## TDDE01 Machine Learning

Lab3

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#### Assignment 1. Kernel methods

The task for this assignment was to predict the temperature in 2 hour intervals for a whole day, on a specific chosen date and location in Sweden. The given data contained 50000 temperature measurements from weather stations in Sweden. The prediction was made using the sum of three Gaussian kernels; The first to account for the distance from a station to the chosen location, the second to account for the distance between the date a temperature measurement was made and the chosen date, and the third to account for the distance between the hour of the day a temperature measurement was made and the hour of interest.

First I wrote some setup code, like a function for the Gaussian kernel equation, initialization of the h values for all three kernels and the location and date to do the prediction on.

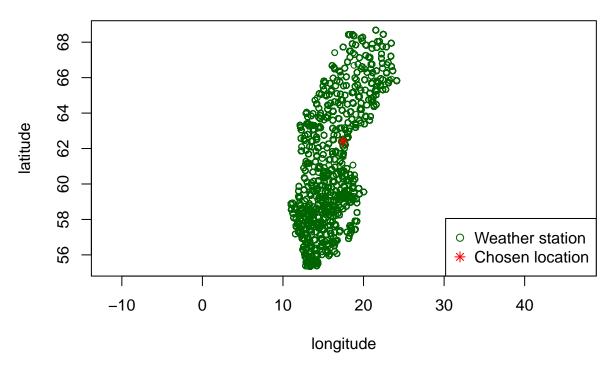
The Gaussian kernel equation looks like this:

$$k(u) = exp(-||u||^2)$$

where || || is the Euclidian norm.

```
# Assignment 1
set.seed(1234567890)
gaussian_kernel = function(u) {
 return(exp(-u^2))
stations <- read.csv("stations.csv", fileEncoding = "iso-8859-1", encoding = "utf8")
temps <- read.csv("temps50k.csv")</pre>
st <- merge(stations,temps,by="station number")</pre>
# Smoothing coefficients for the kernels
h_distance <- 100000
h_date <- 30
h_{time} <- 2
# The point and date to predict
alno = c(17.4604, 62.4035) # order is (long, lat) because of Haversine.
date <- "2018-03-04"
times <- c("04:00:00", "06:00:00", "08:00:00", "10:00:00", "12:00:00", "14:00:00", "16:00:00", "18:00:00"
temp_sum <- vector(length=length(times))</pre>
temp_prod <- vector(length=length(times))</pre>
plot(st$longitude, st$latitude, asp=2.2, col="darkgreen", cex=0.8, main = "Weather station locations",
points(alno[1], alno[2], col="red", pch=8)
legend("bottomright", legend = c("Weather station", "Chosen location"), col = c("darkgreen", "red"), pcl
```

#### **Weather station locations**



Then I created two vectors, one containing the distances (in meters) from all weather stations to my chosen location (Alnö), and the other containing the amount of days between when a measurement was made and the date I chose (2018-03-04). The year was not included in the second calculation (so the days between for example "1990-01-01" and "2010-01-02" are equal to 1). I've also taken into consideration that the 31 Dec is just one day from 1 Jan, so the maximum distance between two dates is 365/2.

Lastly I create a loop that loops over all the times to predict on ("04:00:00" to "24:00:00" in 2 hour increments). In the loop a third vector was created, containing the time diffrences between when a measurement was taken and the time of interest. Using these three vectors and their corresponding h values, three Gaussian kernels were created and added together to create the final kernel. This kernel was then used to predict the temperature for that specific time, and the results were added to a vector of temperatures. The predicted temperature was calculated using the following equation:

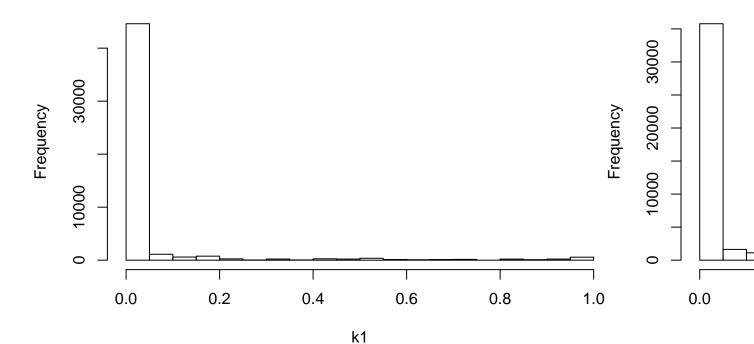
$$y(x) = \frac{\sum_{n} k \left(\frac{x - x_n}{h}\right) t_n}{\sum_{n} k \left(\frac{x - x_n}{h}\right)}$$

where k is the kernel,  $x - x_n$  the distance between the chosen and measured location/date/time and  $t_n$  the measured temperature. A second kernel where the three Gaussian kernels were multiplied instead was also created and used to predict the temperature.

