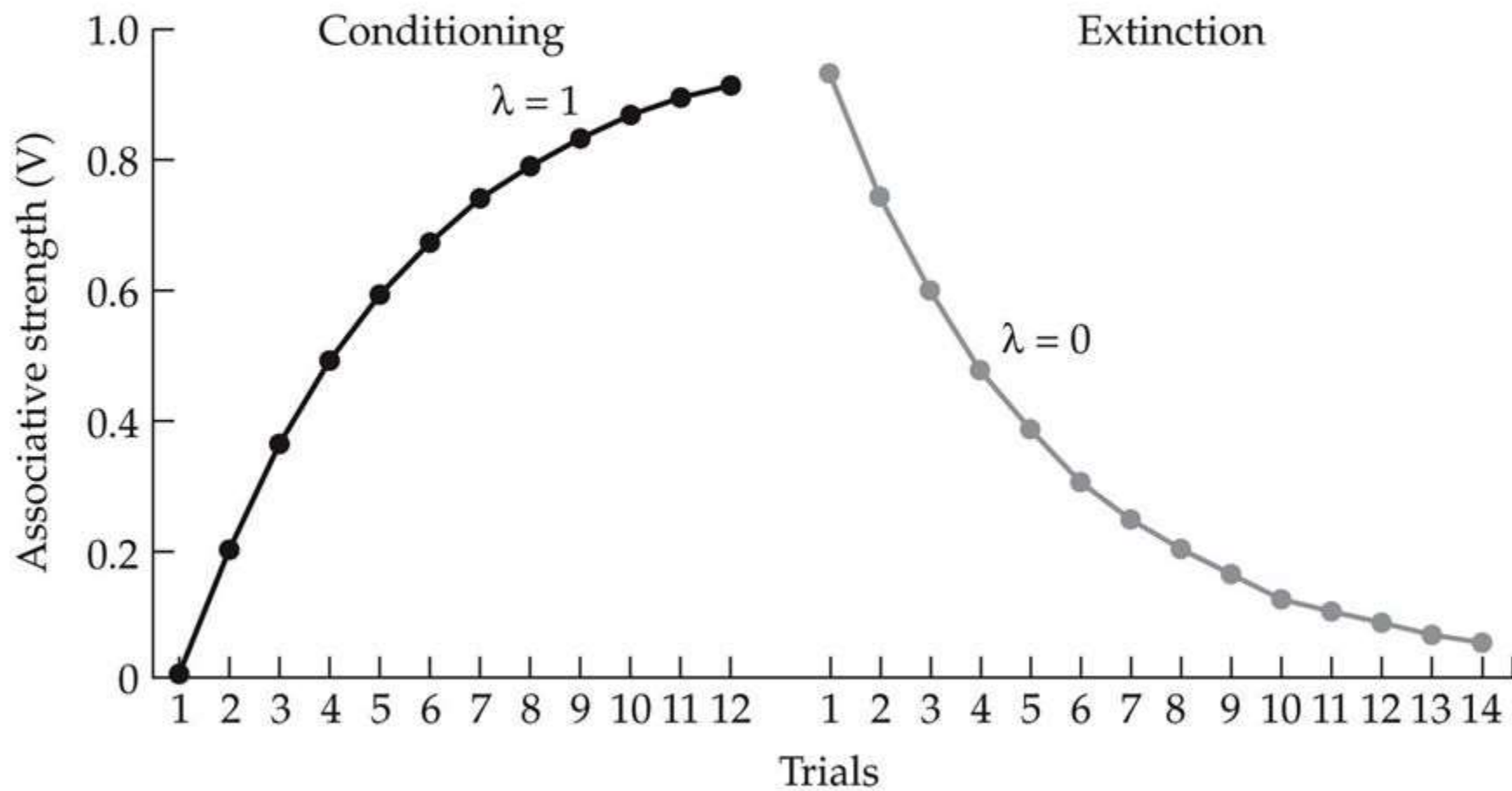
- Most popular approach for years was the Rescorla-Wagner model

$$\Delta V_X^{t+1} = \alpha_X \beta(\lambda - V_{tot}),$$
$$V_X^{t+1} = V_X^t + \Delta V_X^{t+1}$$

