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Sorting concepts

Insertion Sort

Straight Insertion Sort Shell Sort

Selection Sort
Straight Selection Sort

Exchange Sort
Bubble Sort

Devide-and-Conquer

Quick Sort Merge Sort

Sorting algorithms

Data Structures and Algorithms

Dept. Computer Science

Faculty of Computer Science and Engineering Ho Chi Minh University of Technology, VNU-HCM

Overview

Sorting Dept. Computer





Sorting concepts

Insertion Sort

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Selection Sort
Straight Selection Sort

Exchange Sort

Bubble Sort

Devide-and-Conquer

Quick Sort Merge Sort

1 Sorting concepts

2 Insertion Sort Straight Insertion Sort Shell Sort

3 Selection Sort Straight Selection Sort

4 Exchange Sort
Bubble Sort

5 Devide-and-Conquer
Quick Sort

Merge Sort

Course learning outcomes

L.0.1 Determine the complexity of simple algorithms (polynomial time - nested loop - no recursive) Give definition of Big-O notation L.O.1.1 L.O.1.2 Determine complexity of simple polynomial algorithms 1.02Manipulate basic data structures such as list, tree and graph 1021Describe and present basic data structures such as: array, linked list, stack, queue, tree, and graph L.O.2.2 Implement basic methods for each of basic data structures: array, linked list, stack, queue, tree, and graph L.O.3 Implement basic sorting and searching algorithms I 0 3 1 Illustrate how searching algorithms work on data structures: array, linked list, stack, queue, tree, and graph L.O.3.2 Illustrate how sorting algorithms work on an array L.O.3.3 Implement necessary methods and proposed algorithms on a given data structure for problem solving

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Insertion Sort

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Bubble Sort

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Ouick Sort

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Sorting concepts

Insertion Sort

Straight Insertion Sort Shell Sort

Selection Sort Straight Selection Sort

Exchange Sort

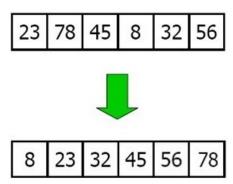
Bubble Sort

Devide-and-Conquer

Quick Sort Merge Sort

Sorting concepts

One of the most important concepts and common applications in computing.



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Sorting concepts

Insertion Sort

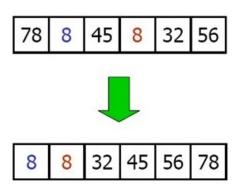
Straight Insertion Sort Shell Sort

Selection Sort
Straight Selection Sort

Exchange Sort

Devide-and-Conquer

Sort stability: data with equal keys maintain their relative input order in the output.



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Selection Sort Straight Selection Sort

Exchange Sort

Bubble Sort Devide-and-Conquer

Quick Sort Merge Sort

Sort efficiency: a measure of the relative efficiency of a sort = number of comparisons + number of moves.

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Insertion Sort

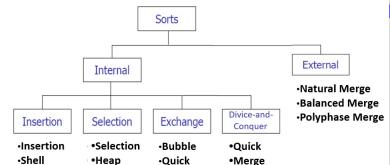
Straight Insertion Sort Shell Sort

Selection Sort
Straight Selection Sort

Exchange Sort

Bubble Sort

Devide-and-Conquer



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Sorting concepts

Insertion Sort

Insertion Sort

Straight Insertion Sort Shell Sort

Selection Sort
Straight Selection Sort

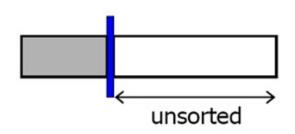
Exchange Sort

Exchange Sort

Bubble Sort

Devide-and-Conquer

- The list is divided into two parts: sorted and unsorted.
- In each pass, the first element of the unsorted sublist is inserted into the sorted sublist.



