

2020-2021学年秋季学期

自然语言处理

Natural Language Processing



授课教师：胡玥

助 教： 于静

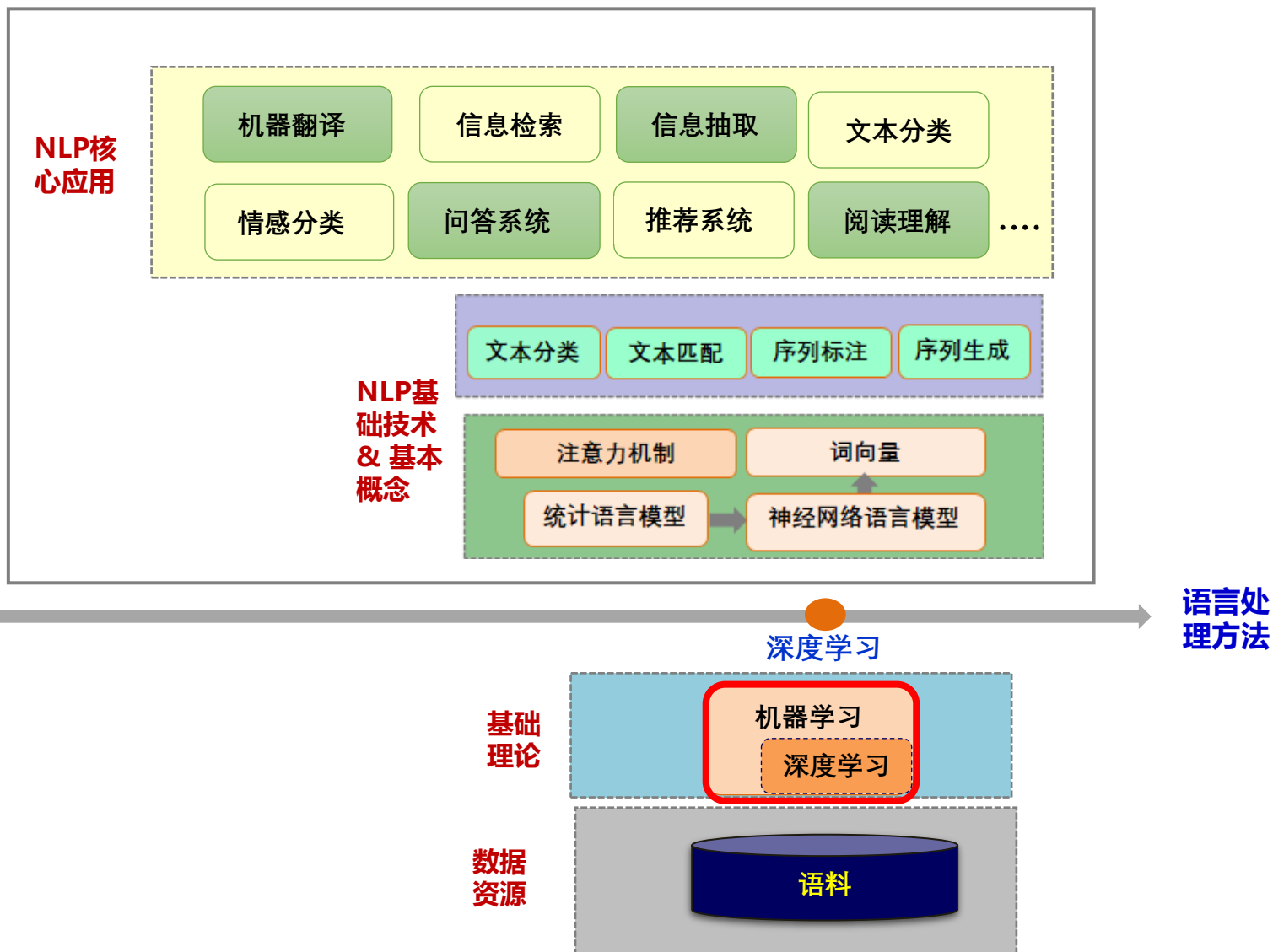
自然语言处理
Natural Language Processing

第 6 章 图卷积神经网络

授课教师：胡玥

授课时间：2020.9

基于深度学习的自然语言处理课程内容



概 要

本章主要内容：

介绍图卷积神经网络（GNN）的基本概念，模型结构

本章教学目的：

