

Knowledge Representation

Nada Mimouni

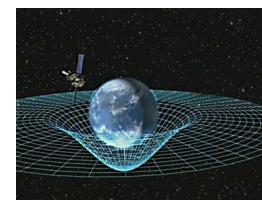
based on slides by: Fabian M. Suchanek

Overview

- Entities & Classes
- Relations
- Binary Relations
- Schema
- Knowledge Graphs
- Reification
- Canonic Entities
- Reality

Entity

An **entity** (also: resource) is any particular object of the world or imagination, be it abstract or concrete.



>digression

(The exact definition of "entity" is a philosophical conundrum. Don't worry about it.)

Digression: Entities



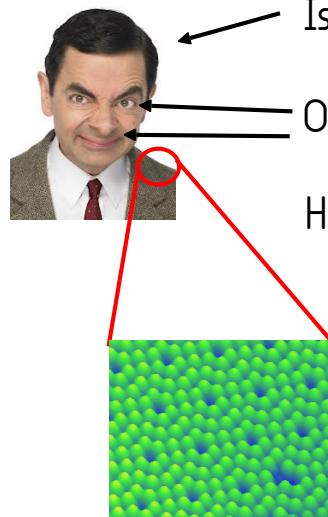
Is this an entity?



Or this?

How many entities are there?

Digression: Entities



Is this an entity?

Or this?

How many entities are there?

Isn't everything just atoms?

>digression

Digression: Identity



Over time, all parts of a ship are replaced at some point of time.
Then, is it still the same ship?

[see: Theseus's ship on Wikipedia](#)

Digression: Identity



Over time, all parts of a ship are replaced at some point of time.
Then, is it still the same ship?

[see: Theseus's ship on Wikipedia](#)

Humans replace their cells every 7 years.

New York Times

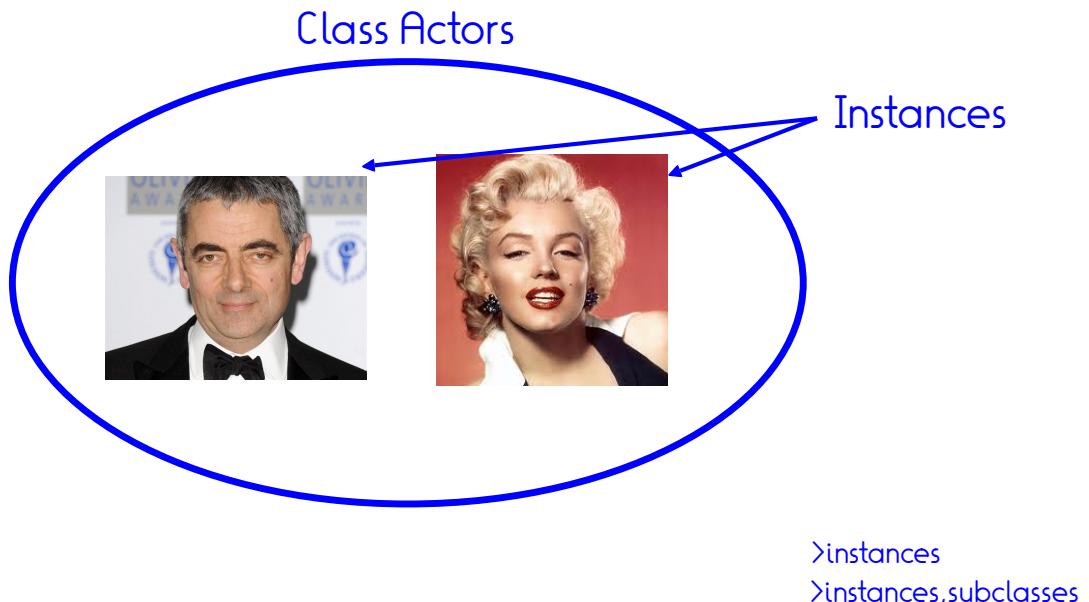
Class

A **class** (also: **concept**) is a set of similar entities.

Entities that are not classes (and not literals, relations, ids) are called **instances** (or **common entities**).

Classes:

- Actors
- Cars
- Cities
- Rivers
- Universities
- Theories
- ...

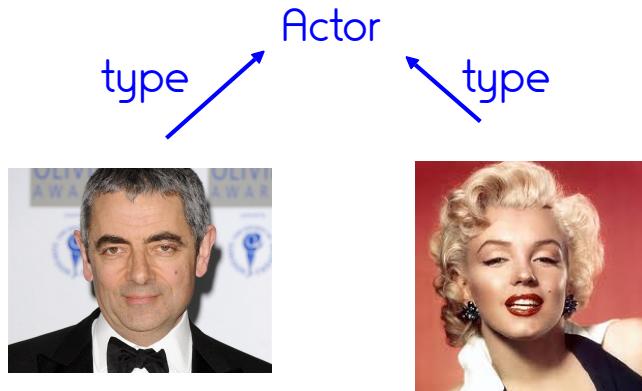


(The exact definition of "class" is a philosophical conundrum, too. See later in this lecture.)

Def: Instance of a class

An entity is an **instance of a class**

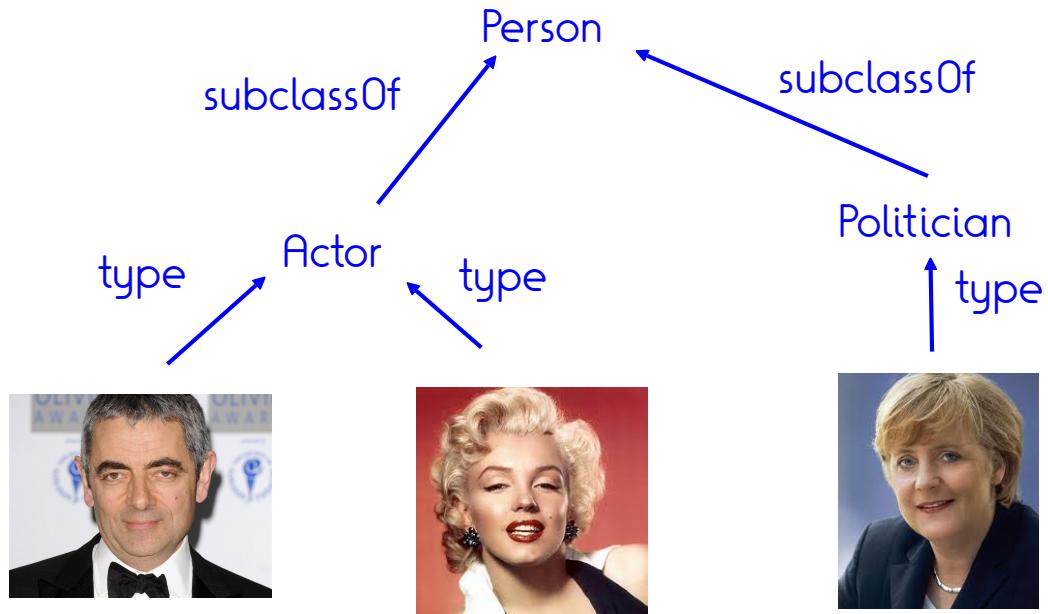
(also: belongs to a class, has the type, is of the class),
if the entity is an element of that class.