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Insertion Sort

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Straight Selection Sort

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Devide-and-Conquer

23	78	45	8	32	56
8					

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Sorting concepts

Insertion Sort

Straight Insertion Sort

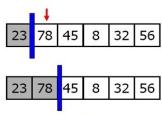
Shell Sort

Selection Sort Straight Selection Sort

Exchange Sort

Bubble Sort

Devide-and-Conquer



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Sorting concepts

Insertion Sort

Straight Insertion Sort

Shell Sort

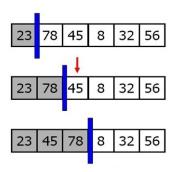
Selection Sort Straight Selection Sort

Straight Selection Sort

Exchange Sort Bubble Sort

Devide-and-Conquer Ouick Sort

Merge Sort



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Sorting concepts

Insertion Sort

Straight Insertion Sort

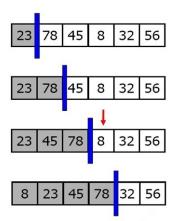
Shell Sort
Selection Sort

Straight Selection Sort

Exchange Sort Bubble Sort

Bubble Sort

Devide-and-Conquer Ouick Sort



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Sorting concepts

Insertion Sort

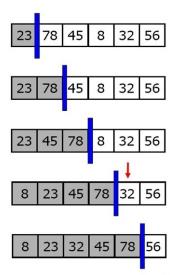
Straight Insertion Sort Shell Sort

Selection Sort
Straight Selection Sort

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Insertion Sort

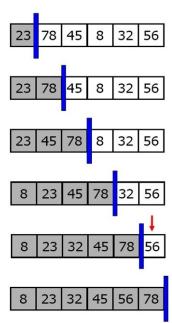
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Selection Sort Straight Selection Sort

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Sorting concepts

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3 if count > 1 then

end

- 1 Algorithm InsertionSort()
- 2 Sorts the contiguous list using straight insertion sort.





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Sorting concepts

Insertion Sort

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Selection Sort Straight Selection Sort

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Devide-and-Conquer Quick Sort Merge Sort

current = 1

while current < count do

temp = data[current]

walker = current - 1

while walker >= 0 AND temp.key < data[walker].key do

data[walker+1] = data[walker]

walker = walker - 1

data[walker+1] = temp

current = current + 1end

15 end

10

11

12

13

- Named after its creator Donald L. Shell (1959).
- Given a list of N elements, the list is divided into K segments (K is called the increment).
- Each segment contains N/K or more elements.
- Segments are dispersed throughout the list.
- Also is called diminishing-increment sort.

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Sorting concepts

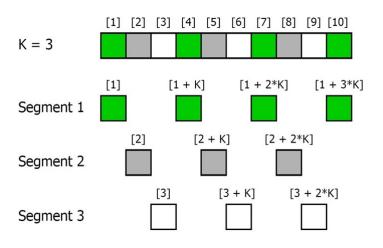
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- For the value of K in each iteration, sort the K segments.
- After each iteration, K is reduced until it is 1 in the final iteration.

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Example of Shell Sort

Sorting

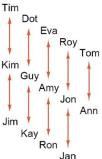
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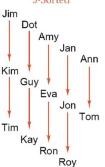
Unsorted

Tim Dot Eva Roy Tom Kim Guy Amy Jon Ann Jim Kay Ron Jan

Sublists incr. 5



5-Sorted



Recombined

Jim Dot Amy Jan Ann Kim Guy Eva Jon Tom Tim Kay Ron Roy

Sorting concepts

Insertion Sort
Straight Insertion Sort
Shell Sort

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Straight Selection Sort

Straight Selection Sort

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Quick Sort Merge Sort

Bubble Sort

Example of Shell Sort

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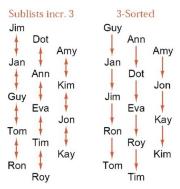


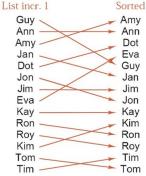






Bubble Sort





Choosing incremental values

 From more of the comparisons, it is better when we can receive more new information

- Incremental values should not be multiples of each other, other wise, the same keys compared on one pass would be compared again at the next.
- The final incremental value must be 1.