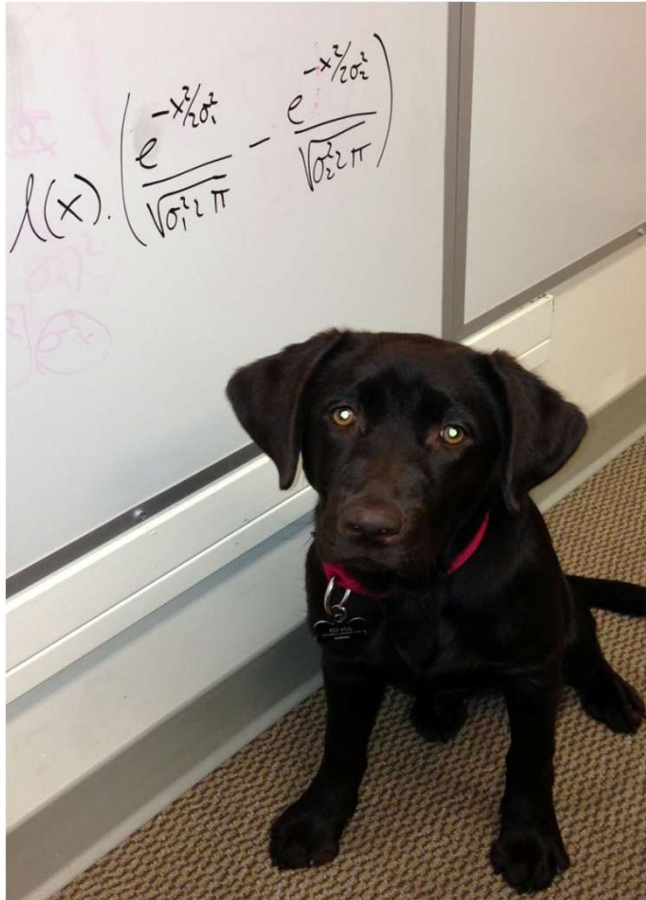
Some versions replace  $V_{tot}$  with  $V_x$ ; what is the difference?

- Could reproduce a number of empirical observations in classical conditioning experiments

### 4.3 Conditioning and extinction in the Rescorla-Wagner model



# What RW could explain



# What it couldn't



Pre-exposed

$$l(x) \cdot \left( \frac{e^{-x^2/2\sigma^2}}{\sqrt{\sigma^2\pi}} - \frac{e^{-x^2/2\sigma^2}}{\sqrt{\sigma^2\pi}} \right)$$

