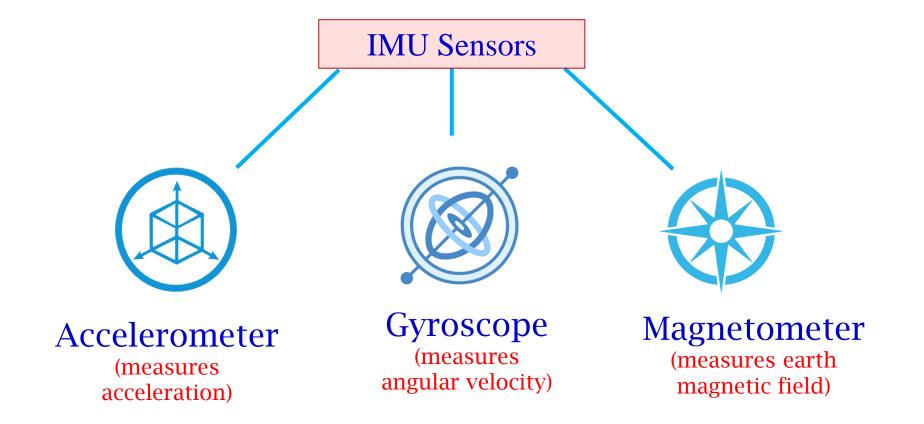
# Motion Tracking using IMU sensors

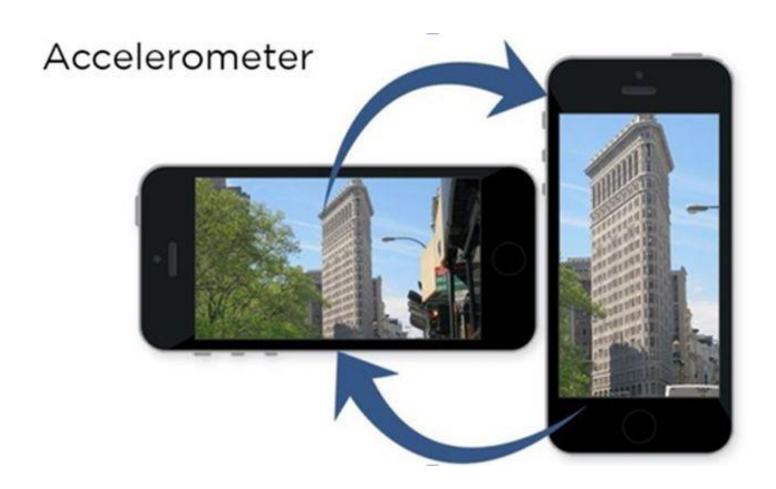
Amitangshu Pal

### IMU Sensors

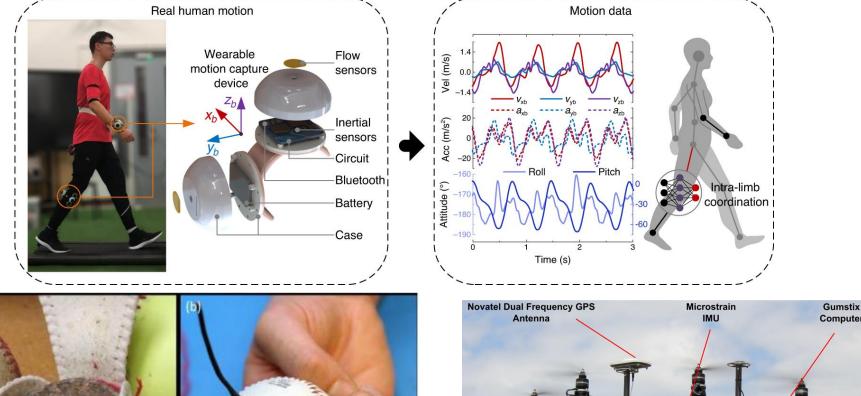


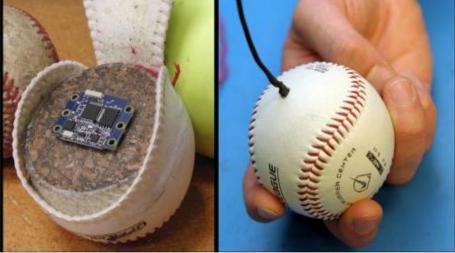
Install **Physics Toolbox Sensor Suite** in your smartphone