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Sorting concepts

Insertion Sort

Straight Insertion Sort
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Straight Selection Sort

Exchange Sort Bubble Sort

Choosing incremental values

• Incremental values may be:

$$1, 4, 13, 40, 121, ...$$

 $k_t = 1$
 $k_{i-1} = 3 * k_i + 1$
 $t = |\log_3 n| - 1$

or:

$$1, 3, 7, 15, 31, ...$$

 $k_t = 1$
 $k_{i-1} = 2 * k_i + 1$
 $t = |\log_2 n| - 1$

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Sorting concepts

Insertion Sort

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Shell Sort

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Exchange Sort

Bubble Sort

- 1 Algorithm ShellSort()
- 2 Sorts the contiguous list using Shell sort.
- 3 k = first incremental value
- 4 while k >= 1 do
 - segment = 1
 - while segment <= k do
 - SortSegment(segment)
 - $\mathsf{segment} = \mathsf{segment} + 1$
 - end
 - k = next_incremental_value
- 1 end

6

2 End ShellSort

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Sorting concepts

Insertion Sort

Straight Insertion Sort Shell Sort

Selection Sort Straight Selection Sort

Exchange Sort

Bubble Sort

Devide-and-Conquer

11

13 end

- 1 Algorithm SortSegment(val segment <int>, val k $\langle int \rangle$
- 2 Sorts the segment beginning at segment using insertion sort, step between elements in the segment is k.

3 current = segment + k

while current < count do

temp = data[current]5 walker = current - k

while walker >=0 AND temp.kev <

data[walker].key do

data[walker + k] = data[walker]

walker = walker - k

end data[walker + k] = tempcurrent = current + k

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Sorting concepts Insertion Sort

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Straight Selection Sort

Exchange Sort Bubble Sort

Insertion Sort Efficiency

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Sorting concepts

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Bubble Sort

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Quick Sort Merge Sort

Straight insertion sort:

$$f(n) = n(n+1)/2 = O(n^2)$$

• Shell sort: $O(n^{1.25})$ (Empirical study)

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Sorting concepts

Insertion Sort

Straight Insertion Sort Shell Sort

Selection Sort

Selection Son

Straight Selection Sort

Exchange Sort

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Selection Sort

In each pass, the smallest/largest item is selected and placed in a sorted list.

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Sorting concepts

Insertion Sort

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lection Sort

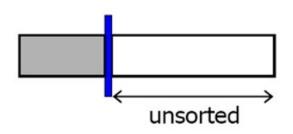
Straight Selection Sort

Exchange Sort

Bubble Sort

Devide-and-Conquer

- The list is divided into two parts: sorted and unsorted.
- In each pass, in the unsorted sublist, the smallest element is selected and exchanged with the first element.



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Sorting concepts

Insertion Sort

Straight Insertion Sort Shell Sort

Selection Sort

Straight Selection Sort

Exchange Sort Bubble Sort

Devide-and-Conquer

23 78 45 8 32 56

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Sorting concepts

Insertion Sort

Straight Insertion Sort Shell Sort

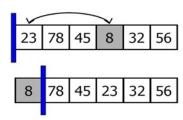
Selection Sort

Straight Selection Sort

Exchange Sort

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Sorting concepts

Insertion Sort

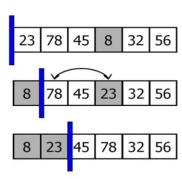
Straight Insertion Sort Shell Sort

Selection Sort Straight Selection Sort

Exchange Sort

Bubble Sort

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Sorting concepts

Insertion Sort Straight Insertion Sort

Shell Sort

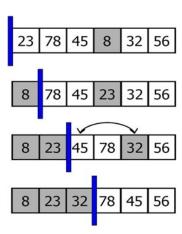
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Exchange Sort

Bubble Sort

Devide-and-Conquer Ouick Sort



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Sorting concepts

Insertion Sort

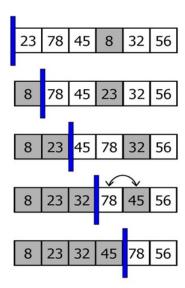
Straight Insertion Sort Shell Sort

Selection Sort Straight Selection Sort

Straight Selection 50

Exchange Sort
Bubble Sort

Devide-and-Conquer



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Sorting concepts

Insertion Sort

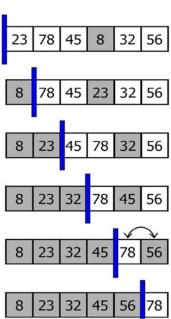
Straight Insertion Sort Shell Sort

Selection Sort Straight Selection Sort

Straight Selection So

Exchange Sort
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Sorting concepts

Insertion Sort

Straight Insertion Sort Shell Sort

Selection Sort Straight Selection Sort

Exchange Sort

Bubble Sort

Devide-and-Conquer Quick Sort

Straight Selection Sort 1 Algorithm SelectionSort()

- 2 Sorts the contiguous list using straight selection sort.

