# Statistical analysis

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### Statistical analysis

In this report, we will perform a statistical analysis to a biomedical dataset.

#### The dataset

The data belongs to the *Duke University Cardiovascular Disease Databank* and includes records and features of patients under diagnostic cardiac catheterization. The dataset has 3504 patients and 6 features.

Data obtained from http://biostat.mc.vanderbilt.edu/DataSets

#### Data overview

We will start by importing the data.

```
library(Hmisc)

## Loading required package: lattice

## Loading required package: survival

## Loading required package: Formula

## Loading required package: ggplot2

##

## Attaching package: 'Hmisc'

## The following objects are masked from 'package:base':

##

## format.pval, units

getHdata(acath)
```

Let's check we imported the righ dataset.

```
dim(acath)
```

```
## [1] 3504 6
```

The dataset has 3504 samples and 6 features, as we introduced in the previous section.

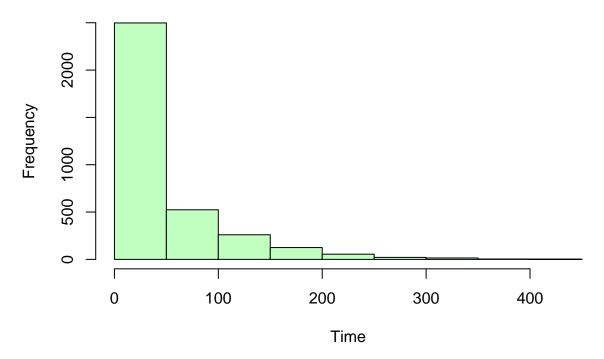
Let's use the *summary*, str and names functions to overview the data.

```
names (acath)
## [1] "sex"
                  "age"
                              "cad.dur"
                                         "choleste" "sigdz"
                                                                "tvdlm"
summary(acath)
##
                                         cad.dur
                                                        choleste
         sex
                           age
##
    Min.
           :0.0000
                     Min.
                             :17.00
                                                    Min.
                                                            : 29.0
                                                     1st Qu.:196.0
##
    1st Qu.:0.0000
                     1st Qu.:46.00
                                      1st Qu.:
                                                4
##
   Median :0.0000
                     Median :52.00
                                      Median: 18
                                                    Median :224.5
##
  Mean
           :0.3136
                                             : 43
                     Mean
                             :52.28
                                      Mean
                                                    Mean
                                                            :229.9
##
    3rd Qu.:1.0000
                     3rd Qu.:59.00
                                      3rd Qu.: 60
                                                     3rd Qu.:259.0
##
    Max.
           :1.0000
                     Max.
                             :82.00
                                      Max.
                                             :416
                                                    Max.
                                                            :576.0
##
                                                     NA's
                                                            :1246
##
        sigdz
                         tvdlm
##
    Min.
           :0.0000
                     Min.
                             :0.0000
##
    1st Qu.:0.0000
                     1st Qu.:0.0000
##
    Median :1.0000
                     Median :0.0000
##
    Mean
           :0.6661
                             :0.3225
                     Mean
                     3rd Qu.:1.0000
##
    3rd Qu.:1.0000
##
    Max.
           :1.0000
                     Max.
                             :1.0000
##
                     NA's
                             :3
str(acath)
                    3504 obs. of 6 variables:
   'data.frame':
              : 'labelled' int 0001100000...
              : 'labelled' int 73 68 54 58 56 64 65 41 68 52 ...
##
##
     ..- attr(*, "label")= chr "Age"
     ..- attr(*, "units")= chr "Year"
    $ cad.dur : 'labelled' int 132 85 45 86 7 0 76 15 30 1 ...
##
    ..- attr(*, "label") = chr "Duration of Symptoms of Coronary Artery Disease"
##
    \ choleste: 'labelled' int \ 268 120 NA 245 269 NA NA 247 NA NA ...
##
##
     ..- attr(*, "label")= chr "Cholesterol"
     ..- attr(*, "units")= chr "mg %"
##
##
    $ sigdz
              : 'labelled' int
                                1 1 1 0 0 1 1 1 1 1 ...
     ..- attr(*, "label")= chr "Significant Coronary Disease by Cardiac Cath"
##
              : 'labelled' int 1 1 0 0 0 0 1 0 1 0 ...
     ..- attr(*, "label") = chr "Three Vessel or Left Main Disease by Cardiac Cath"
##
    - attr(*, "comment") = chr "Data from the Duke University Cardiovascular Disease Databank"
```

From the overview, we can notice that we have several  $missing\ values$ , specially in choleste and tvdlm features. Let's study the features more closely.

For instance, let's plot the distribution of cad.dur variable, which is the duration of the heart symptoms.

# Distribution of heart symptoms in the coronary artery disease



We could also check the maximum and minimum of the variable age.

```
print(paste0("The older patient is ", max(acath$age), " years old"))
## [1] "The older patient is 82 years old"
print(paste0("and the youngest patient is ", min(acath$age), " years old"))
```

## [1] "and the youngest patient is 17 years old"

Another interesting question we could make is how many patients had high level of cholesterol (more than 200).

```
nrow(subset(acath, acath$choleste>200))
```

## [1] 1602

1602 patients had high cholesterol.