Def: Subclass, Taxonomy

A **class** is a subclass of another class, if all instances of the first class are also instances of the second class.

A **taxonomy** is a hierarchy of classes.



>examples

Cheat Sheet

If we can say...	then...
• "a/an X", "every X"	X is a class
• "Xs" (plural)	X is a class
• "This is X"	X is an instance of some class
• "X is a Y"	X is an instance of Y
• "Every X is a Y"	X is a subclass of Y

>examples

Cheat Sheet

If we can say...	then...
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Try it out: city, Elvis, Coli bacteria, Ford, time

>examples

Examples

iPhone -> smartphone

finger -> hand

apple -> orange

flower -> plant

Paris -> city

fruit -> food

France -> Europe

Paris -> France

city -> country

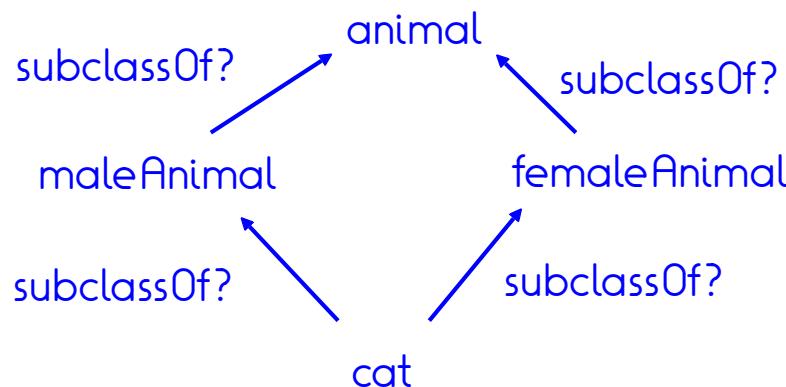
Examples

iPhone -> smartphone	subclass
finger -> hand	partof
apple -> orange	sibling
flower -> plant	subclass
Paris -> city	type
fruit -> food	subclass
France -> Europe	locatedIn
Paris -> France	locatedIn
city -> country	domain and range of "locatedIn"

Examples

Consider a taxonomy of the animal kingdom.

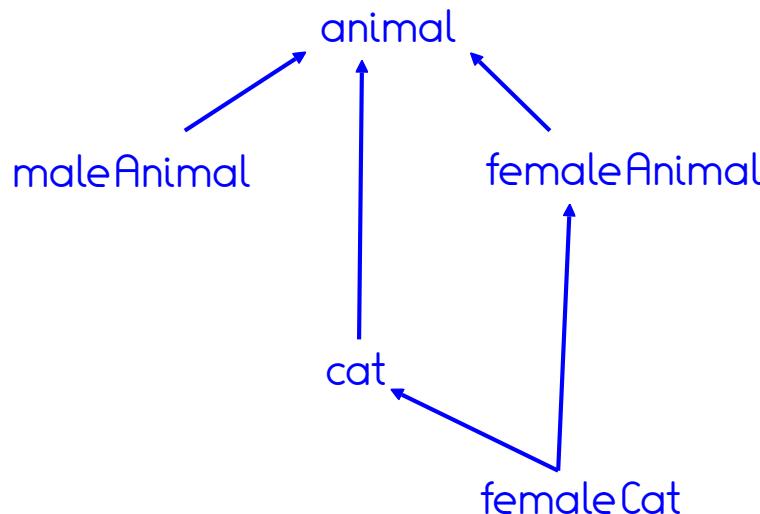
How do we deal with "male" and "female"?



Examples

Consider a taxonomy of the animal kingdom.

How do we deal with "male" and "female"?



Intuition: Relations

A relation is like a table.

Relation "born":

Person	City	Year
Atkinson	Consett	1955
Monroe	Los Angeles	1926
...		

Def:Relation

A **relation** (also: predicate) over classes is a subset of their cartesian product. The classes are called the **domains** of the relation.
The number of classes is called the **arity** of the relation.

$$R \subseteq C_1 \times C_2 \times \dots \times C_n$$

$$\text{born} \subseteq \text{person} \times \text{city} \times \text{year}$$

$$\begin{aligned}\text{born} = & \{ <\text{Atkinson}, \text{Consett}, 1955>, \\ & <\text{Monroe}, \text{Los Angeles}, 1926>, \dots \}\end{aligned}$$

>digression (tough)

Digression: Semantics

A relation is **any** subset of the cartesian product. It does not have to correspond to a real-world relation. Its name is arbitrary.

born= {<Atkinson, Consett, 1955>, <Monroe, LosAngeles, 1926>, ...}

Digression: Semantics

The semantics/denotation of a symbol is
the “meaning” of the symbol,
i.e., the real world entity or tuples.

$$D(\text{Atkinson}) = \text{Rowan Atkinson}$$

Syntax

Semantics

$$D(\text{born}) = \{ \langle x, y, z \rangle \mid x \text{ was born in } y \text{ in year } z \}$$

Digression: Semantics

But these are again symbols.



$$D(\text{born}) = \{ \langle x, y, z \rangle \mid x \text{ was born in } y \text{ in year } z \}$$

What is their semantics?

Def: Binary Relation, Triple

A binary relation is a relation of arity 2.

$$\text{bornInCity} \subseteq \text{person} \times \text{city}$$

For binary relations, the first class is called the **domain** and the second class is called the **range**.

An element of a binary relation is called a **fact** (or: triple), and we usually visualize it by an arrow:

$$\text{bornInCity}(\text{Atkinson}, \text{Consett})$$



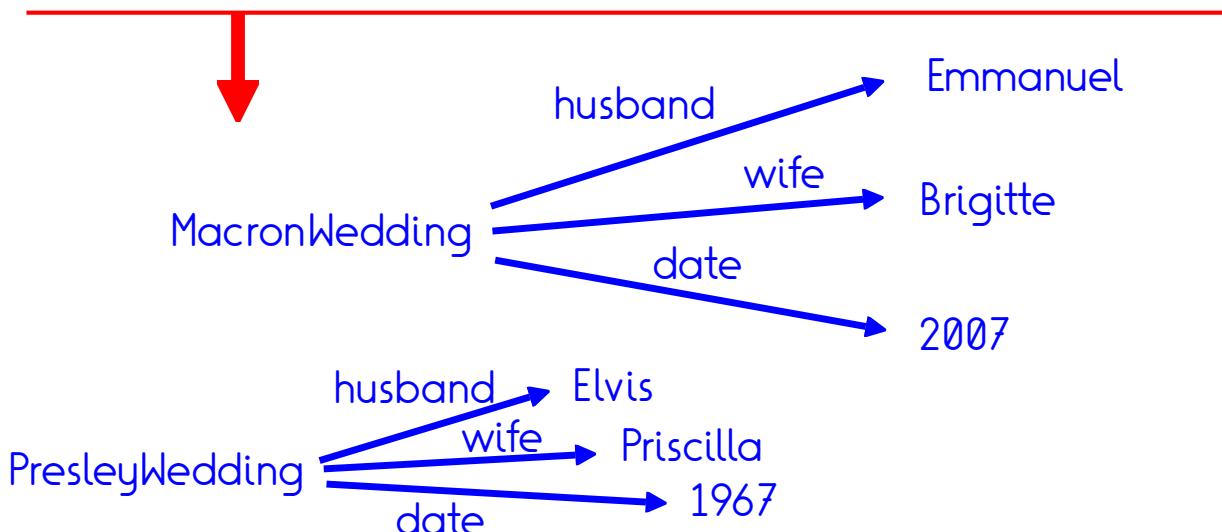
The first argument of a fact is the **subject**, the second the **object**.