了解并掌握图卷积神经网络（GNN）的相关知识

内 容 提 要

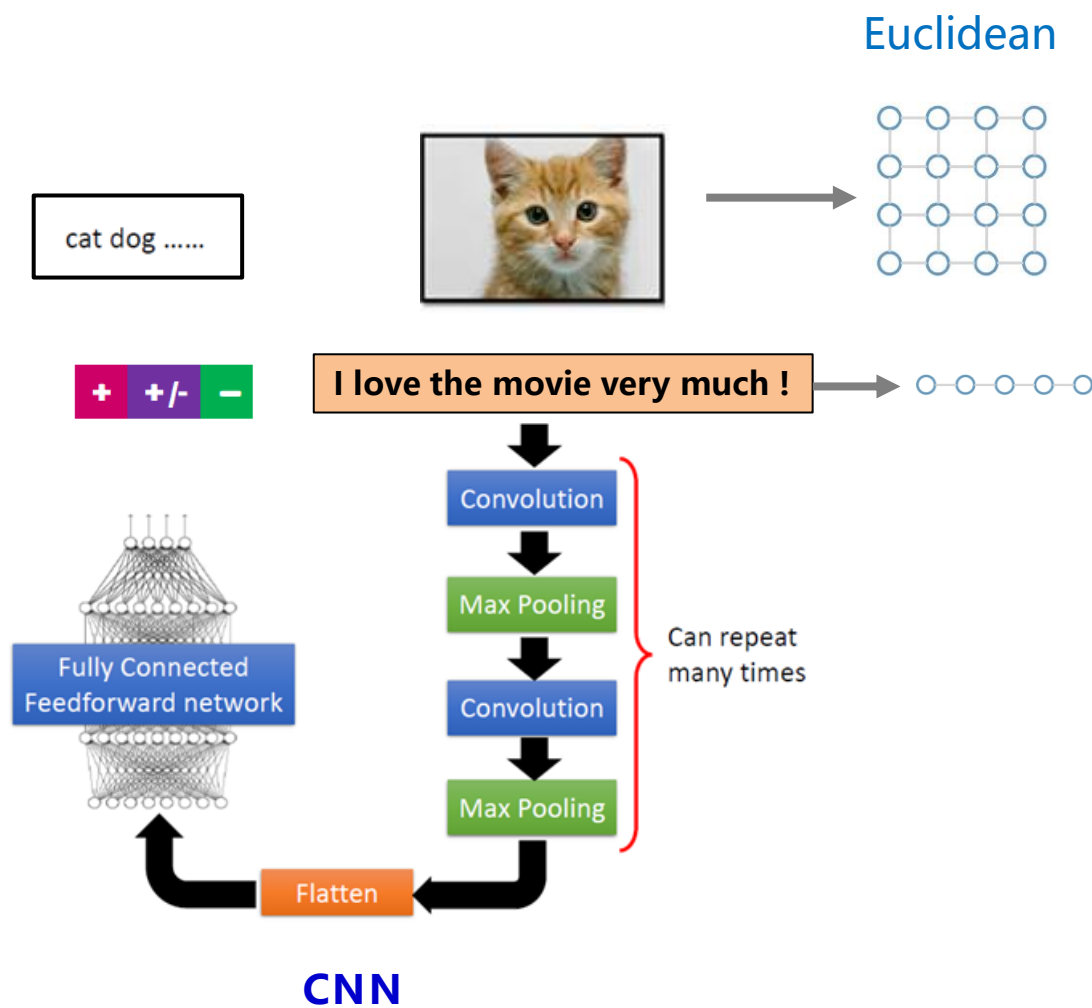
6.1 概述

6.2 Spatial-based GNN

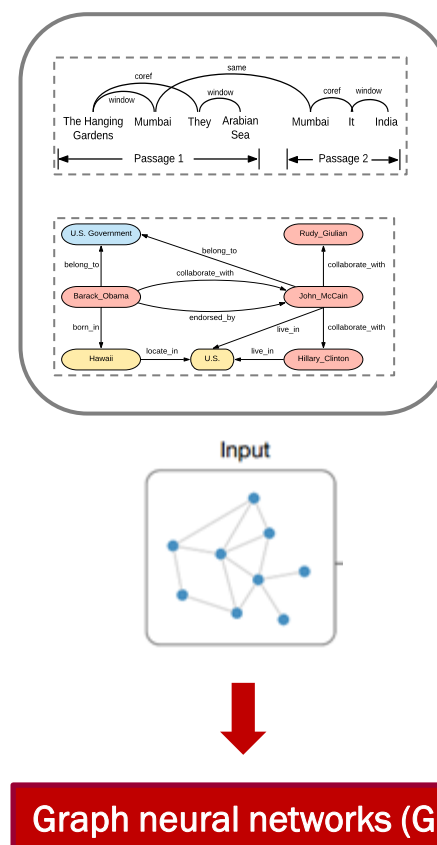
6.3 GNN 变形

6.1 概述

问题引入:

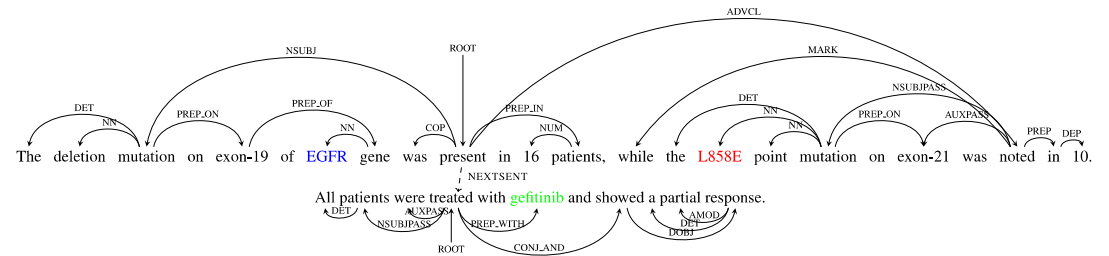
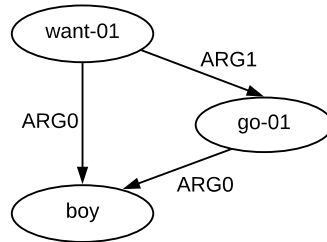


