Course Outcome: Students well have underestanding how to write system of equations using matrise notation, about matrise multiplication and how to compute elimination matrices and their we to convert ce matrier into cepper triangular form.

$$E_{x}$$
: $2u + v + w = 5$
 $+u - 6v = -2$
 $-2u + 7v + 2w = 9$

where
$$R = \begin{bmatrix} 2 & 1 & 1 \\ 4 & -6 & 0 \\ -2 & 7 & 2 \end{bmatrix}$$
 (coefficient matrix)

Let A be a matrix with order man and B be a matrier with order prq. Then mulliplication of A with B is possible it n=p and order of

$$\frac{E_{X}}{2} = \begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix}, B = \begin{bmatrix} 4 \\ 5 \\ 6 \end{bmatrix}_{1X3}$$

AB = \[4 5 6 7 \ (matrix product which is 12 15 18 \] column times row)

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$$\frac{E_{x}}{1} = \begin{bmatrix} 1 & 1 & 6 \\ 3 & 0 & 1 \\ 1 & 1 & 4 \end{bmatrix}, x = \begin{bmatrix} 2 \\ 5 \\ 0 \end{bmatrix}$$

Points to remember:

1. Matrix multiplication is associative:

2. Matrix multiplication às disatributive:

3. Matrix multiplication is not commutative:

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Elimination Matrices:

Ex: Let
$$A = \begin{bmatrix} 2 & 1 & 1 \\ -2 & 7 & 2 \end{bmatrix}$$

$$= \begin{bmatrix} 2 & 1 & 1 \\ 0 & 8 & -2 \\ 0 & 8 & 3 \end{bmatrix} R_2 + R_2 - 2R_1 (2)$$

$$= \begin{bmatrix} 2 & 1 & 1 \\ 0 & 8 & 3 \end{bmatrix} R_3 + R_3 + R_1 (-1)$$

$$= \begin{bmatrix} 2 & 1 & 1 \\ 0 & -8 & -2 \\ 0 & 0 \end{bmatrix} R_3 + R_3 + R_2 (-1)$$

The elimination matrices are

$$E_{21} = \begin{bmatrix} -2 & 0 & 0 \\ -2 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}, E_{31} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 1 & 0 \end{bmatrix}, E_{32} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 1 \\ 0 & 1 & 0 \end{bmatrix}$$

E32 E31 E21 A= U

In this example 2, -1 and -1 are the multipliers of the 2nd now 1st column, 3nd now 1st column and 3nd now 2nd column places respectively. We are writing the opposite value of the multipliers in the respective places of a 3nd order identity matrix to get the elimination matrices.

Note: It a now operation is $R_i \leftarrow R_i - LR_j$, then i's the multiplien for the i-th now and j-th column place.

$$HB = \begin{bmatrix} -1 & 1 \\ -1 & 1 \end{bmatrix} \quad BA = \begin{bmatrix} -1 & -1 \\ 1 & 1 \end{bmatrix}$$

No. 4 @ Diagonal matrix:

A square matrix is said to be a diagonal matrix it all the off diagonal elements are zeroi.e. aij =0 (for i +j.

6 Symmetric matrix:

A square matrix A is said to be a symmetric matrix it A = A i.e. aij = aji for all i and j.

@ Upper triangular matrix:

A square matrix is said to be an appear triangular matrix it all its lower diagonal elements are zero i.e. aij =0 it iti.

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@ Skew-Lymmercic motrix:

A square matrix \hat{H}' is seed to be a show-symmetric matrix if $\hat{H}^T = -\hat{H}$ i.e. Aij = -Aji for all i and j.

$$Ex : R = \begin{bmatrix} 0 & -2 \\ 2 & 0 \end{bmatrix}, B = \begin{bmatrix} 0 & h & q \\ -h & 0 & 4 \\ -q & -5 & 0 \end{bmatrix}$$

$$\frac{10-5}{4} \cdot \frac{1}{5} = \begin{bmatrix} 4x3 + 0x4 + 1x5 \\ 0 & 1 & 0 \\ 4 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 4x3 + 0x4 + 1x5 \\ 0x3 + 1x4 + 0x5 \\ 4x3 + 0x4 + 1x5 \end{bmatrix} = \begin{bmatrix} 17 \\ 4 \\ 17 \end{bmatrix}$$