#### Probability and simulation

Now, let's use probaility theory to answer some questions:

• What is the probability to find more than 60 patients with the disease if 100 tests were performed?

This case follows a binomial distribution, therefore we need to find the probability to have the disease from the data.

```
est<-subset(acath,acath$sigdz==1) #patients with the disease
p<-nrow(est)/nrow(acath) #probability = patients with the disease/total patients</pre>
```

Once we have the probability p, we can solve the question:

```
p60<-1-pbinom(60,100,p,lower.tail=T) #dist binomial print(paste0("The probability to find more than 60 patients with the disease after evaluating 100 tests
```

- ## [1] "The probability to find more than 60 patients with the disease after evaluating 100 tests is 0."
  - Probability of not having the disease if someone has a narrow coronary artery?

This follows conditional probability as:

$$P(no\: disease | narrow\: artery) = \frac{P(no\: disease \bigcap narrow\: artery)}{P(narrow\: artery)}$$

Let's calculate the probabilities:

```
sya<-subset(acath,acath$tvdlm==0 & acath$sigdz==1)
psya<-nrow(sya)/nrow(acath) #probability no disease and narrow artery
ps<-psya/p #conditional probability
print(paste0("Probability of not having the disease while having narrow coronary artery is ",ps))</pre>
```

## [1] "Probability of not having the disease while having narrow coronary artery is 0.515424164524422"

In some situations, performing simulations can be very useful when analyzing data. For instance, let's simulate 10,000 times the number of patients with a narrow coronary artery if 100 tests were performed.

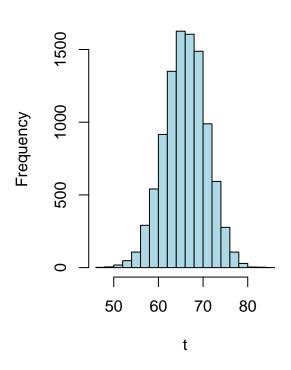
```
set.seed(12345)
t<-rbinom(10000,100,p)
str(t)</pre>
```

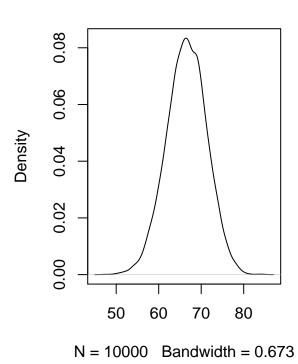
## int [1:10000] 72 65 67 63 74 63 71 72 66 61 ...

```
#plots
par(mfrow=c(1,2))
hist(t,col="lightblue")
plot(density(t))
```



## density.default(x = t)





mean(t)

## [1] 66.5515

sd(t)

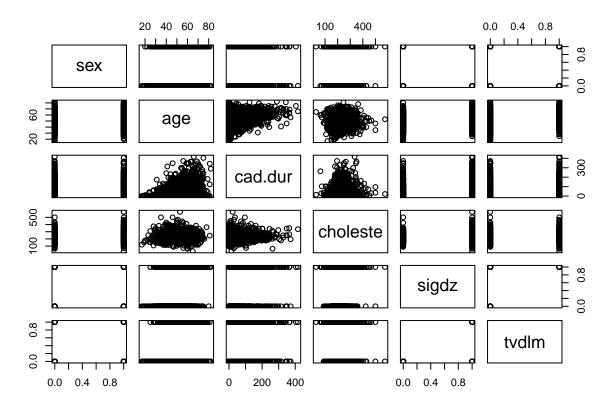
## [1] 4.718429

As we could expect, the mean obtained simulating 10,000 times is very close to the 1-time mean. It is interesting that the standard deviation is not important, therefore there is not much variability in the process.

#### Regression analysis

Regression analysis is also very useful when answering questions about our data. For instance, let's question how age influences in the duration of the symptoms.

pairs(acath)



Let's generate the linear regression model with *symptoms duration* and *age*.

```
RegModel <- lm(cad.dur~age, data=acath)
summary(RegModel)</pre>
```

```
##
## Call:
## lm(formula = cad.dur ~ age, data = acath)
##
## Residuals:
## Duration of Symptoms of Coronary Artery Disease
             1Q Median
                           3Q
                                 Max
##
  -89.56 -34.89 -16.10 17.07 349.95
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) -44.79200
                           5.04381 -8.881
                                             <2e-16 ***
## age
                 1.67937
                           0.09479 17.717
                                             <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 55.72 on 3502 degrees of freedom
## Multiple R-squared: 0.08226,
                                   Adjusted R-squared: 0.082
## F-statistic: 313.9 on 1 and 3502 DF, p-value: < 2.2e-16
```

Determination coefficient is 0.08226. The model has a low explanatory power, so the model is not idoneal or the variables are independent.

Next, let's calculate the correlation coefficient between these variables.

```
cor(acath[,c("age","cad.dur")])
```

```
## age cad.dur
## age 1.000000 0.286806
## cad.dur 0.286806 1.000000
```

The coefficient is 0.2868. As we suspected, the dependency is low.

After this analysis, we can conclude that variable age doesn't influence in a significant level to the variable  $symptoms\ duration$ .