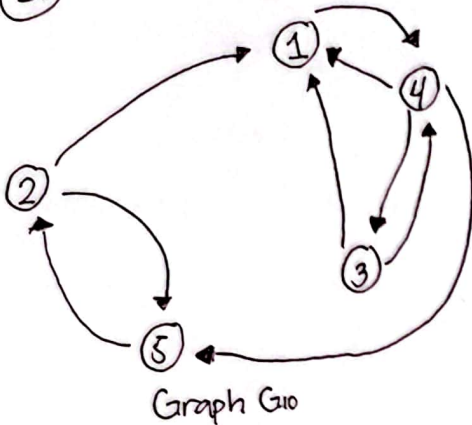


# Exercise

Give the formal description of the directed graph below.

1.



$$G_{10} = (V_{10}, E_{10})$$

$$V_{10} = \{1, 2, 3, 4, 5\}$$

$$E_{10} = \{(1, 2), (2, 1), (2, 5), (5, 2), (1, 4), (4, 1), (3, 4), (4, 3), (3, 1), (1, 3), (4, 5), (5, 4)\}$$

$$\text{Paths} = \{1, 4, 5, 2\}$$

length is 3

Simple path or

$$V = \{1, 4, 5, 2\}$$

length=3

$$V = \{2, 1, 4, 5\}$$

length=3

$$V = \{5, 2, 1, 4\}$$

length=3

$$V = \{4, 5, 2, 1\}$$

length=3

$$V = \{3, 4, 5, 2, 1\}$$

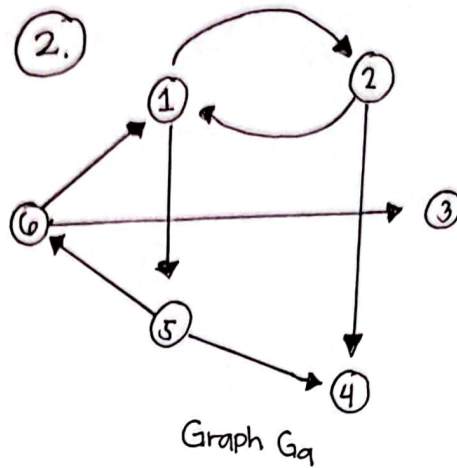
length=4

$$\text{Simple cycle} = \{1, 4, 5, 2, 1\},$$

$$\{4, 3, 1, 4\}, \{5, 2, 1, 4, 5\},$$

$$\{2, 1, 4, 5, 2\}$$

2.



$$G_9 = (V_9, E_9)$$

$$V_9 = \{1, 2, 3, 4, 5, 6\}$$

$$E_9 = \{(1, 2), (2, 1), (1, 3), (3, 1), (1, 5), (5, 1), (2, 4), (4, 2), (3, 6), (6, 3), (5, 4), (4, 5)\}$$

$$\text{Paths} = \{1, 2, 4\}$$

length is 2

Simple path or  $V = \{1, 2, 4\}$ , length = 2

$$V = \{1, 5, 4\}$$

length = 2

$$V = \{6, 1, 5, 4\}$$

length=3

$$V = \{1, 5, 6\}$$

length=2

$$V = \{5, 6, 1\}$$

length=2

$$\text{Simple cycle} = \{1, 5, 6, 1\}, \{5, 6, 1, 5\},$$

$$\{6, 1, 5, 6\}$$

①

Indegree of

	no. of indegree
Node 1 : $V = (2, 3, 4)$	3
Node 2 : $V = (5)$	1
Node 3 : $V = (4)$	1
Node 4 : $V = (1, 3)$	2
Node 5 : $V = (2, 4)$	2

Out degree of

	no. of outdegree
Node 1 : $V = \{4\}$	1
Node 2 : $V = (2, 5)$	2
Node 3 : $V = (1, 4)$	2
Node 4 : $V = (1, 3, 5)$	3
Node 5 : $V = (2)$	1

adjacent to: of

- Node 1 :  $(2, 3, 4)$
- Node 2 :  $(5)$
- Node 3 :  $(4)$
- Node 4 :  $(1, 3)$
- Node 5 :  $(2, 4)$

adjacent from:

- Node 1 :  $(4)$
- Node 2 :  $(1, 5)$
- Node 3 :  $(1, 4)$
- Node 4 :  $(1, 3, 5)$
- Node 5 :  $(2)$

The edges incident to:

- Node 1 :  $(1, 4), (2, 1), (3, 1), (4, 1)$
- Node 2 :  $(2, 1), (2, 5), (5, 2)$
- Node 3 :  $(3, 1), (3, 4), (4, 3)$
- Node 4 :  $(1, 4), (4, 1), (4, 2), (3, 4), (4, 5)$
- Node 5 :  $(5, 2), (2, 5), (4, 5)$

②

Indegree of

	no. of indegree
Node 1 : $V = (2, 6)$	2
Node 2 : $V = (1)$	1
Node 3 : $V = (6)$	1
Node 4 : $V = (2, 5)$	2
Node 5 : $V = (1)$	1
Node 6 : $V = (5)$	1

Out degree of

	Number of out degree:
Node 1 : $V = (2, 5)$	2
Node 2 : $V = (4, 1)$	2
Node 3 : $V = \text{None}$	0
Node 4 : $V = \text{None}$	0
Node 5 : $V = (4, 6)$	2
Node 6 : $V = (1, 3)$	2

adjacent to:

- Node 1 :  $(2, 6)$
- Node 2 :  $(1)$
- Node 3 :  $(6)$
- Node 4 :  $(2, 5)$
- Node 5 :  $(1)$
- Node 6 :  $(5)$

adjacent from:

- Node 1 :  $(2, 5)$
- Node 2 :  $(4, 1)$
- Node 3 :  $\text{None}$
- Node 4 :  $\text{None}$
- Node 5 :  $(4, 6)$
- Node 6 :  $(1, 3)$

The edges incident to:

- Node 1 :  $(1, 2), (2, 1), (1, 5), (6, 1)$
- Node 2 :  $(2, 1), (1, 2), (1, 5)$
- Node 3 :  $(6, 3)$
- Node 4 :  $(2, 4), (5, 4)$
- Node 5 :  $(5, 4), (1, 5), (5, 6)$
- Node 6 :  $(6, 1), (5, 6)$