3 current = 0

8

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12

15 end

- 4 while current < count 1 do
- smallest = current
- walker = current + 16
 - while walker < count do
 - if data [walker].key < data [smallest].key then
 - smallest = walker
 - end
 - walker = walker + 1end
 - swap(current, smallest)
- 13 current = current + 114

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Sorting



Sorting concepts

Insertion Sort

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Selection Sort Straight Selection Sort

Exchange Sort

Bubble Sort

Devide-and-Conquer Quick Sort

Selection Sort Efficiency

 $O(n^2)$

• Straight selection sort:

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Sorting concepts

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Exchange Sort

Bubble Sort

Devide-and-Conquer

Exchange Sort

 In each pass, elements that are out of order are exchanged, until the entire list is sorted

• Exchange is extensively used.

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Sorting concepts

Insertion Sort

Straight Insertion Sort Shell Sort

Selection Sort

Straight Selection Sort

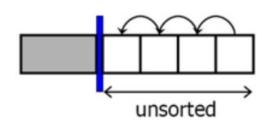
Exchange Sort

Bubble Sort

Devide-and-Conquer

Bubble Sort

- The list is divided into two parts: sorted and unsorted.
- In each pass, the smallest element is bubbled from the unsorted sublist and moved to the sorted sublist.



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Sorting concepts

Insertion Sort

Straight Insertion Sort Shell Sort

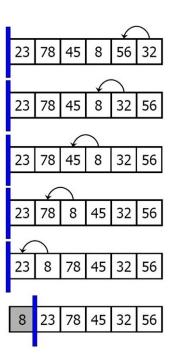
Selection Sort
Straight Selection Sort

Exchange Sort

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Bubble Sort



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Sorting concepts

Insertion Sort

Straight Insertion Sort Shell Sort

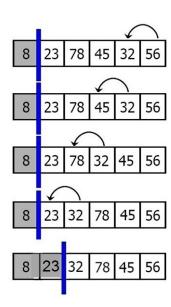
Selection Sort Straight Selection Sort

Exchange Sort

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Devide-and-Conquer

Bubble Sort



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Sorting concepts

Insertion Sort

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Selection Sort
Straight Selection Sort

Exchange Sort

Exchange 3

Bubble Sort

Devide-and-Conquer

Bubble Sort 1 Algorithm BubbleSort() 2 Sorts the contiguous list using bubble sort. 3 current = 04 flag = False

5 **while** current < count AND flag = False **do** walker = count - 1flag = Truewhile walker > current do if data [walker].key < data [walker-1].key then flag = Falseswap(walker, walker - 1) end walker = walker - 1end

current = current + 1

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Sorting concepts

Insertion Sort

Straight Insertion Sort Shell Sort Selection Sort

Straight Selection Sort **Exchange Sort**

Devide-and-Conquer Quick Sort Merge Sort

9

10

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12

13

14

16

Exchange Sort Efficiency

Sorting

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Sorting concepts

Insertion Sort

Straight Insertion Sort Shell Sort

Selection Sort
Straight Selection Sort

Exchange Sort

Bubble Sort

Devide-and-Conquer

Quick Sort Merge Sort

• Bubble sort:

 $f(n) = n(n+1)/2 = O(n^2)$

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Sorting concepts

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Devide-and-Conquer

Selection Sort Straight Selection Sort

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- Sorting concepts
- Insertion Sort
- Straight Insertion Sort Shell Sort
- Selection Sort
- **Exchange Sort**
- Merge Sort

- Straight Selection Sort
- Bubble Sort
- Quick Sort

- 1 Algorithm DevideAndConquer()
- 2 **if** the list has length > 1 **then**
 - partition the list into lowlist and highlist
 - lowlist.DevideAndConquer()
 - highlist.DevideAndConquer()
 - combine(lowlist, highlist)
- 7 end
- 8 End DevideAndConquer

Devide-and-Conquer Sort

Merge Sort

Quick Sort

Partition

easy

hard

Combine

hard

easy

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Sorting concepts

Insertion Sort

Straight Insertion Sort Shell Sort

Selection Sort Straight Selection Sort

Exchange Sort Bubble Sort

.. ..

