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CECS 328 Section 11  
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## Programming Assignment 1: RunForYourLife

### Freddy's Algorithm

| s=1    | Trial 1 | Trial 2 | Trial 3 | Trial 4 | Trial 5 | Trial 6 | Trial 7 | Trial 8 | Trial 9 | Trial 10 | Average | Units |
|--------|---------|---------|---------|---------|---------|---------|---------|---------|---------|----------|---------|-------|
| n=1000 | 336.952 | 340.102 | 337.234 | 338.722 | 336.927 | 337.221 | 336.153 | 337.112 | 338.781 | 336.457  | 337.566 | ms    |
| n=2000 | 2.661   | 2.624   | 2.656   | 2.611   | 2.634   | 2.679   | 2.615   | 2.645   | 2.617   | 2.609    | 2.635   | s     |
| n=4000 | 22.513  | 22.512  | 22.567  | 22.524  | 22.531  | 22.511  | 22.545  | 22.551  | 22.526  | 22.531   | 22.531  | s     |

**Predictions:** n=2000 : 2.701sec , n=4000 : 21.608sec,

**Complexity:**  $n^3$

Prediction justification: I came to this prediction based on the average time if n inputs were doubled. We need to cube the amount and multiply it by the average time to get an accurate prediction. So by this logic, for everytime n is doubled we need to multiply the average by 8. So we multiply 337.566 ms by 8, and the same for the next average after to get the next value. Doing so gives us an accurate representation that was very close to our actual values.

**Deviation:** We did see some slight deviation, less than 5%, and this can be because of other factors like outside programs and the fact that I am running this via VM.

### Sophie's Algorithm

| s=1     | Trial 1 | Trial 2 | Trial 3 | Trial 4 | Trial 5 | Trial 6 | Trial 7 | Trial 8 | Trial 9 | Trial 10 | Average | Units |
|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|----------|---------|-------|
| n=10000 | 94.134  | 94.144  | 94.132  | 93.991  | 94.072  | 94.163  | 94.122  | 94.131  | 94.102  | 94.156   | 94.115  | ms    |
| n=20000 | 0.421   | 0.423   | 0.429   | 0.431   | 0.427   | 0.425   | 0.432   | 0.426   | 0.431   | 0.429    | 0.427   | s     |
| n=40000 | 1.681   | 1.701   | 1.695   | 1.691   | 1.694   | 1.689   | 1.698   | 1.709   | 1.693   | 1.690    | 1.694   | s     |

**Prediction:** n=20000 : 0.421sec, n=40000 : 1.684sec,

**Complexity:**  $n^2$

I found that the runtime complexity of Sophie's algorithm was  $n^2$  so when we double n from 10,000 inputs to the next n value of 20,000 we also multiply our average from the previous trial by 4x and from the one before that we double it to obtain the theoretical average. So for example from n=20000 we get an average of 0.427, and to predict what we want we need to multiply our average by 4 to get our prediction for n=40000.

**Deviation:** There is not as much deviation in this program compared to Freddy's, and was found to be under 3% overall. This can be related to the compiler or to background applications.

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### Johnny's Algorithm

| s=1        | Trial 1 | Trial 2 | Trial 3 | Trial 4 | Trial 5 | Trial 6 | Trial 7 | Trial 8 | Trial 9 | Trial 10 | Average | Units |
|------------|---------|---------|---------|---------|---------|---------|---------|---------|---------|----------|---------|-------|
| n=1000000  | 96.922  | 97.332  | 96.512  | 97.562  | 98.323  | 96.124  | 95.343  | 97.221  | 96.231  | 95.871   | 96.744  | ms    |
| n=2000000  | 188.221 | 186.234 | 185.891 | 188.451 | 187.201 | 188.561 | 181.992 | 187.221 | 185.910 | 183.102  | 186.278 | ms    |
| n=50000000 | 5.076   | 5.129   | 5.221   | 4.991   | 5.012   | 5.192   | 5.294   | 5.124   | 5.081   | 5.009    | 5.113   | s     |

**Prediction:** n=2000000: 161.243 ms, n=50000000 : 5.231secs

**Complexity:**  $n * \log(n)$

I had a more difficult time getting an accurate calculation for Johnny's but used the same method to formulate it as I did before. So when  $T(n) = K \text{ Value} * n * \log(n)$ , where  $T(n)$  is the average used in n=1000000. We see a more accurate calculation.

Method:  $K \text{ Value} * 1000000 \log 1000000 = 96.74 \rightarrow k = 161.243 \text{ ms}$

**Deviation:** I saw significantly more deviation in this algorithm compared to the other ones. It may be because I am using a virtual machine, But I think more likely that any other background computer computations, like my google chrome, really affect the outcome of this algorithm

### Sally's Algorithm

| s=1         | Trial 1 | Trial 2 | Trial 3 | Trial 4 | Trial 5 | Trial 6 | Trial 7 | Trial 8 | Trial 9 | Trial 10 | Average | Units |
|-------------|---------|---------|---------|---------|---------|---------|---------|---------|---------|----------|---------|-------|
| n=50000000  | 94.331  | 95.112  | 95.295  | 94.987  | 94.345  | 94.872  | 94.511  | 93.998  | 95.107  | 94.416   | 94.697  | ms    |
| n=100000000 | 187.231 | 187.691 | 188.623 | 188.191 | 188.142 | 187.432 | 188.275 | 188.312 | 188.144 | 187.671  | 187.97  | ms    |
| n=200000000 | 374.292 | 375.312 | 375.674 | 375.981 | 373.911 | 375.102 | 374.912 | 375.531 | 376.112 | 375.678  | 375.051 | ms    |

**Prediction:** n=100000000: 189.394ms, n=200000000 : 378.788ms

**Complexity:** n

We can multiply the time it takes to run this program by 2 when n is doubled. So when we double that again or 4n, we can multiply it by a power of 4. Knowing this, when we double n from 50M, to 100M for the n value, we are also doubling the averages that are based on the previous trials. So to get our predictions we can just multiply the current average by 2 to get the value of 2n. For example,  $n=100000000: 189.394\text{ms} * 2 \rightarrow 378.788\text{ms}$  for n=200000000

Deviation: There is also a slight deviation in this algorithm that can be pointed to the compiler and background applications, especially when making a calculation of this magnitude in such a short amount of time.

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**Overall**, I think that Sally's algorithm is significantly more efficient than the other algorithms. Based on the theoretical run times and the actual trials that I conducted, I can confirm that Sally's algorithm is the most effective and I would say Freddy's algorithm is the worst because of its runtimes compared to the other algorithms. I didn't even reach into the nano seconds for some tests on Freddy's because of its clunkiness. I would say that Sally algorithm has the best runtime complexity and the preferred program. I also had a few problems with runtimes originally because I was using an online compiler and the data wasn't very consistent. I found that Sally's program ran about 21 times faster than Freddy's and these calculations are very significant for efficiency. Even a time and a half slower is a big deal if someone were to make a larger calculation, I would expect any deviations and runtime differences to have a huge effect on the overall performance of the task. This can also be seen in the complexity of the algorithms, with Freddy's complexity of  $n^3$  while Sally's was just  $n$ . This makes a huge difference and we can see this in overall performance.