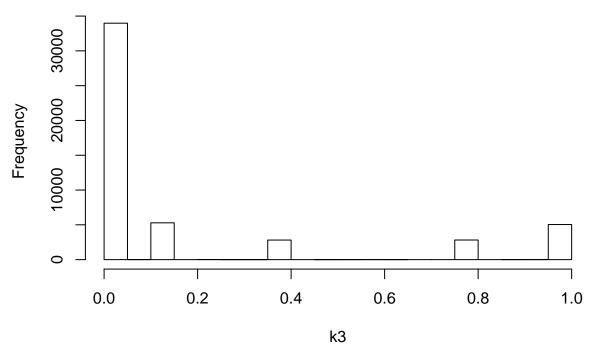
```
station_coords = mapply(c, st$longitude, st$latitude, SIMPLIFY = FALSE)
dist_diff = sapply(station_coords, distHaversine, p2=alno)
date_diff = as.numeric(as.Date(gsub("^....", "0000", date), format = "%Y-%m-%d") - as.Date(as.character
date_diff = sapply(date_diff, function(days) {
   if (abs(days) > 365/2) {
      return(365 - abs(days))
   }
   return(abs(days))
}
```

```
i = 1
for (time in times) {
  time_diff = as.numeric(difftime(as.POSIXct(time, format = "%H:%M:%S"), as.POSIXct(st$time, format = "
  k1 = gaussian_kernel(dist_diff/h_distance)
  k2 = gaussian_kernel(date_diff/h_date)
  k3 = gaussian_kernel(time_diff/h_time)
  kernel_sum = k1 + k2 + k3
  kernel_prod = k1 * k2 * k3
  temp_sum[i] = sum(kernel_sum * st$air_temperature) / sum(kernel_sum)
  temp_prod[i] = sum(kernel_prod * st$air_temperature) / sum(kernel_prod)
  i = i + 1
  if(time == "12:00:00") {
    hist(k1, main = "Histogram of k1 (distance)")
    hist(k2, main = "Histogram of k1 (date)")
    hist(k3, main = "Histogram of k1 (time)")
  }
}
```

### Histogram of k1 (distance)



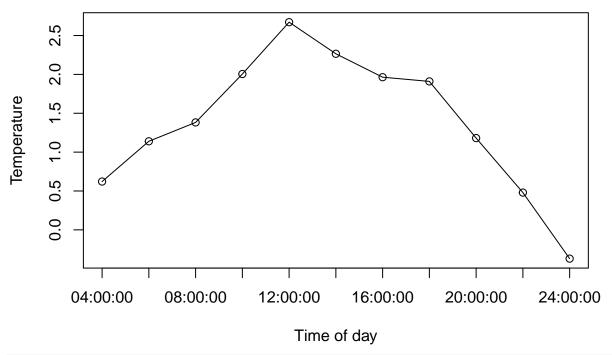
#### Histogram of k1 (time)



At hour 12:00:00 I decided to create histograms of the three Gaussian kernels to see if my chosen h values were reasonable. The h value is used to regulate how the differences in distance/date/time will influence the result. For the Gaussian kernel the h value can be thought of as a "soft limit" to how big the difference is allowed to become before the measurement is considered useless for the prediction. I chose h distance = 100000 (100km). What that means is that measurements from weather stations within ~100km from Alnö contribute (much) to the prediction, which seems like a reasonable area to look at for similar temperatures. I chose h date = 30, so measurements from  $\sim$  a month forward and back contribute to the prediction. This may be strething it a bit since the temperature can change a lot in 2 months. But since I'm not considering what year it is I believe this should give a good average temperature for the chosen date. I chose he time = 2, which means that measurements within  $\sim 2$  hours contribute to the prediction. The temperature can change fast in just one hour, but the given measurements are (mostly) taken at three hour intervals, so 2 hours seemed like a good h value for the time. From the first histogram we can see that most stations don't contribute the the prediction very much (Sweden is a long country, and most weather stations are in the south). From the second histogram we can see that most dates are to far away from my chosen date to contribute, but more measurements are considered than with the distance. The last histogram looks a bit weird, but it shows that most of the measurements are taken on a time to far away from "12:00:00" to be considered. These results look like they should give a pretty good prediction.

