Introduction

Philip Schulz and Wilker Aziz

VI Tutorial @ Host Site

Because NN models work

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- lack of inductive bias

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well... that's no longer true!

What are you getting out of this today?

As we progress we will

- develop a shared vocabulary to talk about generative models powered by NNs
- derive crucial results step by step

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Goal

- you should be able to navigate through fresh literature
- and start combining probabilistic models and NNs

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Supervised problems

We have data $x^{(1)}, \ldots, x^{(N)}$ e.g. sentences, images generated by some **unknown** procedure which we assume can be captured by a probabilistic model

• with **known** probability (mass/density) function e.g.

$$X \sim \mathsf{Cat}(\theta_1, \dots, \theta_K)$$
 or $X \sim \mathcal{N}(\theta_\mu, \theta_\sigma^2)$

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$$X \sim \mathsf{Cat}(heta_1, \dots, heta_{\mathsf{K}}) \quad ext{ or } \quad X \sim \mathcal{N}(heta_{\mu}, heta_{\sigma}^2)$$

and estimate parameters θ that assign maximum likelihood $p(x^{(1)}, \dots, x^{(N)} | \theta)$ to observations

Supervised NN models

Let y be all side information available e.g. deterministic *inputs/features/predictors*

Have neural networks predict parameters of our probabilistic model

$$X|y \sim \mathsf{Cat}(\pi_{m{ heta}}(y))$$
 or $X|y \sim \mathcal{N}(\mu_{m{ heta}}(y), \sigma_{m{ heta}}(y)^2)$

and proceed to estimate parameters θ of the NNs

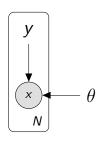
Graphical model

Random variables

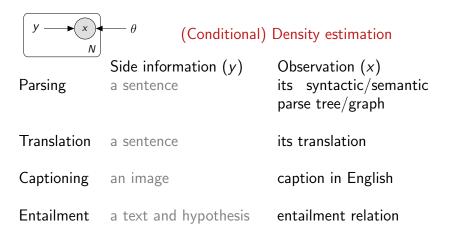
• observed data $x^{(1)}, \dots, x^{(N)}$

Deterministic variables

- inputs or predictors $y^{(1)}, \dots, y^{(N)}$
- ullet model parameters heta



Multiple problems, same language



Task-driven feature extraction

Often our side information is itself some high dimensional data

- y is a sentence and x a tree
- y is the source sentence and x is the target
- y is an image and x is a caption

and part of the job of the NNs that parametrise our models is to also deterministically encode that input in a low-dimensional space

NN as efficient parametrisation

From a statistical point of view, NNs do not generate data

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- compact and efficient way to map from complex side information to parameter space

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Prediction is done by a decision rule outside the statistical model

• e.g. argmax, beam search

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and we can update θ in the direction

$$\gamma \nabla_{\theta} \mathcal{L}(\theta|x^{(1:N)})$$

to attain a local maximum of the likelihood function

For large N, computing the gradient is inconvenient

$$oldsymbol{
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abla}_{ heta} \log p(x^{(s)}| heta) \ &= \mathbb{E}_{S \sim \mathcal{U}(1/N)} \left[N oldsymbol{
abla}_{ heta} \log p(x^{(S)}| heta)
ight] \end{aligned}$$

S selects data points uniformly at random

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Stochastic optimisation

For large N, we can use a gradient estimate

$$\nabla_{\theta} \mathcal{L}(\theta|x^{(1:N)}) = \underbrace{\mathbb{E}_{S \sim \mathcal{U}(1/N)} \left[N \nabla_{\theta} \log p(x^{(S)}|\theta) \right]}_{\text{expected gradient :)}}$$

Stochastic optimisation

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and take a step in the direction

$$\gamma \frac{N}{M} \underbrace{\nabla_{\theta} \mathcal{L}(\theta | x^{(s_1:s_M)})}_{\text{stochastic gradient}}$$

where $x^{(s_1:s_M)}$ is a random mini-batch of size M

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DL in NLP recipe

Maximum likelihood estimation

 tells you which loss to optimise (i.e. negative log-likelihood)

Automatic differentiation (backprop)

 "give me a tractable forward pass and I will give you gradients"

Stochastic optimisation powered by backprop

general purpose gradient-based optimisers

Constraints

Differentiability

- intermediate representations must be continuous
- activations must be differentiable

Tractability

 the likelihood function must be evaluated exactly, thus it's required to be tractable

When do we have intractable likelihood?