Non-Euclidean

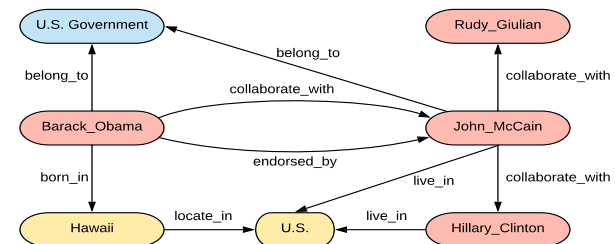
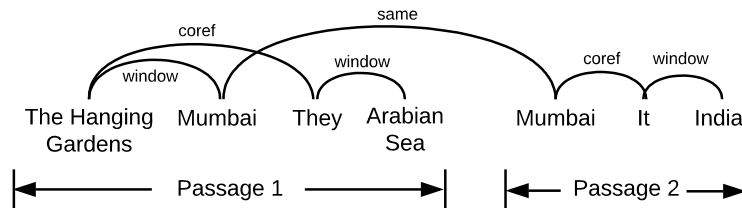


6.1 概述

GNN in NLP



Graph neural networks (GNN)

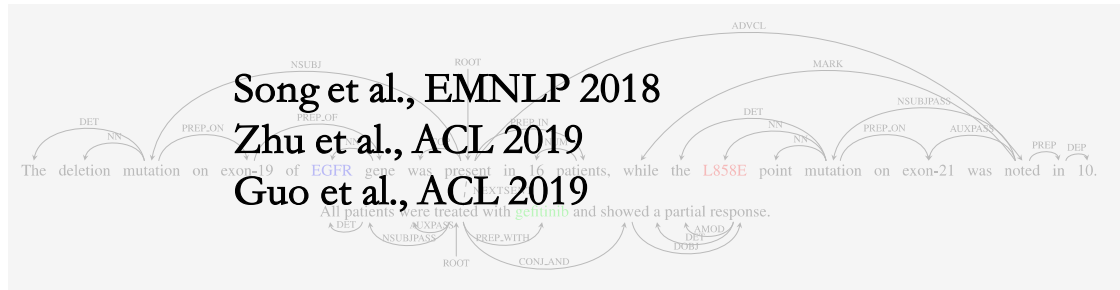


■ ■ ■

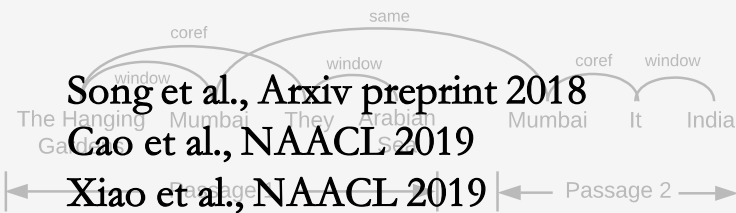
6.1 概述

GNN in NLP

Song et al., ACL 2018
Song et al., TACL 2019
Ding et al., ACL 2019
Tu et al., ACL 2019



Graph neural networks (GNN)



6.1 概述

图卷积神经网络

■ Spectral-based Graph Convolutional neural Networks

Define Convolution in Spectral domain , Convolutional is defined via graph Fourier transform and Convolutional theorem.

Challenge : Convolution filter define in spectral domain (not in vertex domain)

■ Spatial-based Graph Convolutional neural Networks

Define Convolution in the vertex domain , Convolutional is defined as a weighted average function over all vertices located in the neighborhood of target vertex.