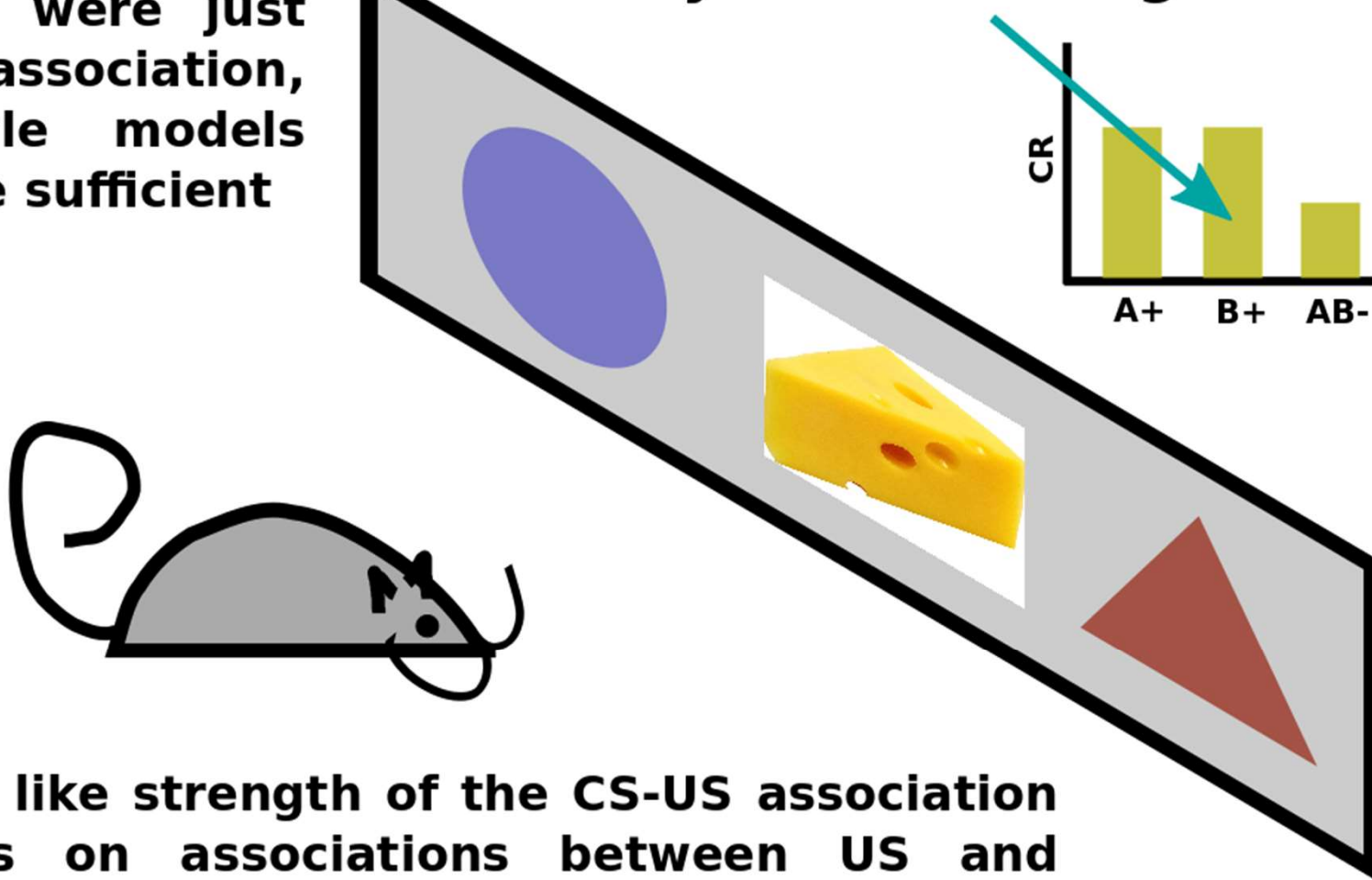


**Latent inhibition**



If value were just CS-US association, RW style models would be sufficient

**Plenty of conflicting evidence**



It looks like strength of the CS-US association depends on associations between US and other stimuli too. Why not model these relationships stochastically?

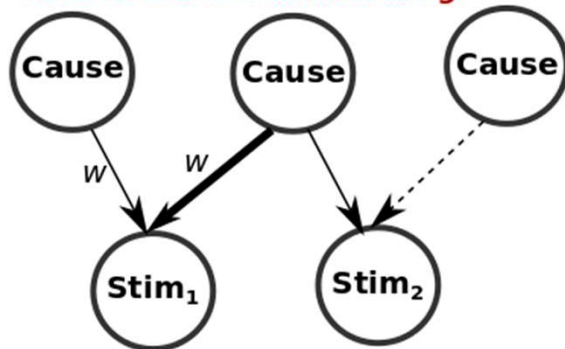
[https://en.wikipedia.org/wiki/Rescorla%E2%80%93Wagner\\_model](https://en.wikipedia.org/wiki/Rescorla%E2%80%93Wagner_model)



# Bayesian models of classical conditioning

(Courville, Daw & Touretzky, 2004)

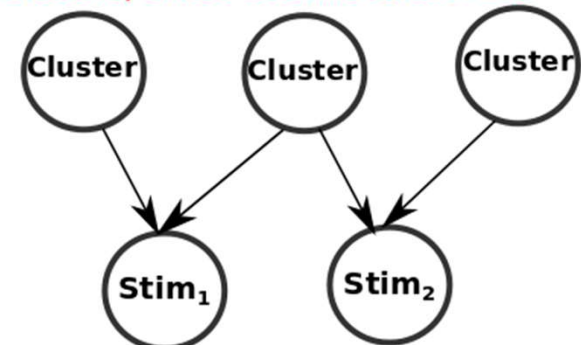
**LVs are causes that animals think lead to observations arising**



