

Assignment - 4

x_i	y_i
7.6	157
7.1	174

step 1: [7.6, 157] $\eta = 0.01$, $m = 1$, $c = -1$

$$\begin{aligned}\text{step 2: } \frac{\partial E}{\partial m} \bigg|_{m=1} &= -(y_i^a - mx_i^a - c)(-x_i^a) \\ &= (157 - 7.6(-1)) (7.6) \\ &= (150.4) (7.6) \\ &= 1143.04\end{aligned}$$

$$\begin{aligned}\frac{\partial E}{\partial c} \bigg|_{c=-1} &= (y_i^a - mx_i^a - c) \\ &= (157 - (1)(7.6) - (-1)) \\ &= -150.4\end{aligned}$$

$$\begin{aligned}\text{step-3: } \Delta m &= -\eta \frac{\partial E}{\partial m} = -(0.01) (1143.04) \\ &= -11.430\end{aligned}$$

$$\begin{aligned}\Delta c &= -\eta \frac{\partial E}{\partial c} = -(0.01) (-150.4) \\ &= 1.504\end{aligned}$$

$$\begin{aligned}\text{step-4: } m &= m + \Delta m = 1 + (-11.43) \\ &= -10.43\end{aligned}$$

$$c = c + \Delta c$$

$$= -1 + (1.504)$$

$$= 0.504$$

Iteration-2

$$S1: [7.6, 157], \eta = 0.01, m = -10.43, C = 0.504$$

$$\begin{aligned} S2: \frac{\partial E}{\partial m} \Big|_{m=10.43} &= (157 - (10.43)(7.61) - 0.504)(7.61) \\ &= (157 + (10.43)(1.61) - 0.504)(7.61) \\ &= (156.496 + 79.372)(7.61) \\ &= 1794.955 \end{aligned}$$

$$\begin{aligned} \frac{\partial E}{\partial C} \Big|_C &= 0.504 = -(157 - (-10.43)(7.61) - 0.504) \\ &= 235.868 \end{aligned}$$

$$S3: \Delta m = -\eta \frac{\partial E}{\partial C} = (0.01 \times 1794.955) = -17.949$$

$$\begin{aligned} \Delta C &= -\eta \frac{\partial E}{\partial C} = (-0.01)(-235.868) \\ &= 2.358 \end{aligned}$$

$$\begin{aligned} S4: m &= m + \Delta m = -10.43 + (-17.943) \\ &= -28.379 \end{aligned}$$

$$\begin{aligned} C &= C + \Delta C = 0.504 + 2.358 \\ &= 2.862 \end{aligned}$$

Sample-2 Iteration-1

$$S1: (7.1, 174) \quad \eta = 0.01, m = 1, C = -1$$

$$\begin{aligned} S2: \frac{\partial E}{\partial m} \Big|_{m=1} &= -(y_i^q - m x_i^q - C) - x_i^q \\ &= (174 - (7.1) - (-1)) + 7.1 \\ &= (175 - 7.1)(7.1) \end{aligned}$$

$$\frac{\partial E}{\partial c} \Big|_{c=1} = - (y_i^a - m x_i^a - c)$$

$$= - (174 - (7 \cdot 1) - (-1))$$

$$= -167 \cdot 9$$

$$S3: \Delta m = -\eta \frac{\partial E}{\partial m} = - (0.01) 1192.09$$

$$= -11.920$$

$$\Delta c = -\eta \frac{\partial E}{\partial c} = - (0.01) (-167.9)$$

$$= 1.679$$

$$S4: m = m + \Delta m = 1 + (-11.920) = -10.920$$

$$c = c + \Delta c = -1 + 1.679 = 0.679$$

Iteration - 2:

$$S1: [7.1, 174] \quad \eta = 0.01, \quad m = 10.92, \quad c = 0.67$$

$$S2: \frac{\partial E}{\partial m} \Big|_{m=-10.92} = (174 - (10.92)(7.1) - 0.67(7.1))$$

$$= 1781.056$$

$$\frac{\partial E}{\partial c} \Big|_{c=0.679} = - (174 - (-10.92)(7.1))$$

$$= 250.853$$

$$S3: \Delta m = -\eta \frac{\partial E}{\partial m} = (-0.01) \times (1781.056)$$

$$= -17.810$$

$$\Delta c = -\eta \frac{\partial E}{\partial c} = - (0.01) (-250.853)$$

$$= 2.508$$

$$S4: m = m + \Delta m = -10.92 - 17.81$$

$$= -28.73$$

$$c = c + \Delta c$$

$$= 0.679 + 2.508$$

$$= 3.187$$