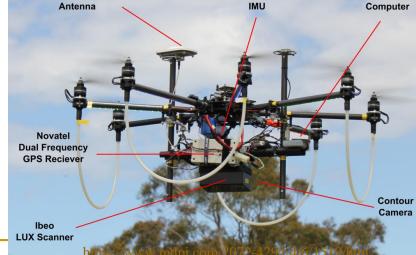
## IMU Sensors



Motion Tracking Applications



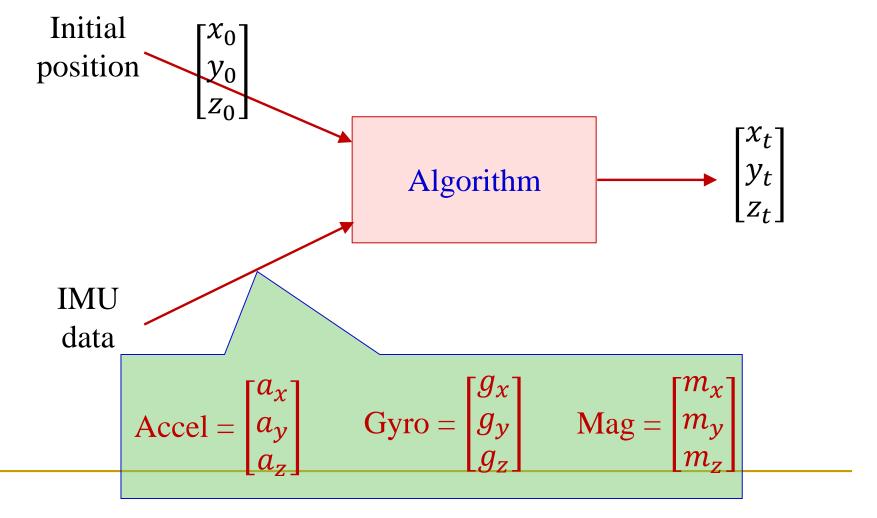




https://www.nature.com/articles/s41467-020-19424-2

# Motion Tracking Problem Formulation

Suppose we want to track the trajectory of a drone from its IMU data

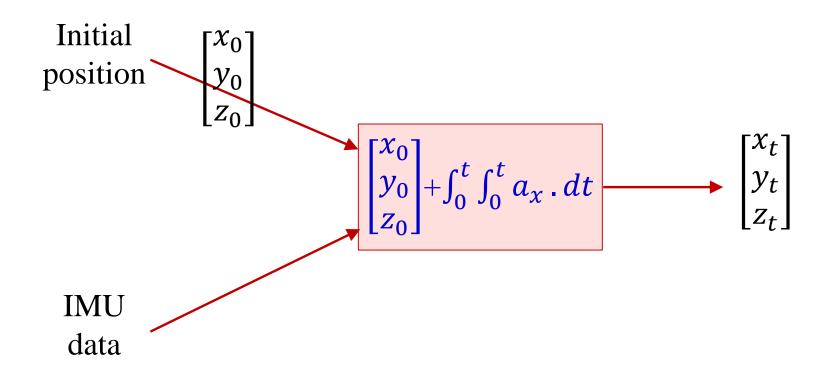


Let' see why this problem is so complicated

# Simple Case: No Rotation

$$v_{x} = \int_{0}^{t} a_{x} \cdot dt$$

$$d_{x} = \int_{0}^{t} v_{x} \cdot dt \quad \to d_{x} = \int_{0}^{t} \int_{0}^{t} a_{x} \cdot dt$$

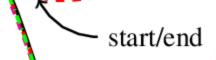


# Simple Case: No Rotation

$$v_{x} = \int_{0}^{t} a_{x} \cdot dt$$

$$d_{x} = \int_{0}^{t} v_{x} \cdot dt \quad \to d_{x} = \int_{0}^{t} \int_{0}^{t} a_{x} \cdot dt$$

$$d_{x} = \int_{0}^{t} \int_{0}^{t} (a_{x} + noise) \cdot dt$$



Error accumulates over time

Accelerometer values are mixed with gravity

### What if the Motion Includes Rotation also?

Let's model rotation using Ax = b form

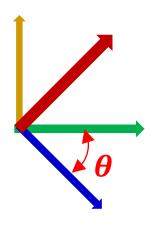
$$X: \begin{bmatrix} 0 \\ -1 \end{bmatrix} \qquad Y: \begin{bmatrix} 1 \\ 0 \end{bmatrix} \qquad Y: \begin{bmatrix} 0 \\ 1 \end{bmatrix} \qquad Y: \begin{bmatrix} 0 \\ 1 \end{bmatrix} \qquad Y: \begin{bmatrix} -1 \\ 0 \end{bmatrix} \qquad X: \begin{bmatrix} 0 \\ 1 \end{bmatrix}$$

$$\begin{bmatrix} \cos 90^{\circ} & -\sin 90^{\circ} \\ \sin 90^{\circ} & \cos 90^{\circ} \end{bmatrix} \begin{bmatrix} 0 & 1 \\ -1 & 0 \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$\begin{bmatrix} \cos 90^{\circ} & -\sin 90^{\circ} \\ \sin 90^{\circ} & \cos 90^{\circ} \end{bmatrix} \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} = \begin{bmatrix} 0 & -1 \\ 1 & 0 \end{bmatrix}$$