Challenge : The size of neighborhood varies remarkably across nodes

内 容 提 要

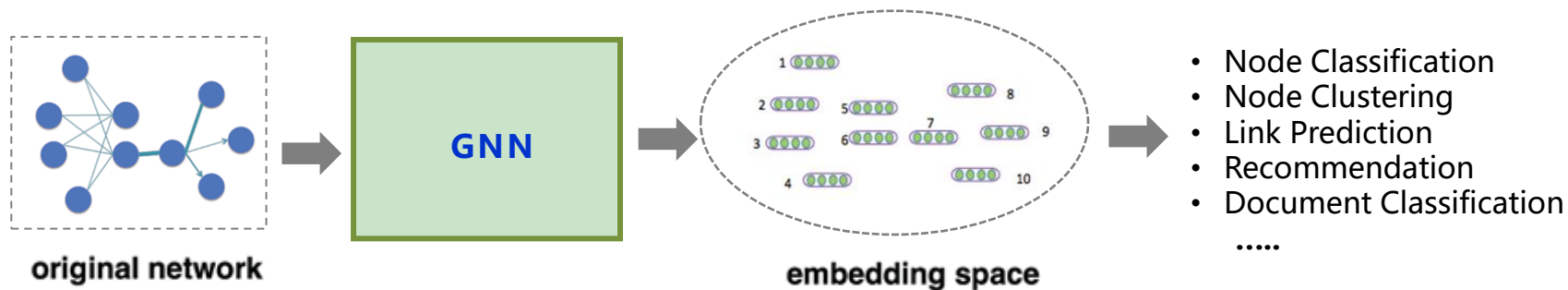
6.1 概述

6.2 Spatial-based GNN

6.3 GNN 变形

6.2 Spatial-based GNN

GNN Goal

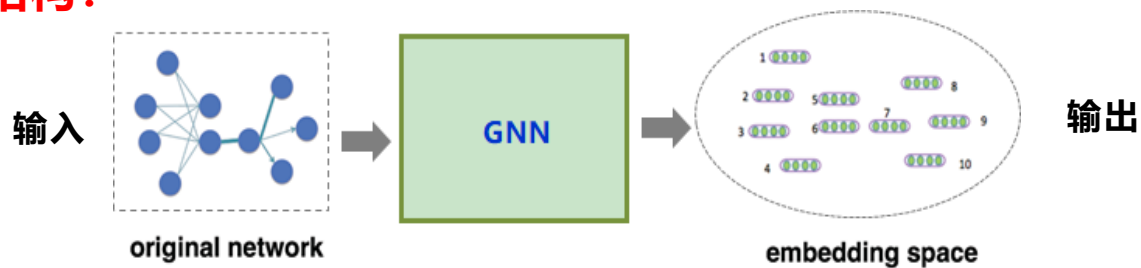


输入: original network

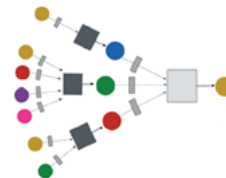
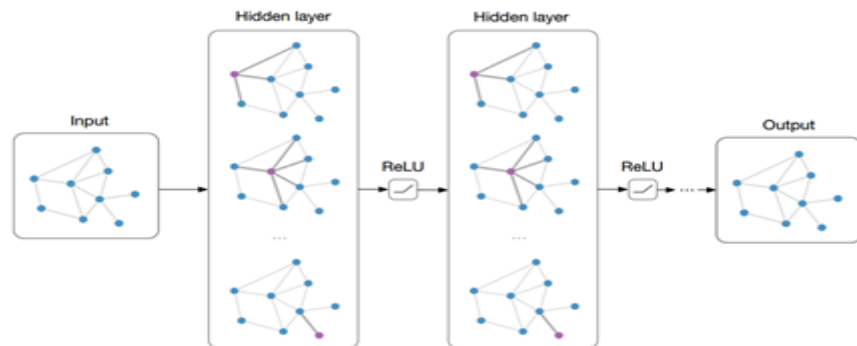
输出: Node representation set
每个表示带有原图的特征信息

6.2 Spatial-based GNN

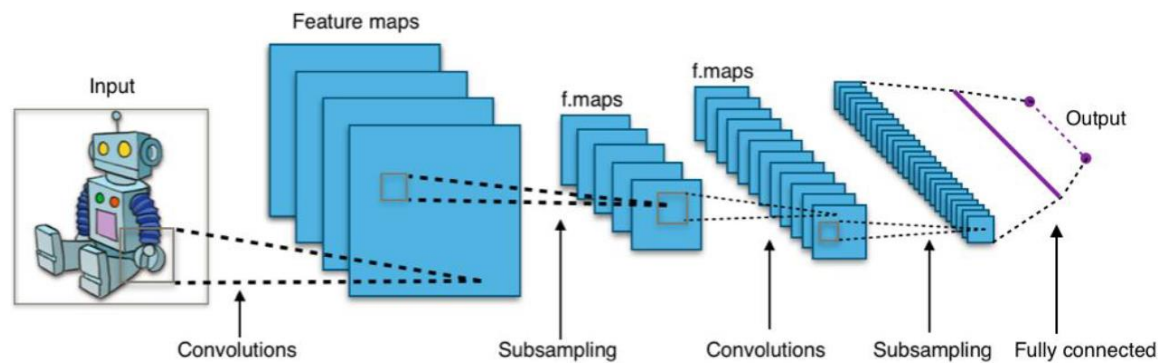
GNN模型结构:



GNN



CNN



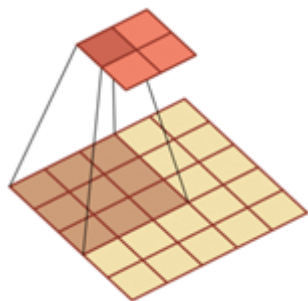
- 卷积层
Weight sharing
- 池化层
Reduce the number of parameters