>events

n-ary facts as binary facts

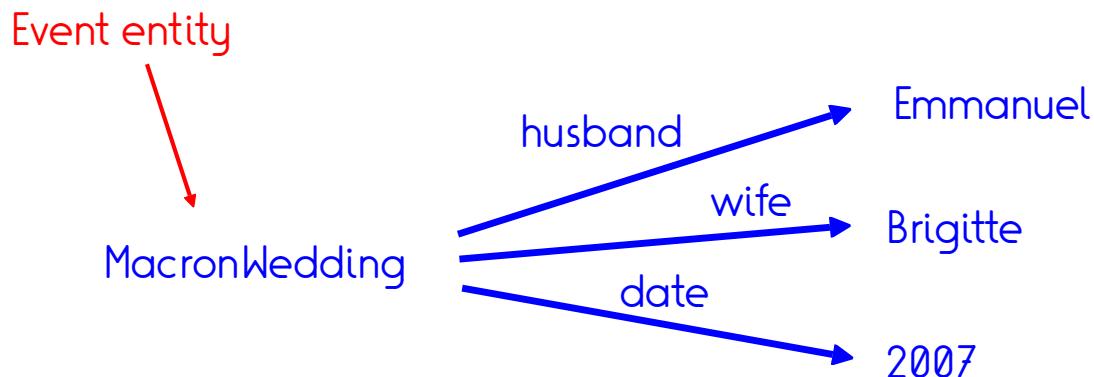
Every n-ary fact can be represented as binary facts.

WEDDINGS	Husband	Wife	WeddingDate
	Emmanuel	Brigitte	2007
	Elvis	Priscilla	1967



Def: Event Entity

An **event entity** represents an n-ary fact.



Task: Event Entities

Draw a knowledge graph for the following facts.

Irma loves Mr. Bean since 1955.

Mr. Bean drives with Irma to the cinema.

Irma and Mr. Bean watch "Titanic".

The movie is about the trip of the ship
"Titanic" from Europe to New York.

(There may be multiple solutions)

Binary relations are flexible

n-ary relations enforce the presence of all arguments:

born	Person	City	Year
	Atkinson	Consett	1955

Binary relations don't:



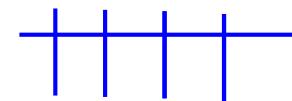
1955

Binary vs n-ary

Binary and n-ary relations can represent the same facts.



binary



n-ary

- more relations
- less arity
- more flexibility

- less relations
- more arity
- more control

Def: Inverse

The **inverse** of a binary relation r is a relation r' , such that $r'(x,y)$ iff $r(y,x)$.

$livesInCity \subseteq person \times city$

$livesInCity(Atkinson, Consett)$

inverses
of each
other

$hasInhabitant \subseteq city \times person$

$hasInhabitant(Consett, Atkinson)$

Def: Function

A **function** (also: functional relation) is a binary relation that has at most 1 object for each subject.

$$r \text{ functional} \equiv \forall x: |\{y : r(x,y)\}| \leq 1$$

hasNationality

hasSpouse (in medieval ages)

hasNumberOfTeeth

Def: Inverse Functional Rel.

An **inverse functional relation** is a relation whose inverse is functional.

$$r \text{ inv. functional} \equiv \forall y: |\{x : r(x,y)\}| \leq 1$$

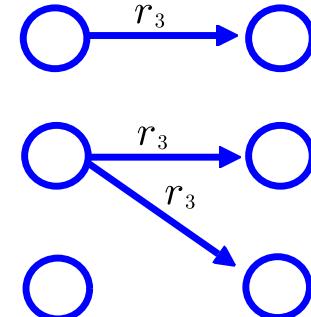
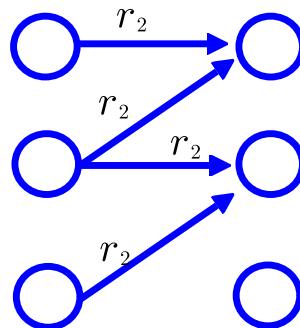
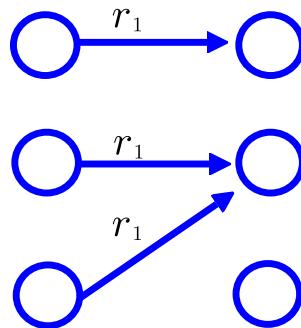
hasCitizen

hasSpouse (in medieval ages)

>task

Task: Functions

Which of the following relations are functional?



Digression: Equality

If two entities share the same object of an inverse functional relation, they are equal.

hasEmail(Bean,me @bean.com)

hasEmail(MrBean,me @bean.com)

$\Rightarrow MrBean = Bean$

born(Bean,1955)

born(MrBean,1955)

(Nothing follows)

Def: Name

A **name** (also: label) of an entity is a human-readable string attached to that entity. The entity is called the **meaning** of the name.



label

Name

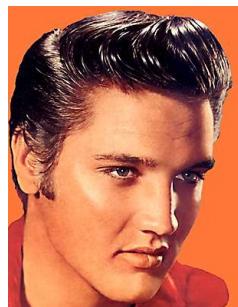
"Mr. Bean"

>ambiguity

Def: Synonymy

If an entity has multiple names,
the names are called ***synonymous***.

(The adjective for the names is "synonymous", each name is a "synonym", the phenomenon is called "synonymy")

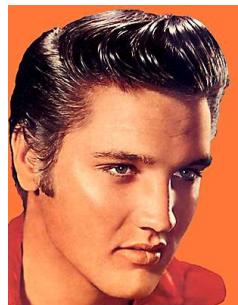


A diagram illustrating a mapping or relationship between labels and names. It consists of two blue arrows originating from the word "label". The top arrow points from "label" to the name "The King". The bottom arrow points from "label" to the name "Elvis".

Def: Ambiguity

If a name is attached to multiple entities,
the name is called **ambiguous**.