**Plasticity arises from learning weights connecting stimuli and causes**

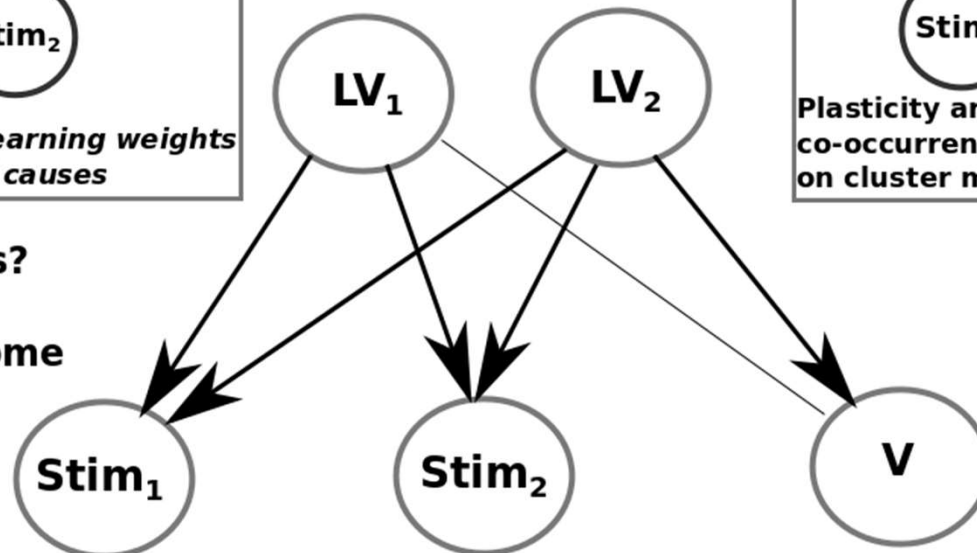
(Gershman & Niv, 2012)