Unsupervised problems contain unobserved random variables

$$p(x, z|\theta)$$

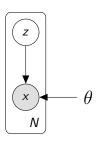
thus assessing the marginal likelihood requires marginalisation of latent variables

$$p(x|\theta) = \int p(x,z|\theta) dz$$

Latent variable model

Latent random variables

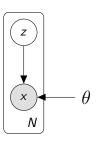
- unobserved
- or unobservable



Latent variable model

Latent random variables

- unobserved
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A joint distribution over data and unknowns

$$p(x, z|\theta) = p(z)p(x|z, \theta)$$

Examples of latent variable models

Discrete latent variable, continuous observation

$$p(x|\theta) = \underbrace{\sum_{c=1}^{K} \mathsf{Cat}(c|\pi_1, \dots, \pi_K)}_{\mathsf{forward\ pass}} \underbrace{\mathcal{N}(x|\mu_{\theta}(c), \sigma_{\theta}(c)^2)}_{\mathsf{forward\ pass}}$$

too many forward passes

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Continuous latent variable, discrete observation

$$p(x|\theta) = \int \mathcal{N}(z|0, I) \underbrace{\operatorname{Cat}(x|\pi_{\theta}(z))}_{\text{forward passes}} dz$$
infinitely many forward passes

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$$\nabla_{\theta} \log p(x|\theta)$$

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$$= \underbrace{\frac{1}{\int p(x,z|\theta) dz} \int \nabla_{\theta} p(x,z|\theta) dz}_{\text{chain rule}}$$

$$\begin{split} \boldsymbol{\nabla}_{\boldsymbol{\theta}} \log p(\boldsymbol{x}|\boldsymbol{\theta}) &= \boldsymbol{\nabla}_{\boldsymbol{\theta}} \log \underbrace{\int p(\boldsymbol{x},\boldsymbol{z}|\boldsymbol{\theta}) \, \mathrm{d}\boldsymbol{z}}_{\text{marginal}} \\ &= \underbrace{\frac{1}{\int p(\boldsymbol{x},\boldsymbol{z}|\boldsymbol{\theta}) \, \mathrm{d}\boldsymbol{z}} \int \boldsymbol{\nabla}_{\boldsymbol{\theta}} p(\boldsymbol{x},\boldsymbol{z}|\boldsymbol{\theta}) \, \mathrm{d}\boldsymbol{z}}_{\text{chain rule}} \\ &= \underbrace{\frac{1}{p(\boldsymbol{x}|\boldsymbol{\theta})} \int \underbrace{p(\boldsymbol{x},\boldsymbol{z}|\boldsymbol{\theta}) \boldsymbol{\nabla}_{\boldsymbol{\theta}} \log p(\boldsymbol{x},\boldsymbol{z}|\boldsymbol{\theta})}_{\text{log-identity for derivatives}} \, \mathrm{d}\boldsymbol{z} \end{split}$$

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But the posterior is not available!

$$p(z|x,\theta) =$$

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But the posterior is not available!

$$p(z|x,\theta) = \frac{p(x,z|\theta)}{p(x|\theta)}$$

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Some reasons

 better handle on statistical assumptions e.g. breaking marginal independence

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- uncertainty quantification e.g. Bayesian NNs

Examples: Lexical alignment

Generate a word x_i in L1 from a word y_{a_i} in L2

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Examples: Rationale extraction

Sentiment analysis based on a subset of the input

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where p(x|f, y) conditions on y_i iff $f_i = 1$.

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A factor model whose factors are labelled by words marginalisation $O(2^{|y|})$

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Probabilistic models parametrised by neural networks

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- explicit modelling assumptions one of the reasons why there's so much interest
- but requires efficient inference which is the reason why we are here today