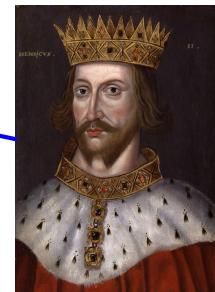
(The adjective for the names is "ambiguous", the phenomenon is called "ambiguity")



label

"The King"

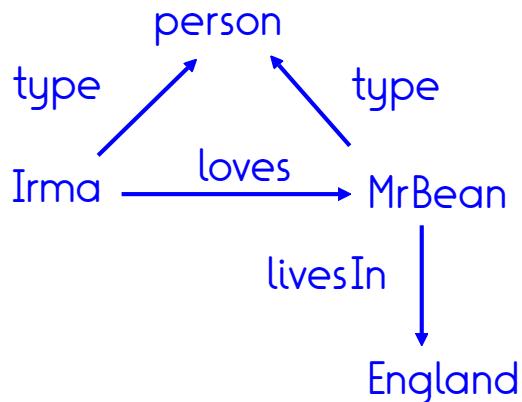
label



Def: Knowledge Graph

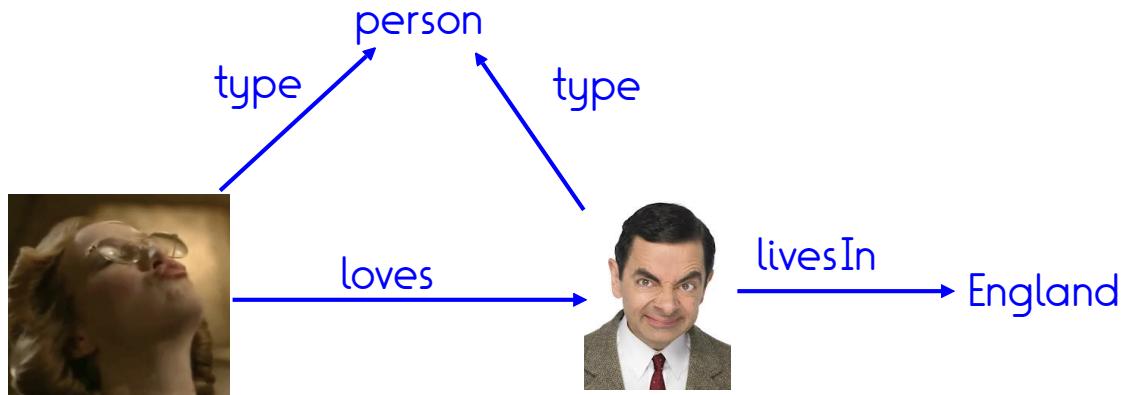
A **knowledge graph** (also: Entity-Relationship graph, Knowledge base, KB) is a directed labeled multi-graph that has an edge $x \rightarrow y$ with label r , iff $r(x,y)$.

*loves(Irma, MrBean)
type(Irma, person)
type(MrBean, person)
livesIn(MrBean, England)*



Def: Knowledge Graph

A **knowledge graph** (also: Entity-Relationship graph, Knowledge base, KB) is a directed labeled multi-graph that has an edge $x \rightarrow y$ with label r , iff $r(x,y)$.



-> schema

Def: Triple Store

A **triple store** is a table that contains a KB of binary relations in the form of 3 columns: subject, relation, object.

Subject	Relation	Object
Irma	loves	MrBean
Irma	type	person

(The middle column is often called "Predicate")

Popular triple stores are:

- BlazeGraph
- Jena
- Virtuoso
- ...or classical databases

->schema

Classes as binary relations

One way to represent a class is by the binary relations *type*, *subclassOf*.

$$\text{type} \subseteq \text{entity} \times \text{class}$$

$$\text{type}(\text{Atkinson}, \text{actor})$$

$$\text{subclassOf} \subseteq \text{class} \times \text{class}$$

$$\text{subclassOf}(\text{actor}, \text{person})$$

Person



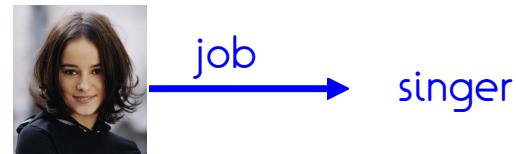
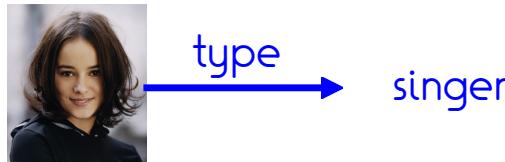
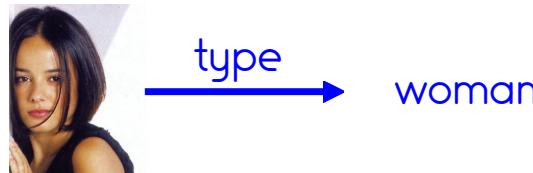
Actor



("entity" is the class of entities, "class" is the class of classes. See later in the lecture for details.)

Digression: Classes and Relations

A fact can be modeled as a class or as a relation.



>domain

Domains as binary relations

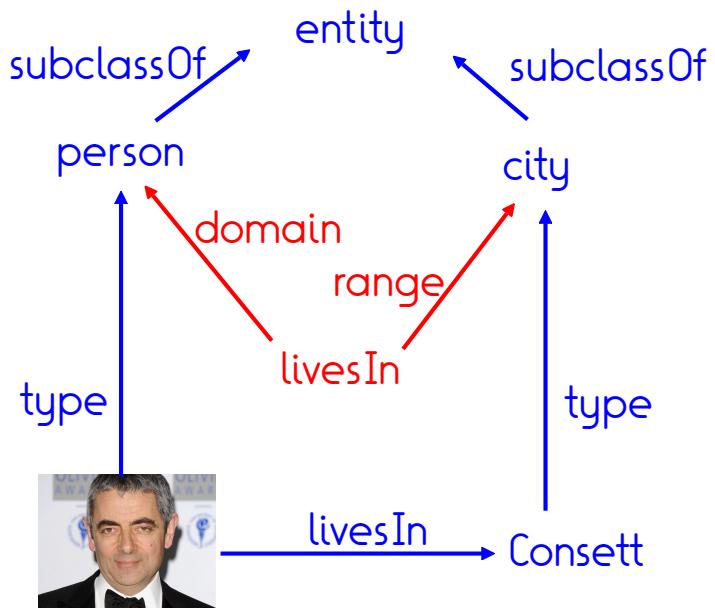
The domain and range of relations can be expressed by binary relations *domain* and *range*.