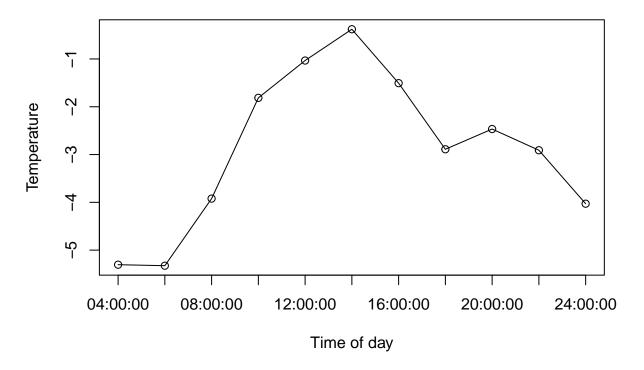
```
plot(temp_sum, type="o", xaxt="n",
    main = "Predicted temperature 2018-03-04 (Summed kernels)",
    xlab = "Time of day",
    ylab = "Temperature")
axis(side=1, at=1:11, labels=times)
```

### Predicted temperature 2018–03–04 (Summed kernels)



```
plot(temp_prod, type="o", xaxt="n",
    main = "Predicted temperature 2018-03-04 (Multiplied kernels)",
    xlab = "Time of day",
    ylab = "Temperature")
axis(side=1, at=1:11, labels=times)
```

# Predicted temperature 2018–03–04 (Multiplied kernels)



Lastly the predictions for both the summed and multiplied kernels were plotted. The results look pretty good, but I think the multiplied kernels give a better prediction than the summed. According to SMHI the average temperature on Alnö in March is around -3 degrees Celsius, which is pretty much what the results from the multiplied kernels says. I believe this is because measurements that are taken on a nearby date and time, but from a weather station very far away, are still contributing some to the results when you add them together. When you multiply them, it's almost like multiplying with 0 because of the distance, so the measurements are not considered even though they are on a close date and time.

#### Assignment 3. Neural Networks

In this assignment the task was to train a neural network with a single hidden layer of 10 units, to learn the trigonometric sine function. This was done using 50 uniformly sampled points from the interval [0, 10] and their corrisponding sine values.

First the data was generated and devided into a training and a validation set. The weights for the 10 units were also randomly generated from the interval [-1, 1].

```
# Assignment 3
set.seed(1234567890)
Var <- runif(50, 0, 10)
trva <- data.frame(Var, Sin=sin(Var))
tr <- trva[1:25,] # Training
va <- trva[26:50,] # Validation

# Random initialization of the weights in the interval [-1, 1]
winit <- runif(10, -1, 1)</pre>
```

Then a loop was created to train 10 neural networks using different thresholds, and compare the error to find the best threshold. The thresholds tested were i/1000 for i = 1, ..., 10.

```
best_nn = NULL
best_error = Inf
best_threshold = NULL
for(i in 1:10) {
    nn <- neuralnet(Sin ~ Var, data=tr, hidden = 10, threshold = i/1000, startweights = winit)
    error = nn$result.matrix[[1]]
    if(error < best_error) {
        best_nn = nn
        best_error = error
        best_threshold = i/1000
    }
}</pre>
```

The threshold that gave the smallest error was 0.002. Lastly a new neural network was trained using the best threshold, and then used to predict the sine values for the validation set.

```
plot(nn <- neuralnet(Sin ~ Var, data=tr, hidden = 10, threshold = best_threshold, startweights = winit)
# Plot of the predictions (black dots) and the data (red dots)
plot(prediction(nn)$rep1)
## Data Error: 0;
points(trva, col = "red")</pre>
```

legend("bottomright", legend = c("Preditcion (validation)", "Original data"), col = 1:2, pch = c(1, 1))

As we can	see from	the resulting	plot, the	e neural	network	did a	a great	job	predicting	the sine	function	from
the tiny ar	nount of	data used.										