**Animals group observed stimuli into clusters; these become causal LVs**



**Plasticity arises from learning stimuli co-occurrence frequencies conditioned on cluster membership (also learned)**

**How to interpret latent variables?**



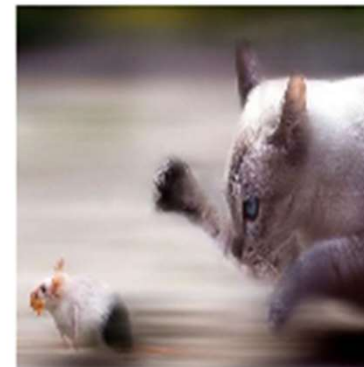
**How many causes?**

**Where do they come from?**

**Fails to predict summation-based conditioning effects.**

**What does clustering buy us?**

Interpret latent variables as **situations**.  
not **causes**



Index **situations** by stimuli co-occurrence  
patterns



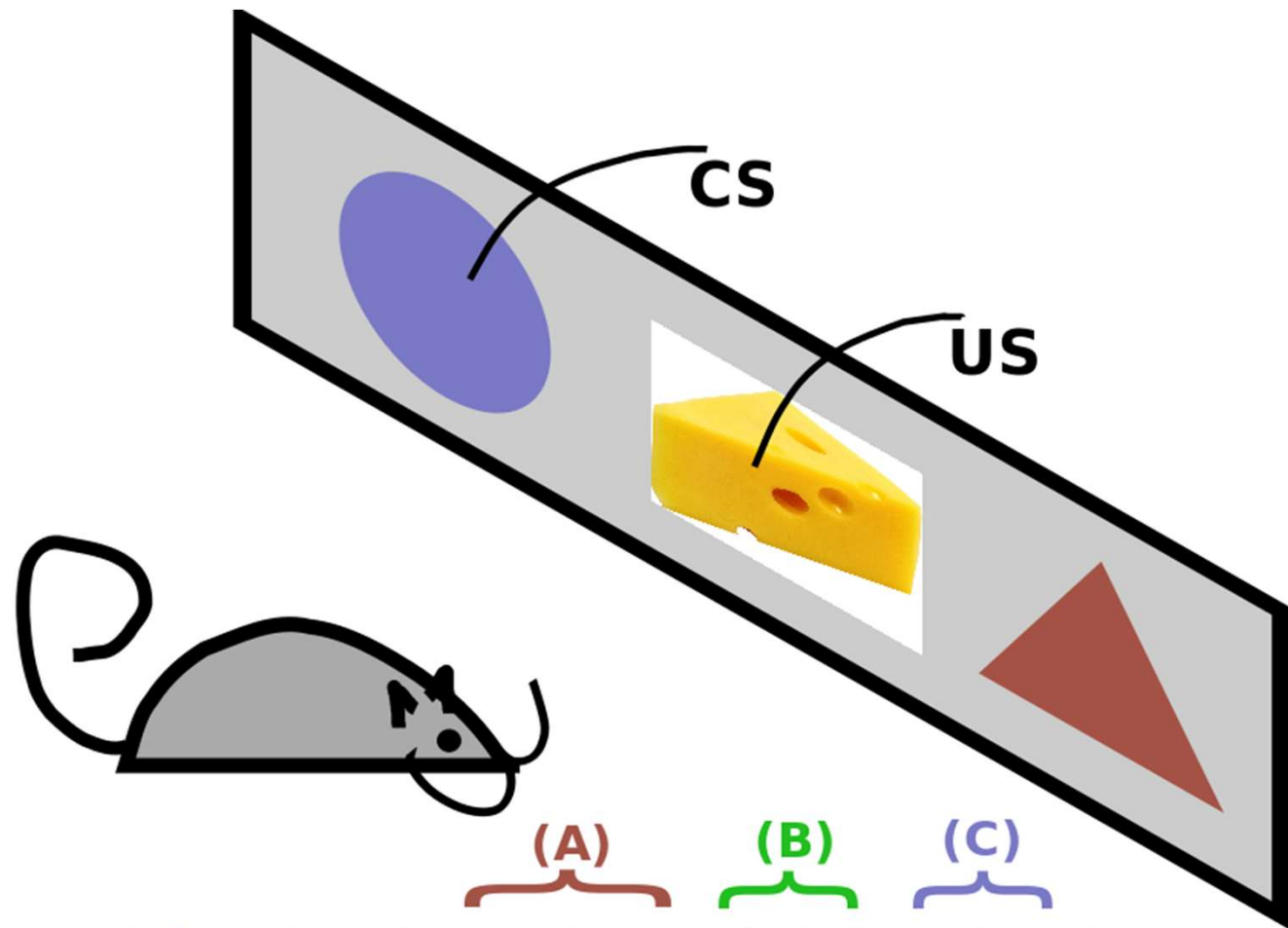
s = **Yeah!**



s = *Smooth* ...



s = **Yikes!!!**



$$p(\text{cheese} | \text{blue circle}) = \frac{\sum_s \underbrace{p(\text{cheese} | \text{blue circle}, s)}_{(A)} \underbrace{p(\text{blue circle} | s)}_{(B)} \underbrace{p(s | o_{1:t})}_{(C)}}{\sum_s p(\text{blue circle} | s) p(s | o_t)}$$

### (A) Association computation

$$p(\text{cheese} | \text{red triangle}, s) = 1 \text{ iff } s = \boxed{\text{cheese} \text{ ? } \text{red triangle}}$$

### (B) Likelihood computation

s		o <sub>t</sub>
<div style="border: 1px solid black; padding: 5px; display: inline-block;"> </div>	<div style="border: 1px solid black; padding: 5px; display: inline-block;"> </div>	
$p(\text{green square}   s) = 1$	$p(\text{beer glass}   s) = 0$	$p(\text{four dots}   s) = 0$

# Summary

- The mind learns by association
  - Associates novel with known, based on a number of ways of relation
- Association of novel to known causes generalization
- Association of known with known causes reinforcement
- We will talk more about reinforcement soon