$\text{domain} \subseteq \text{relation} \times \text{class}$

$\text{domain}(\text{livesIn}, \text{person})$

$\text{range} \subseteq \text{relation} \times \text{class}$

$\text{range}(\text{livesIn}, \text{city})$

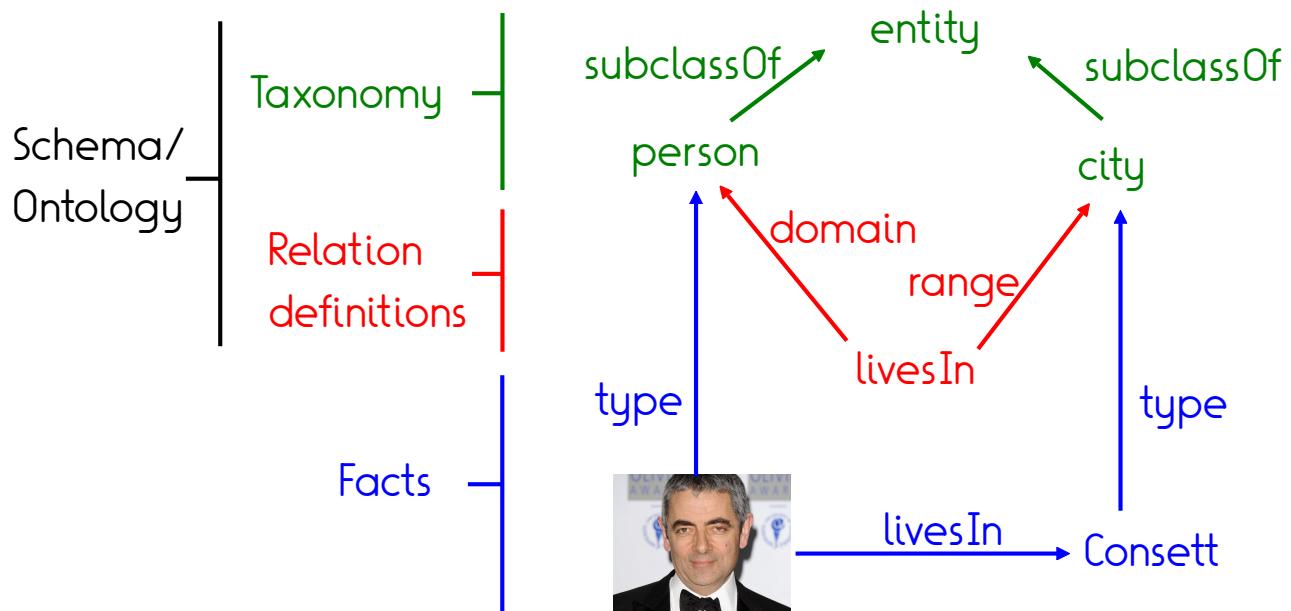


("relation" is the set of relations. See later in this lecture for details.)

Def: Schema

The **schema/ontology** is the part of a knowledge graph that consists of

- the taxonomy (= set of classes with their subclassOf-links)
- relation definitions (= a set of relations with domains and ranges)



Task: Schema

Define a schema for the domain of politics.

In that schema, express that Macron is the president of France, Merkel is the chancellor of Germany, and that Merkel loves Macron.

Digression: Task: Class entities

Draw a knowledge graph with the relations *domain* and *range*.
Can *domain* and *range* appear as nodes?

Digression: The problem with classes

`type(class, class)`

"The class "class" is a class"

`class ∈ class`

...in a naïve set-theoretical interpretation

`class = {cars, frenchPeople, class, ...}`

`class = {cars, frenchPeople, {cars, frenchPeople, { cars, ...}`

Digression: The problem with classes

We distinguish:

- 1) the class/concept/
generalization

The class of
French people



- 2) the extension
of the class

The extension of the
class of French people

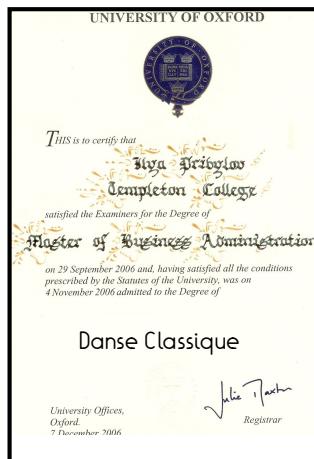
{Emmanuel Macron,
Alizee,
Napoleon Bonaparte,
Pierre Dupont, ...}

(This means that two classes can have the same extension and still be different.
Relations are treated in the same way. See [RDF Semantics](#) for a discussion.)

->canonic ->end

Reified statements

A **reified statement** is an entity that represents a statement. This phenomenon is called reification.



represents

Alizee

completed

Dance
School

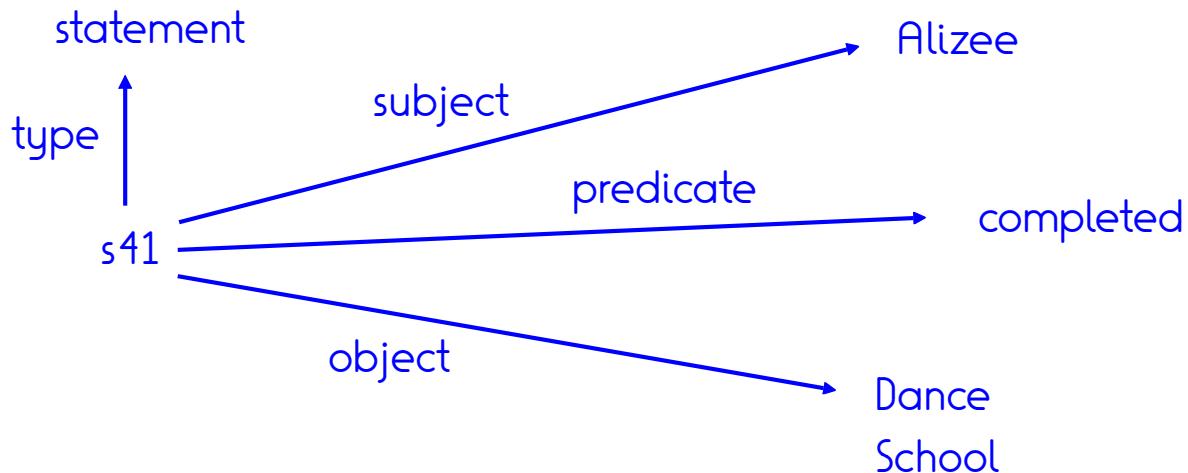
Reification Vocabulary

statement = class of reified statements

subject \subseteq *statement* \times *entity*

predicate \subseteq *statement* \times *relation*

object \subseteq *statement* \times *entity*



Example: Reification

hopes(Pierre, s42)

subject(s42, Alizee)

predicate(s42, type)

object(s42, single)

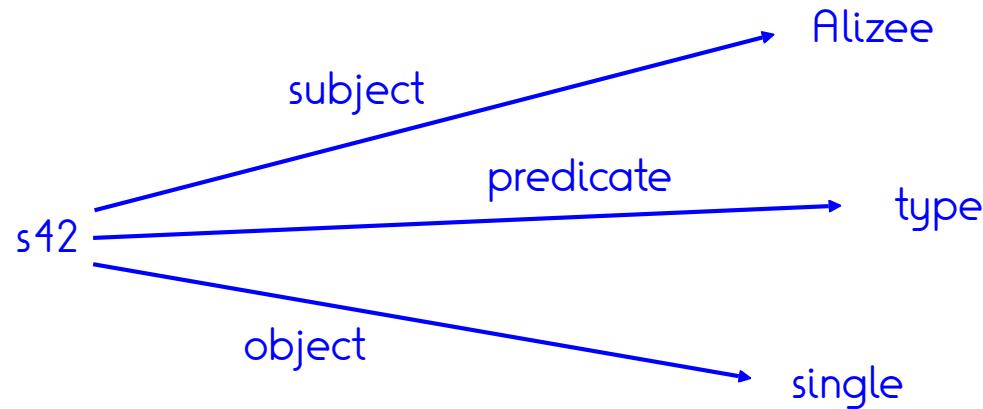


Simplified notation:

hopes(Pierre, type(Alizee, single))

Reification and Event Entities

The difference to event entities is that reified statements can be hypothetical (= not part of the KB).