6.2 Spatial-based GNN

GNN参数如何确定

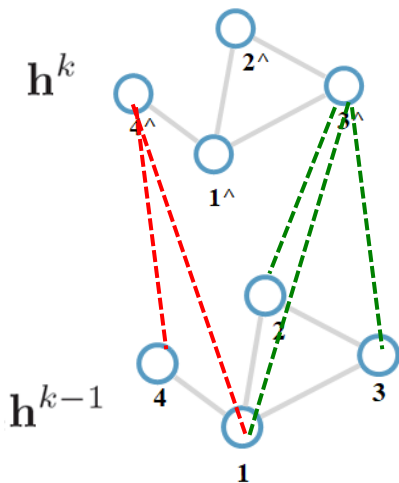
■ 参数个数

CNN



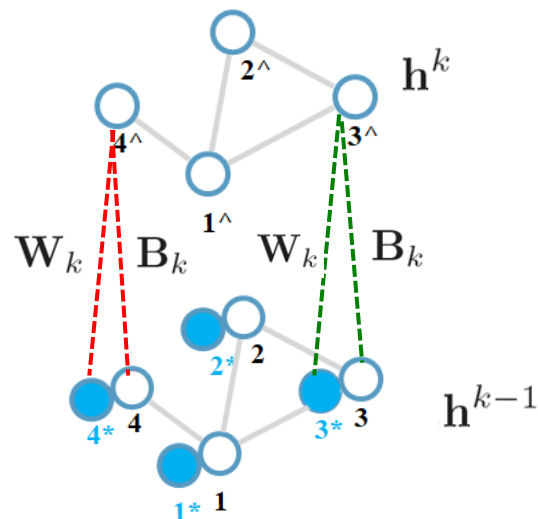
L 层到 L+1 对于同一个卷积核共享一组参数
(参数个数固定)

GNN



问题：邻接节点个数不确定

如何解决？



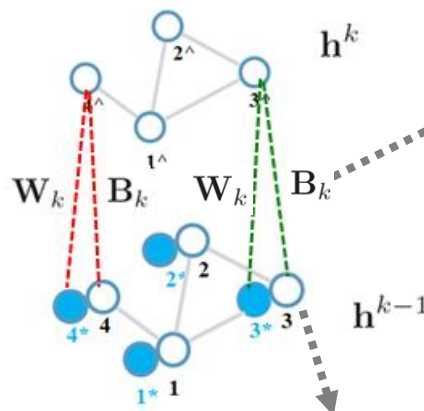
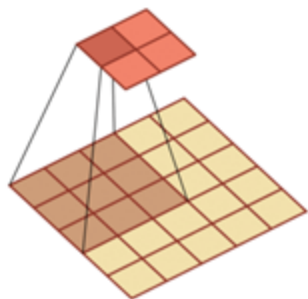
实心结点是对应的空心结点的邻接结点聚集

6.2 Spatial-based GNN

参数维度

$$\mathbf{X}^{(h^{k-1})} \times \mathbf{B} = \mathbf{X}^{(h^k)}$$

h^k : feature matrix $\mathbf{X}^{(h^k)} \in \mathbb{R}^{N \times K}$



参数B

	k 1	k 2	k 3	k 4
w 1	0.1	0.7	1.2	1.1
w 2	0.3	0.4	0.3	0.1
w 3	0.5	0.3	1.5	0.4
w 4	1.0	0.1	0.2	0.5
w 5	2.0	0.4	0.1	2.4

以X为例, X^* 同理

X^* 为 X 的邻接聚集结点

h^{k-1} : weight matrix $\mathbf{B} \in \mathbb{R}^{M \times K}$

图上结点X

	f1	f2	f3	f4	f5
Node 1	0.1	0.7	1.2	1.1	0.9
Node 2	0.3	0.4	0.3	0.1	1.2
Node 3	0.5	0.3	1.5	0.4	0.6
Node 4	1.0	0.1	0.2	0.5	0.1

h^{k-1} : feature matrix $\mathbf{X} \in \mathbb{R}^{N \times M}$

参数: $\mathbf{W}, \mathbf{B} \in \mathbb{R}^{M \times K}$

M: $\mathbf{X}^{(h^{k-1})}$ 特征维度

K: $\mathbf{X}^{(h^k)}$ 特征维度

- Weight sharing
- Reduce the number of parameters

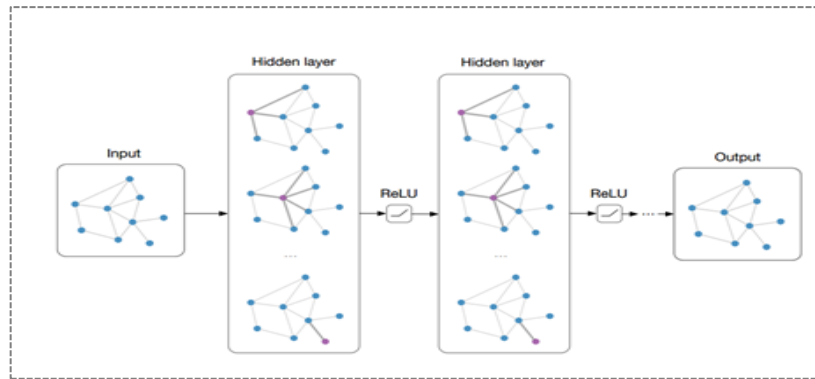
6.2 Spatial-based GNN

GNN 卷积步骤:

Step1: Aggregation

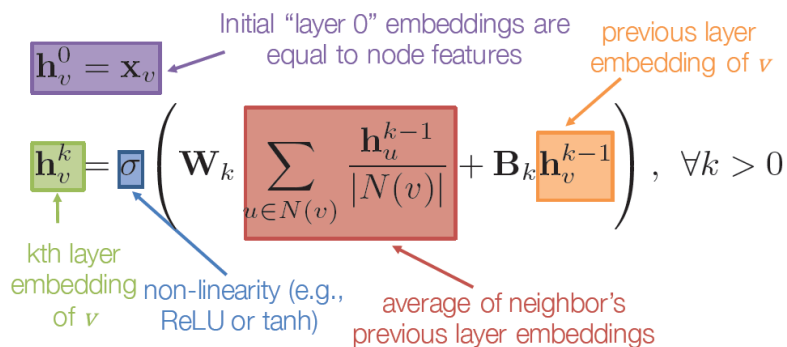
Step2: Transformation

GNN 池化 ?