## Mapping Local Coordinate to Global Coordinate

- So whatever acceleration values we are getting is w.r.t. the IMU's local coordinate system
  - How to map it to the global coordinate system?
- Let's first assume that we know the IMU orientation w.r.t the global axis



$$\begin{bmatrix} x_G \\ y_G \end{bmatrix} = \begin{bmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{bmatrix} \begin{bmatrix} x_S \\ y_S \end{bmatrix}$$

### What if the Motion Includes Rotation also?

For 3D the rotation matrix is

$$R = R_x(\alpha)R_y(\beta)R_z(\gamma)$$

$$= \begin{bmatrix} \cos \alpha \cos \beta & \cos \alpha \sin \beta \sin \gamma - \sin \alpha \cos \gamma & \cos \alpha \sin \beta \cos \gamma + \sin \alpha \sin \gamma \\ \cos \alpha \cos \beta & \sin \alpha \sin \beta \sin \gamma + \cos \alpha \cos \gamma & \sin \alpha \sin \beta \cos \gamma - \cos \alpha \sin \gamma \\ -\sin \beta & \cos \beta \sin \gamma & \cos \beta \cos \gamma \end{bmatrix}$$

But how to find out the IMU orientation w.r.t. the global coordinate?

#### How to Get The 3d Orientation?

Method1: Using accelerometer and magnetometer

Measures acceleration

Measures magnetic north

- What rotation is needed so that
  - Gravity is along the z axis
  - Magnetic north is along the y axis?

$$\begin{bmatrix} 3x3 \\ rotation \\ matrix \end{bmatrix} \begin{bmatrix} a_x & m_x \\ a_y & m_y \\ a_z & m_z \end{bmatrix} = \begin{bmatrix} 0 & 0 \\ 0 & M \\ 9.8 & 0 \end{bmatrix}$$

Works well when the IMU is static
When object is moving → gravity measurement is polluted with acceleration

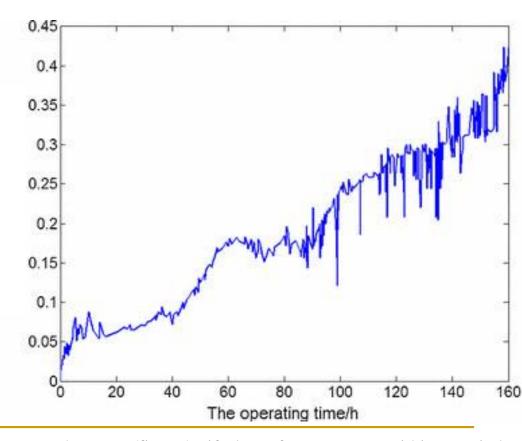
### How to Get The 3d Orientation?

- Method2: Using gyroscope
  - Assume that we know the initial orientation

$$\theta_t = \theta_{t-1} + \int_0^t \omega_t \cdot dt$$

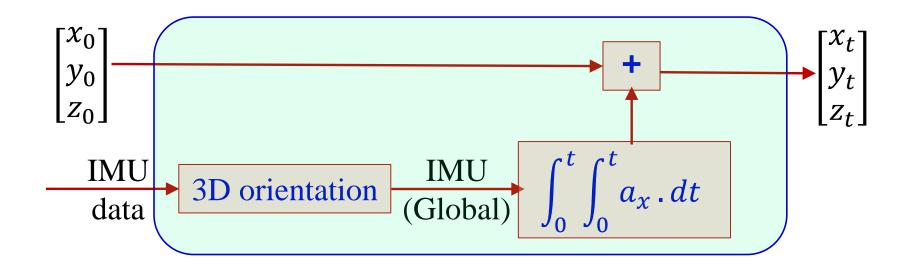
$$\theta_t = \theta_{t-1} + \int_0^t (\omega_t + noise) \cdot dt$$

Error accumulates over time

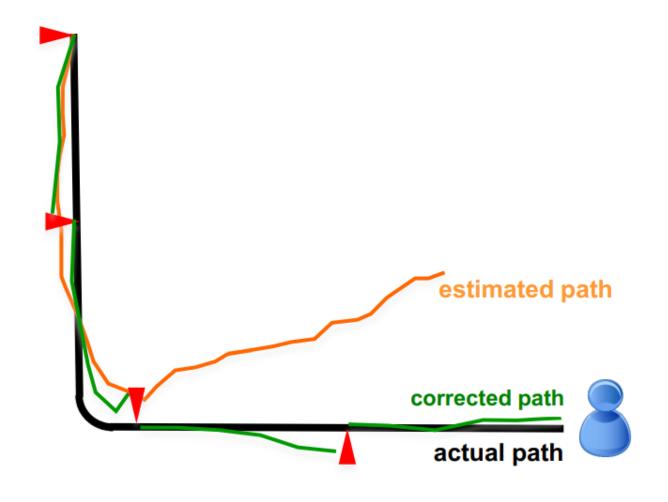


# Overall Algorithm

- Someone can use a mixture of Method1 and Method2
  - While static give preference to Method1
  - While moving give preference to Method2



#### Path Estimation Error Accumulation



## Our Experimental Outcome