Task: Reification

Write down a knowledge base
with some reified facts.

Can you reify facts that have reified arguments?

Def: Canonic Entities

An entity is canonic in a KB, if there is no other entity in the KB that represents the same real-world object.

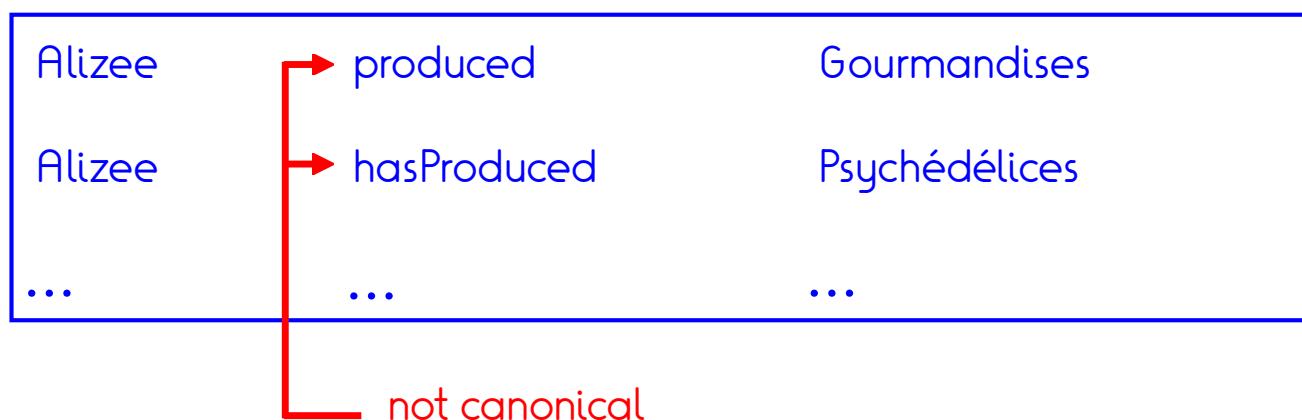
Alizee	produced	Gourmandises
A. Jacotey	hasProduced	Psychédélices
...

not canonical

(Here, we distinguish exceptionally between an entity in the KB, and the real world object. This distinction is correct, but rarely necessary otherwise, which is why this lecture does not make the difference)

Def: Canonic Relations

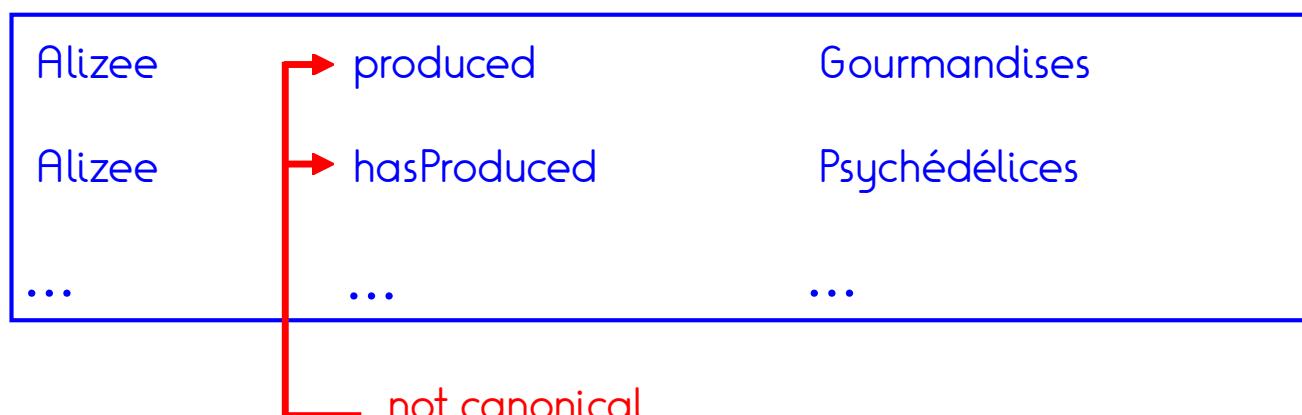
An relation is canonic in a KB, if there is no other relation in the KB that represents the same real-world relation.



Use of Canonicity

Canonicity is essential for

- counting
- answering queries
- constraint satisfaction



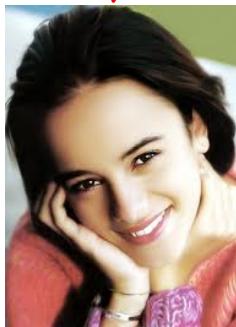
Canonicity and Names

A canonic entity can have multiple names.

Alizee	produced	Gourmandises
Alizee	produced	Psychédélives
Alizee	label	"Alizee"
Alizee	label	"A. Jacotey"
produced	label	"produced"
produced	label	"has produced"
...

Canonicity is not easy

Jacotey is considered one of the "100 Se women of the world". The singer said in that Alizée is married, but she lives sepa



Example: Non-Canonicity



Open Information Extraction

"Tell me about Alizée"

Argument 1:

Relation:

24 answers from 46 sentences

is a french singer (8)

fakes urdukahaniust 2006 (4)

was booed by some of the 3,400 fans (2)

is *French pop singer* (3)