(ii)
$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 5 \\ -2 \\ 3 \end{bmatrix} = \begin{bmatrix} 1 \times 5 + 0 \times (-2) + 0 \times 3 \\ 0 \times 5 + 0 \times (-2) + 1 \times 3 \end{bmatrix} = \begin{bmatrix} 5 \\ -2 \\ 3 \end{bmatrix}$$

$$(iii) \begin{bmatrix} 2 & 0 \end{bmatrix} \begin{bmatrix} 1 \\ 1 & 3 \end{bmatrix} \begin{bmatrix} 1 \\ 1 \end{bmatrix} = \begin{bmatrix} 2x_1 + 0x_1 \\ 1x_1 + 3x_1 \end{bmatrix} = \begin{bmatrix} 2 \\ 4 \end{bmatrix}$$

$$4 \uparrow \qquad \Rightarrow (2,4)$$

$$\frac{Np\cdot 19}{Np\cdot 19} \text{ (i) } H = \begin{bmatrix} \frac{1}{2} & \frac{1}{2} \\ \frac{1}{2} & \frac{1}{2} \end{bmatrix}$$

$$H^{2} = \begin{bmatrix} 1/2 & 1/2 \end{bmatrix} \begin{bmatrix} 1/2 & 1/2 \end{bmatrix} = \begin{bmatrix} 1/2 & 1/2 \end{bmatrix} = H$$

$$\begin{bmatrix} 1/2 & 1/2 \end{bmatrix} \begin{bmatrix} 1/2 & 1/2 \end{bmatrix} \begin{bmatrix} 1/2 & 1/2 \end{bmatrix} = H$$

$$B^{3} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & (-1)^{3} \end{bmatrix}$$

$$B^{2} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & (-1)^{2} \end{bmatrix}$$

$$C^{2} = \begin{bmatrix} 1/2 & -1/2 \\ 1/2 & -1/2 \end{bmatrix} \begin{bmatrix} 1/2 & -1/2 \\ 1/2 & -1/2 \end{bmatrix} \begin{bmatrix} 1/2 & -1/2 \\ 1/2 & -1/2 \end{bmatrix} = \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}$$

$$C^{3} = \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}$$

$$C^{3} = \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}$$

$$C^{3} = \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}$$

$$C^{4} = \begin{bmatrix} 0 & 1 & 0 \\ -2 & 2 & 0 \end{bmatrix}$$

$$= \begin{bmatrix} 1 & 1 & 0 \\ 0 & 0 & 1 \\ 0 & 4 & 0 \end{bmatrix} R_{2} \leftarrow R_{2} - 4R_{1} (4)$$

$$\begin{bmatrix} 0 & 4 & 0 \\ 0 & 4 & 0 \end{bmatrix} R_{3} \leftarrow R_{3} + 2R_{1} (-2)$$

$$= \begin{bmatrix} 1 & 1 & 0 \\ 0 & 2 & 1 \\ 0 & 0 & -2 \end{bmatrix} \quad R_3 \leftarrow R_3 - 2R_2 \quad (2)$$

The multipliers are 4, -2 and 2.

The elimination matrices are

$$E_{34} = \begin{bmatrix} 1 & 0 & 0 \\ -4 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$
, $E_{31} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 2 & 0 & 1 \end{bmatrix}$, $E_{32} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & -2 & 1 \end{bmatrix}$.

$$E_{33} E_{31} E_{21} R = U$$
.
 $\Rightarrow MR = U$,
where $M = E_{33} E_{31} E_{21} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ + & 1 & 0 & 0 \\ -2 & 2 & 1 & 0 \end{bmatrix}$.

He 31. Given:
$$R(0) = \begin{bmatrix} ca20 & -\sin 0 \\ \sin 0 & ca20 \end{bmatrix}$$
 $R(0) = \begin{bmatrix} ca20 & -\sin 0 \\ c\sin 0 & ca20 \end{bmatrix}$, $R(0_2) = \begin{bmatrix} ca20 & -\sin 0 \\ c\sin 0 & ca20 \end{bmatrix}$
 $R(0) R(0_2) = \begin{bmatrix} ca20 & (a20) & -\sin 0 & ca20 \end{bmatrix}$
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 $Cono & (a20) & -\cos 0 & ca20 & ca20 \end{bmatrix}$
 $Cono & (a20) & -\cos 0 & ca20 & ca20 & ca20 \end{bmatrix}$
 $Cono & (a20) & (a20) & -\cos 0 & ca20 & ca20 & ca20 \end{bmatrix}$
 $R(0) R(0) = \begin{bmatrix} ca20 & ca20 &$

$$= \begin{bmatrix} 2 & -1 & 0 & 0 \\ 0 & 3/2 & -1 & 0 \\ 0 & 0 & 4/3 & -1 \\ 0 & 0 & 0 & \boxed{13} \end{bmatrix} \quad R_{4} \leftarrow R_{4} + \frac{2}{4}R_{3} \left(-\frac{3}{4} \right)$$

The multipliers are -3, -2 and -3.

The required elimination matrices are

$$E_{21} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ \frac{1}{93} & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$$
, $E_{39} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & \frac{21}{3} & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$

$$E_{43} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & \frac{3}{4} & 1 \end{bmatrix}$$