Basic GNN

$$\mathbf{h}_v^k = \sigma \left(\mathbf{W}_k \sum_{u \in N(v)} \frac{\mathbf{h}_u^{k-1}}{|N(v)|} + \mathbf{B}_k \mathbf{h}_v^{k-1} \right)$$



GCN

$$\mathbf{h}_v^k = \sigma \left(\mathbf{W}_k \sum_{u \in N(v) \cup v} \frac{\mathbf{h}_u^{k-1}}{\sqrt{|N(u)| |N(v)|}} \right)$$

use the same transformation matrix for self and neighbor embeddings

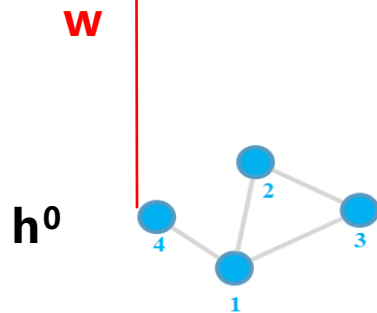
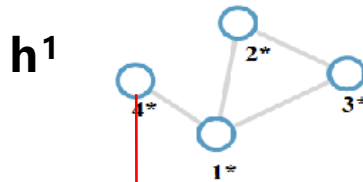
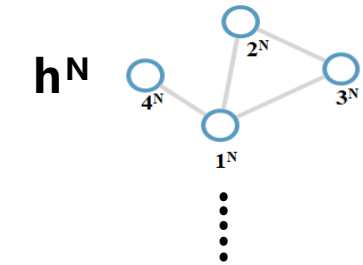
instead of simple average, normalization varies across neighbors

- More parameter sharing.
- Down-weights high degree neighbors.

例:

Output

$$\mathbf{h}_v^k = \sigma \left(\mathbf{W}_k \sum_{u \in N(v)} \frac{\mathbf{h}_u^{k-1}}{|N(v)|} + \mathbf{B}_k \mathbf{h}_v^{k-1} \right)$$



Step2: Transformation

	<i>f1</i>	<i>f2</i>	<i>f3</i>	<i>f4</i>	<i>f5</i>		<i>k 1</i>	<i>k 2</i>	<i>k 3</i>	<i>k 4</i>		<i>k1</i>	<i>k 2</i>	<i>k3</i>	<i>k4</i>
Node 1	1.8	0.8	...			<i>w 1</i>	0.1	0.7	1.2	1.1	Node 1	2.8	4.8	...	
Node 2	0.6	1.0	...			<i>w 2</i>	0.3	0.4	0.3	0.1	Node 2	0.6	4.0	...	
Node 3	...					<i>w 3</i>	0.5	0.3	1.5	0.4	Node 3	...			
Node 4	...					<i>w 4</i>	1.0	0.1	0.2	0.5	Node 4	...			
						<i>w 5</i>	2.0	0.4	0.1	2.4					

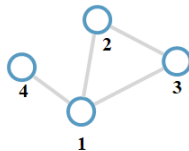
feature matrix $\mathbf{X}' \in \mathbb{R}^{N \times M} \times$ weight matrix $\mathbf{W} \in \mathbb{R}^{M \times K} =$ feature matrix $\mathbf{H} \in \mathbb{R}^{N \times K}$

Step1: Aggregation

	Node 1	Node 2	Node 3	Node 4		<i>f1</i>	<i>f2</i>	<i>f3</i>	<i>f4</i>	<i>f5</i>		<i>f1</i>	<i>f2</i>	<i>f3</i>	<i>f4</i>	<i>f5</i>
Node 1	0	1	1	1	Node 1	0.1	0.7	1.2	1.1	0.9	Node 1	1.8	0.8	...		
Node 2	1	0	1	0	Node 2	0.3	0.4	0.3	0.1	1.2	Node 2	0.6	1.0	...		
Node 3	1	1	0	0	Node 3	0.5	0.3	1.5	0.4	0.6	Node 3	...				
Node 4	1	0	0	0	Node 4	1.0	0.1	0.2	0.5	0.1	Node 4	...				

adjacency matrix $\mathbf{A} \in \mathbb{R}^{N \times N} \times$ feature matrix $\mathbf{X} \in \mathbb{R}^{N \times M} =$ feature matrix $\mathbf{X}' \in \mathbb{R}^{N \times M}$

\mathbf{h}^0



Input:

	Node 1	Node 2	Node 3	Node 4		<i>f1</i>	<i>f2</i>	<i>f3</i>	<i>f4</i>	<i>f5</i>
Node 1	0	1	1	1	Node 1	0.1	0.7	1.2	1.1	0.9
Node 2	1	0	1	0	Node 2	0.3	0.4	0.3	0.1	1.2
Node 3	1	1	0	0	Node 3	0.5	0.3	1.5	0.4	0.6
Node 4	1	0	0	0	Node 4	1.0	0.1	0.2	0.5	0.1

adjacency matrix \mathbf{A} feature matrix $\mathbf{X} \in \mathbb{R}^{N \times M}$