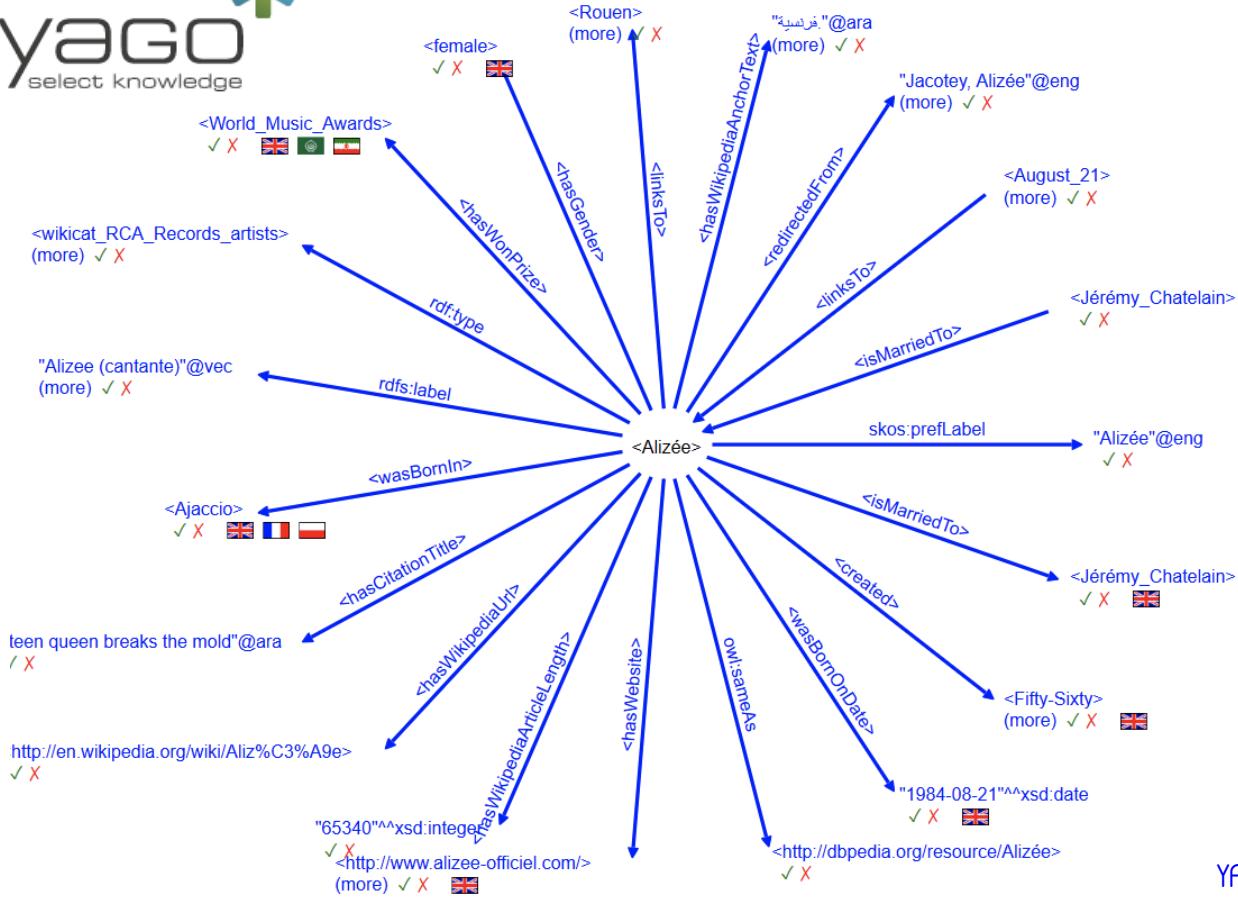
does a little strip-tease move (3)

near duplicates

not Alizee

not an entity

Example: Canonicity



Example: Non-Canonicity



Open Information Extraction

"Who built the pyramids?"

Argument 1:

Relation: built

192 answers from 865 sentences

[all](#) [person \(29\)](#) [deceased person \(16\)](#) [location \(13\)](#) [monarch \(12\)](#)

Egyptians (278) → correct

Pharaoh (41) → not bad

Aliens (35) → less likely

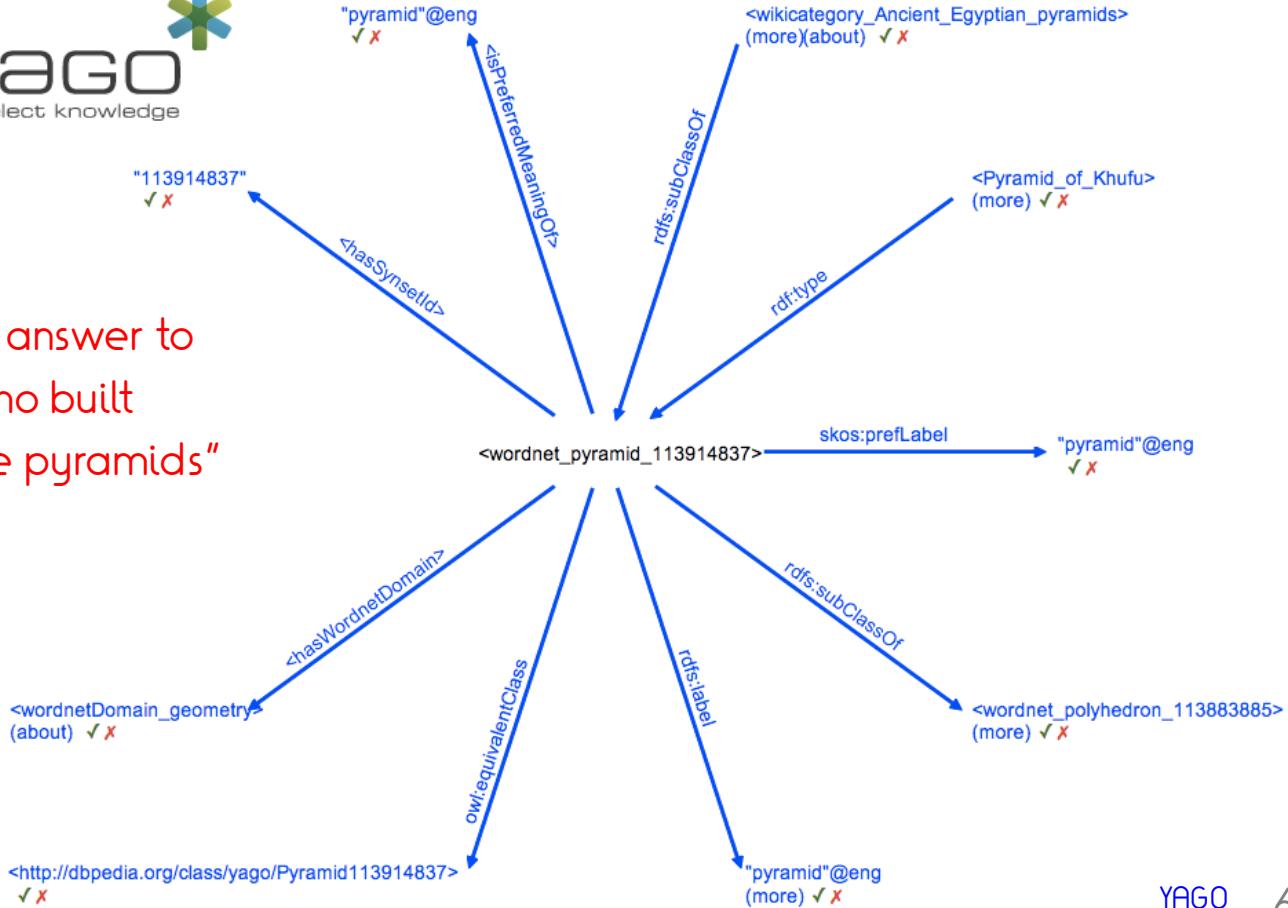
the Ancient Egyptians (31) → duplicate

people (25) → useful

Example: Canonicity



No answer to
"Who built
the pyramids"