Devide-and-Conque

Quick Sort

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Sorting concepts

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Exchange Sort

Bubble Sort

Devide-and-Conquer

Quick Sort

- 1 Algorithm QuickSort()
- 2 Sorts the contiguous list using quick sort.
- 3 recursiveQuickSort(0, count 1)
- 4 End QuickSort

Quick Sort

- 2 Sorts the contiguous list using quick sort.
- 3 Pre: left and right are valid positions
 in the list

4 Post: list sorted

5 **if** left < right **then**

1, right)

pivot_position = Partition(left, right)
recursiveQuickSort(left,
 pivot_position - 1)
recursiveQuickSort(pivot_position +

9 end

8

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Sorting concepts

Insertion Sort Straight Insertion Sort

Shell Sort
Selection Sort

Straight Selection Sort

Exchange Sort
Bubble Sort

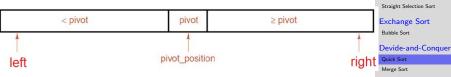
Devide-and-Conquer

Quick Sort Merge Sort

weige Joit

Quick Sort

Given a pivot value, the partition rearranges the entries in the list as the following figure:



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Sorting concepts

Insertion Sort

Straight Insertion Sort Shell Sort

Selection Sort

Quick Sort Efficiency

• Quick sort: $O(nlog_2n)$

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Sorting concepts

Insertion Sort

Straight Insertion Sort Shell Sort

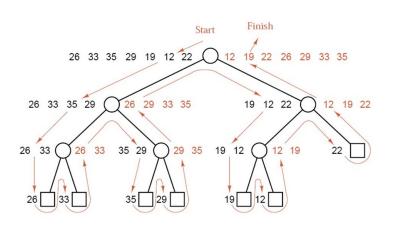
Selection Sort
Straight Selection Sort

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Exchange Sort

Bubble Sort

Devide-and-Conquer Quick Sort

- 1 Algorithm MergeSort()
- 2 Sorts the linked list using merge sort.
- 3 recursiveMergeSort(head)
- 4 **End** MergeSort

- 2 Sorts the linked list using recursive merge sort.
- 3 if sublist is not NULL AND sublist->link is not NULL then
 - Divide(sublist, second_list)
 - recursiveMergeSort(sublist)
 - recursiveMergeSort(second_list)
 - Merge(sublist, second_list)
- 8 end
- 9 End recursiveMergeSort

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Sorting concepts

Insertion Sort

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Devide-and-Conquer Quick Sort

- Algorithm Divide(val sublist <pointer>, ref second_list <pointer>)
- 2 Divides the list into two halves.

```
midpoint = sublist
position = sublist->link
while position is not NULL do
position = position->link
position is not NULL then
midpoint = midpoint->link
position = position->link
end
```

11 end

12 second_list = midpoint->link

13 midpoint->link = NULL

14 End Divide

Sorting

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Sorting concepts

Insertion Sort

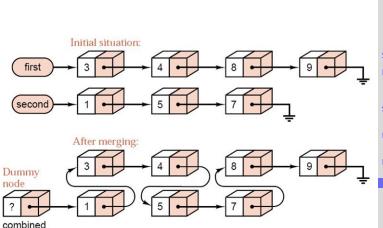
Straight Insertion Sort Shell Sort

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Merge two sublists



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Quick Sort

Merge two sublists

- 2 Merges two sorted lists into a sorted list.
- 3 lastSorted = address of combined
- 4 while first is not NULL AND second is not NULL do

```
if first->data.key <= second->data.key then
lastSorted->link = first
lastSorted = first
first = first->link
```

else

lastSorted->link = second
lastSorted = second
second = second->link

end

ı4 end

10

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12

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Sorting concepts

Insertion Sort

Straight Insertion Sort Shell Sort

Selection Sort
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Bubble Sort

Devide-and-Conquer Quick Sort

Merge two sublists

```
1 // ...
```

8 first = combined.link

9 End Merge

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Sorting.60

THANK YOU.