6.2 Spatial-based GNN

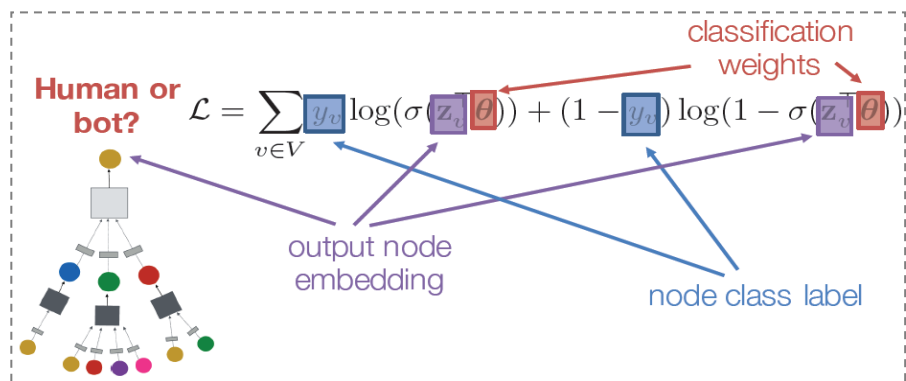
GNN模型训练:

$$\begin{aligned} \mathbf{h}_v^0 &= \mathbf{x}_v \\ \mathbf{h}_v^k &= \sigma \left(\mathbf{W}_k \sum_{u \in N(v)} \frac{\mathbf{h}_u^{k-1}}{|N(v)|} + \mathbf{B}_k \mathbf{h}_v^{k-1} \right), \quad \forall k \in \{1, \dots, K\} \\ \mathbf{z}_v &= \mathbf{h}_v^K \end{aligned}$$

trainable matrices
(i.e., what we learn)

在最后一层 (K层) 得到每个结点的表示后, 可以根据任务将其代入任何损失函数, 然后用梯度下降法训练参数

例1: 结点分类 (有监督)



例2: 相似结点表示相似 (无监督)

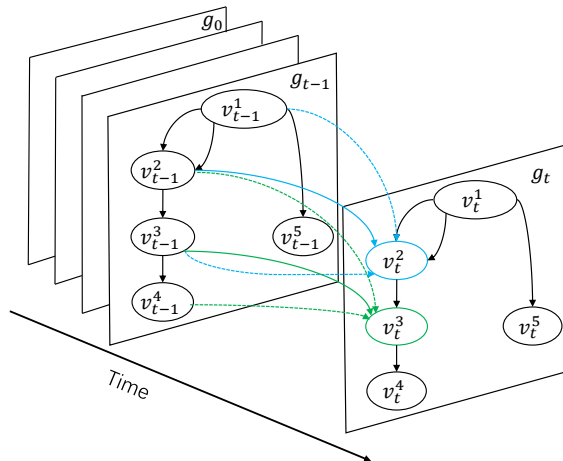
6.2 Spatial-based GNN

有向图的GNN:

GNN 卷积步骤:

Step1: Aggregation

Step2: Transformation



$$\mathbf{h}_{t-1}^k \longrightarrow \mathbf{h}_t^i$$

Step1: Aggregation

$$\begin{aligned} \mathbf{m}_t^{\uparrow i} &= \sum_{k \in \Omega_{\uparrow}(i)} \mathbf{h}_{t-1}^k \\ \mathbf{m}_t^{\downarrow i} &= \sum_{k \in \Omega_{\downarrow}(i)} \mathbf{h}_{t-1}^k \\ \mathbf{m}_t^i &= [\mathbf{m}_t^{\uparrow i}; \mathbf{m}_t^{\downarrow i}] \end{aligned}$$

Step2: Transformation

$$\mathbf{h}_t^i = \sigma(\mathbf{W}_g^m \mathbf{m}_t^i + \mathbf{W}_g^x \mathbf{x}_t^i + \mathbf{b}_g)$$