Canonicity as Trade-Off



non-canonic



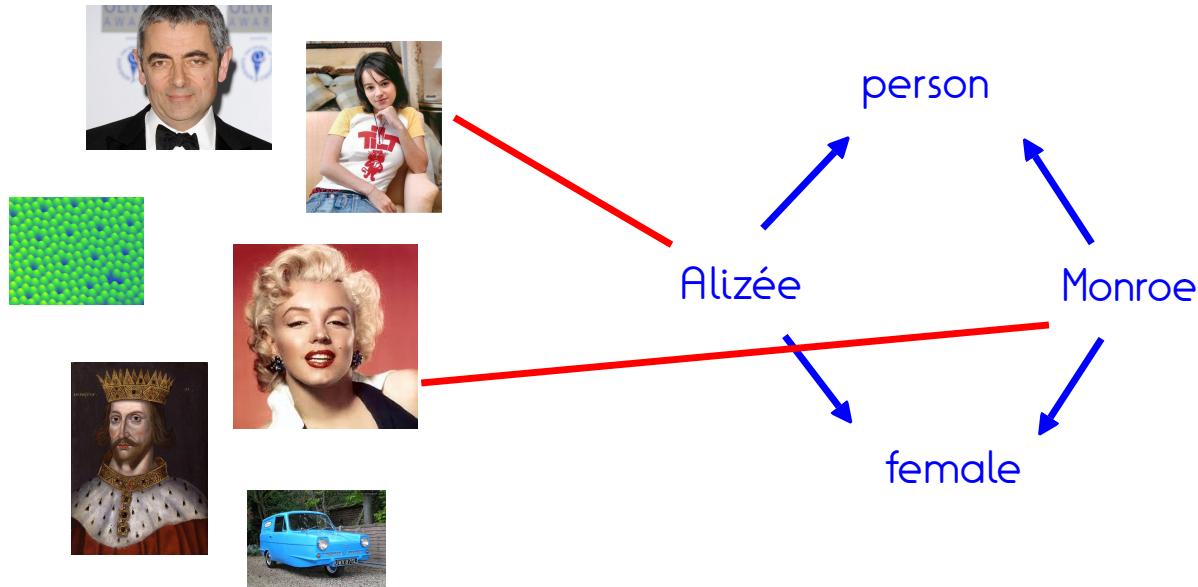
canonic

- easier to extract
- less easy to use
- more noise
- more data

- difficult to extract
- easy to use
- less noise
- less data

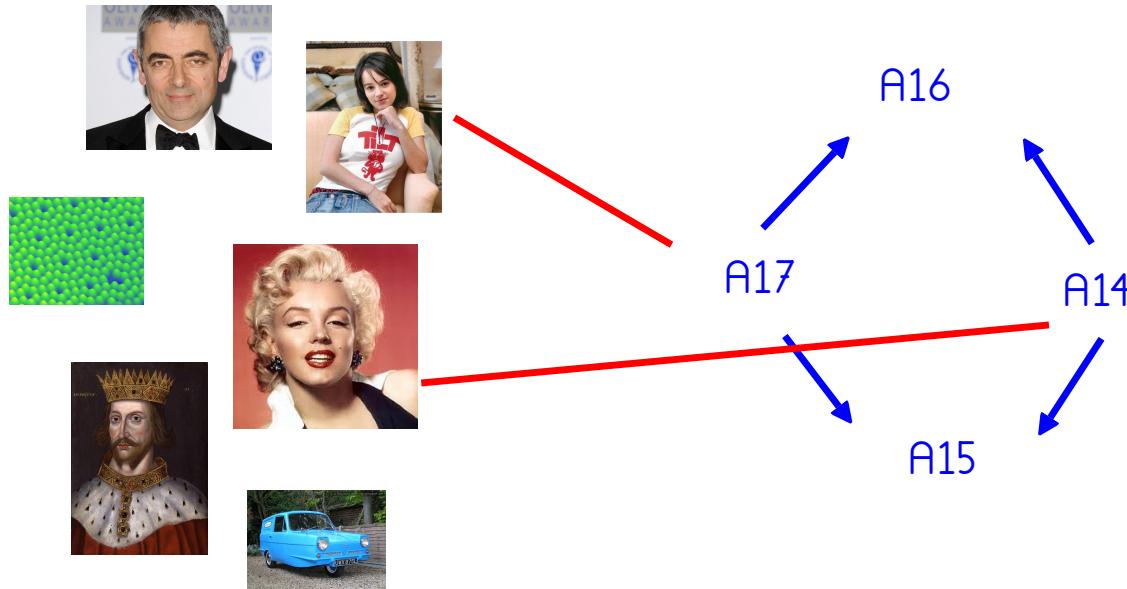
Digression: Reality

We model reality by a representation.



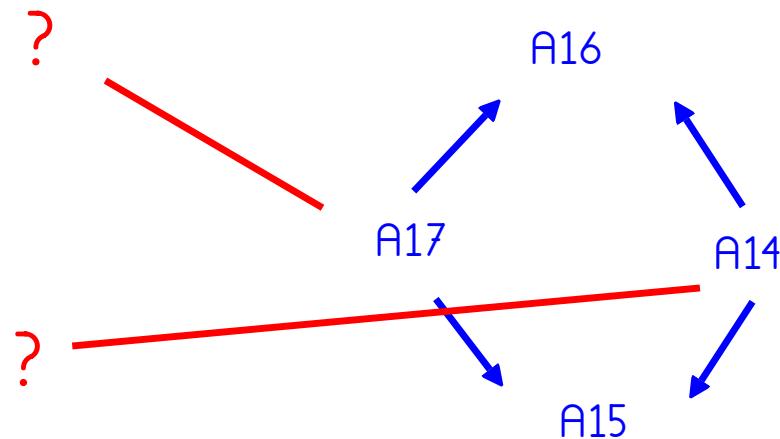
Digression: Reality

Our identifiers are arbitrary names.



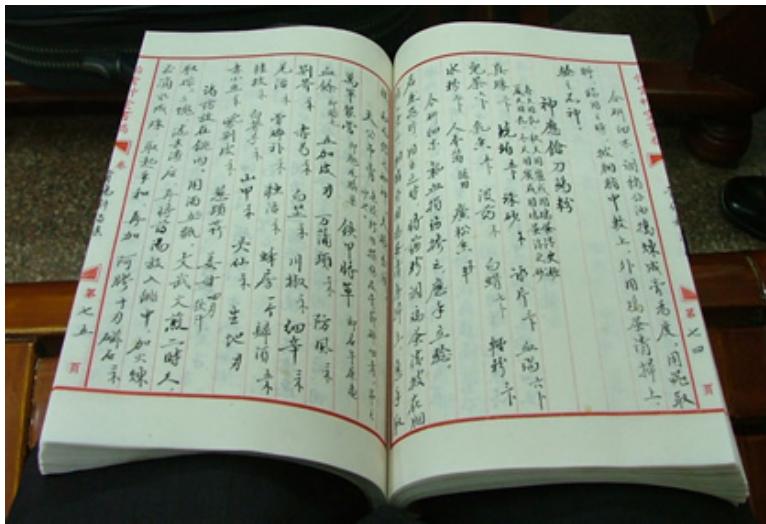
Digression: Reality

Can we reconstruct reality
from our model?



Digression: Reality

Most likely no: A Chinese dictionary
is a model of the world...



...yet, by reading it, you cannot learn Chinese.

- >introduction-nlp
- >corpus ->GAFA
- >character-encodings
- >named-entity-recognition
- >semantic-web

References

The knowledge representation model
we saw today is [RDF](#) without URIs.

See also:

[Knowledge Representation in Entity-Centric Knowledge Bases](#)

- >[introduction-nlp](#)
- >[corpus](#) ->[GAFA](#)
- >[character-encodings](#)
- >[named-entity-recognition](#)
- >[semantic-web](#)