

Quiz 8.2 – Gas Laws

Name: Key

Question 1

A weather balloon starts in Cedar City with $P = 0.82 \text{ atm}$, $T = 21.5^\circ\text{C}$, and $V = 18.75 \text{ L}$

$$\rightarrow 273 + 21.5 = 294.5 \text{ K}$$

- Find the number of moles of gas inside the balloon

$$n = \frac{PV}{RT} = \frac{0.82 \text{ atm} \cdot 18.75 \text{ L}}{0.0821 \frac{\text{L} \cdot \text{atm}}{\text{mol} \cdot \text{K}} \cdot 294.5 \text{ K}} = 0.64 \text{ moles}$$

- If the balloon is filled with He gas, find the mass of the gas inside the balloon

$$\frac{0.64 \text{ moles He} \cdot 4.00 \text{ g He}}{1 \text{ mol He}} = 2.56 \text{ g} = 2.6 \text{ g}$$

- Find the density of the He-filled balloon (assume the instruments and balloon itself have no mass)

$$d = \frac{m}{V} = \frac{2.56 \text{ g}}{18.75 \text{ L}} = 0.14 \frac{\text{g}}{\text{L}} = 1.4 \cdot 10^{-4} \frac{\text{g}}{\text{mL}}$$

- Find the density of the surrounding air (assume it is 100% N_2 gas)

$$\frac{0.64 \text{ moles } \text{N}_2 \cdot 28.01 \text{ g } \text{N}_2}{1 \text{ mol } \text{N}_2} = 17.9 \text{ g } \text{N}_2 \quad d = \frac{17.9 \text{ g}}{18.75 \text{ L}} = 0.96 \frac{\text{g}}{\text{L}} = 9.6 \cdot 10^{-4} \frac{\text{g}}{\text{mL}}$$

Question 2

The weather balloon is released into the upper atmosphere and the instruments on-board indicate a pressure of 0.45 atm and a temperature of -32.4°C

$$\rightarrow 273 - 32.4 = 240.6 \text{ K}$$

What will the new volume of the balloon be?

$$\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2} \rightarrow V_2 = \frac{P_1 V_1 T_2}{T_1 P_2} = \frac{0.82 \text{ atm} \cdot 18.75 \text{ L} \cdot 240.6 \text{ K}}{294.5 \text{ K} \cdot 0.45 \text{ atm}} = 27.9 \text{ L} = 28 \text{ L}$$

Question 3

A car engine burns about 0.1 g of gasoline (C_8H_{18}) for each engine cycle. A car engine may have a cylinder volume of 1.25 L , and operate at a temperature of 80.0°C . If the gasoline combusts completely inside the 1.25 L piston, what is the pressure of the combustion products?

$$\frac{0.1 \text{ g } \text{C}_8\text{H}_{18}}{114.23 \text{ g } \text{C}_8\text{H}_{18}} \cdot \frac{1 \text{ mol } \text{C}_8\text{H}_{18}}{1 \text{ mol } \text{C}_8\text{H}_{18}} \cdot \frac{20 \text{ mol gas products}}{2 \text{ mol } \text{C}_8\text{H}_{18}} = 0.00875 \text{ moles gas product}$$

$$80.0 + 273 = 353 \text{ K}$$

$$P = \frac{nRT}{V} = \frac{0.00875 \text{ moles} \cdot 0.0821 \frac{\text{L} \cdot \text{atm}}{\text{mol} \cdot \text{K}} \cdot 353 \text{ K}}{1.25 \text{ L}} = 0.2 \text{ atm}$$