内 容 提 要

6.1 概述

6.2 Spatial-based GNN

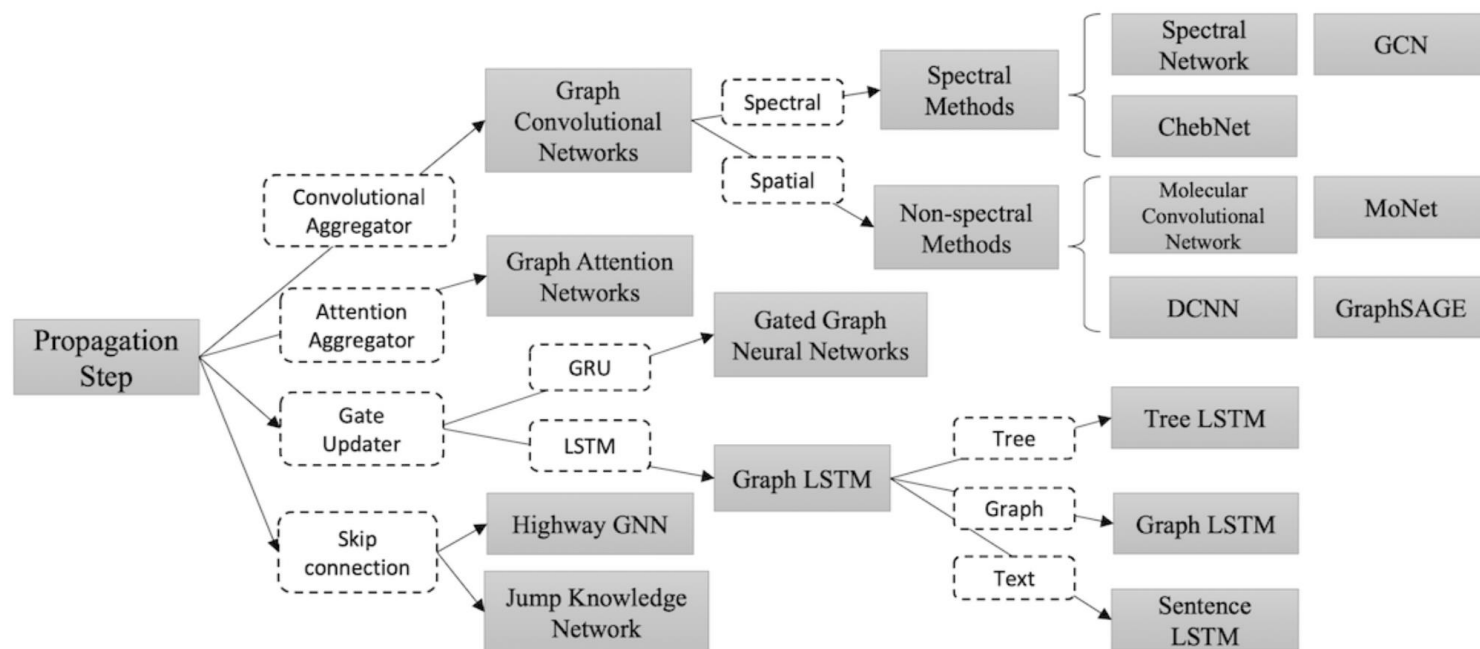
6.3 GNN 变形

6.3 GNN变形

GNN变形:

根据结点聚集和层级连接方法的不同有大量不同形式的GNN

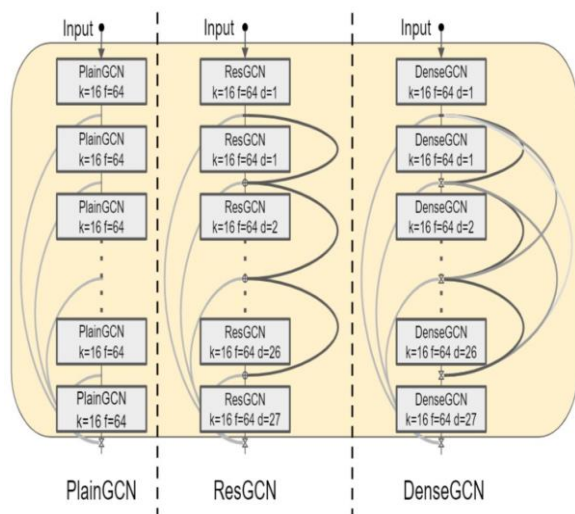
■ GNN Models based on Propagation Step



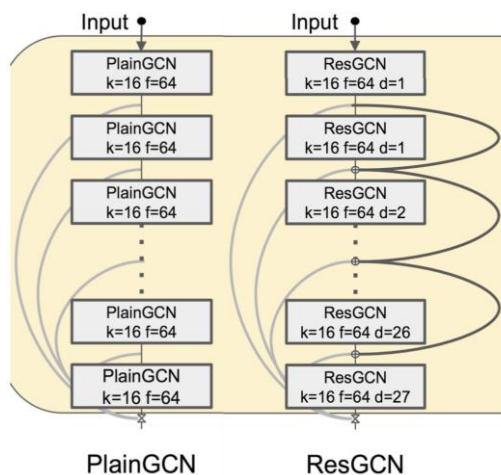
6.3 GNN变形

■ GNN Models based on Connection

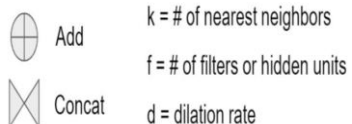
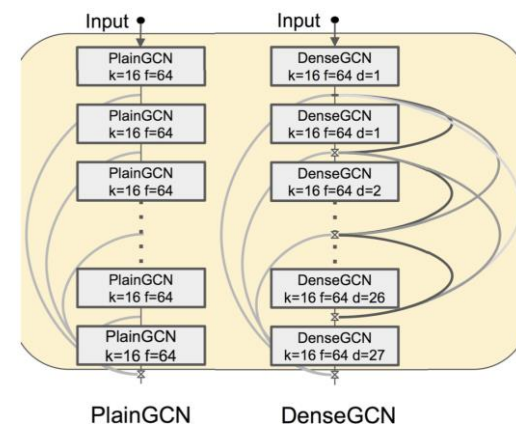
Deep Graph Convolutional Networks



DGCN: Residual Connections



DGCN: Dense Connections



参考文献:

Zhuan Zhou, Graph Convolutional Neural Networks: An introduction
Tutorial ,2018

Jing Yu , Deep Learning on Graphs with Graph Convolutional Networks

Yue Zhang , Graph Neural Networks in NLP

在此表示感谢!

谢谢各位！



Q&A