

## 1. Calculation by hand

a) 4  $x^2 + y^2 + A_x + B_y = C$

b) 6  $(4;6) \begin{cases} 16+36+4A+6B = C \\ (1;4) \end{cases}$

$(1;4) \begin{cases} 1+16+A+4B = C \\ (2;3) \end{cases}$

c) 1  $(2;3) \begin{cases} 4+9+2A+3B = C \end{cases}$

d) 4  $\begin{cases} 4A+6B-C = -52 \\ A+4B-C = -17 \end{cases}$

e) 2  $\begin{cases} 2A+3B-C = -13 \end{cases}$

f) 3  $\left[ \begin{array}{ccc|c} 4 & 6 & -1 & -52 \\ 1 & 4 & -1 & -17 \\ 2 & 3 & -1 & -13 \end{array} \right] \xrightarrow{\div 4} \left[ \begin{array}{ccc|c} 1 & 1,5 & -0,25 & -13 \\ 1 & 4 & -1 & -17 \\ 2 & 3 & -1 & -13 \end{array} \right] \xrightarrow{\begin{matrix} -R_1 \\ -2R_1 \end{matrix}}$

$\left[ \begin{array}{ccc|c} 1 & 1,5 & -0,25 & -13 \\ 0 & 2,5 & -0,75 & -4 \\ 0 & 0 & -0,5 & 13 \end{array} \right] \xrightarrow{\div 2,5} \left[ \begin{array}{ccc|c} 1 & 1,5 & -0,25 & -13 \\ 0 & 1 & -0,3 & -1,6 \\ 0 & 0 & -0,5 & 13 \end{array} \right] \xrightarrow{-1,5R_2} \left[ \begin{array}{ccc|c} 1 & 0 & 0,2 & -10,6 \\ 0 & 1 & -0,3 & -1,6 \\ 0 & 0 & -0,5 & 13 \end{array} \right] \xrightarrow{\div (-0,5)}$

$\rightarrow \left[ \begin{array}{ccc|c} 1 & 0 & 0,2 & -10,6 \\ 0 & 1 & -0,3 & -1,6 \\ 0 & 0 & 1 & -26 \end{array} \right] \xrightarrow{\begin{matrix} -0,2R_3 \\ +0,3R_3 \end{matrix}} \left[ \begin{array}{ccc|c} 1 & 0 & 0 & -5,4 \\ 0 & 1 & 0 & -9,4 \\ 0 & 0 & 1 & -26 \end{array} \right]$

$$x^2 + y^2 - 5,4x - 9,4y = -26$$

$$(x-2,7)^2 - 2,7^2 + (y-4,7)^2 - 4,7^2 = -26$$

$$(x-2,7)^2 + (y-4,7)^2 = 3,38$$

$$r = \sqrt{3,38} = 1,84$$

$$\text{Centre : } (2,7; 4,7)$$

## 2. Python

```
3. import csv # importing CSV library to use csv functions
4. from typing import List
5.
6. import numpy as np # importing CSV library to use matrix-calculations
7.
8. # The class Point initializes an object with x and y coordinates as float
   values.
9. class Point:
10.     def __init__(self, x, y):
11.         self.x = float(x)
12.         self.y = float(y)
13.
14.     # [\]
15.
16.     def print(self):
17.         """
18.         prints the values of the attributes "x" and "y".
19.         """
20.         print("{0} {1}".format(self.x, self.y))
21.
22.     # [\]
23.     def circeq(self):
24.         return [self.x, self.y, -1]
25.
26.     def circsq(self):
27.         return -self.x**2 - self.y**2
28.
29.     x = 0
30.     y = 0
31.
32. def dictionary(self):
33.     """
34.     The function returns the dictionary representation of an object's
       attributes.
35.     :return: The method `dictionary` is returning the dictionary
       representation of the object's
36.     attributes using the `__dict__` attribute.
37.     """
38.     return self.__dict__
39.
40. # [\]
41. # `inputarray = []` initializes an empty list called `inputarray`. This
   list will be used to store
42. # `Point` objects created from the data in the input file.
43. inputarray = []
44. # [\]
45.
```

```

46.# This code is opening a CSV file named "inputfile AS1.csv" in read mode
    using the `open()` function
47.# and assigning it to the variable `input`. Then, it is using the
    `csv.DictReader()` function to read
48.# the contents of the CSV file and convert them into a dictionary format.
    The resulting dictionary is
49.# assigned to the variable `locations`. The `with` statement is used to
    ensure that the file is
50.# properly closed after it has been read.
51.with open(r"inputfile AS1.csv", "r") as input:
52.    locations = csv.DictReader(input)
53.    # [\]
54.
55.    # Essentially, this code is converting the data from the input CSV file
    into a list of `Point` objects
56.    # that can be used for further calculations.
57.    for pointentry in locations:
58.        point = Point(pointentry["x"], pointentry["y"])
59.        inputarray.append(point)
60.# [\]
61.
62.# `calccarray = np.array(inputarray)` is converting the list of `Point`
    objects stored in `inputarray`
63.# into a numpy array called `calccarray`. This allows for easier
    manipulation and calculation of the
64.# data using numpy functions.
65.calccarray = np.array(inputarray)
66.# [\]
67.
68.# `numOfRows = calccarray.shape[0]` is calculating the number of rows in the
    numpy array `calccarray`
69.# and assigning it to the variable `numOfRows`. This value is used later in
    the code to determine if
70.# there are exactly three points in the input file, in which case a circle
    will be calculated.
71.numOfRows = calccarray.shape[0]
72.# [\]
73.
74.sol = []
75.eq = []
76.# This code block checks if the number of rows in the input CSV file is
    equal to 3. If it is, then it
77.# assumes that the input file contains three points and calculates the
    equation of the circle that
78.# passes through those three points.
79.if numOfRows == 3:
80.    print("Given three points a circle will be calculated")
81.    for n in range(3):

```

```

82.         eq.append(inputarray[n].circeq())
83.         sol.append(inputarray[n].circsq())
84.     eqarray = np.array(eq)
85.     solarray = np.array(sol)
86.     solution = np.linalg.solve(eqarray, solarray)
87. # [\]
88.
89. # additional +/- formatting (You do not need to implement this but it is
    recommended to do)
90. if solution[0] < 0:
91.     pr_sol0 = str(solution[0])
92. else:
93.     pr_sol0 = "+" + str(solution[0])
94. if solution[1] < 0:
95.     pr_sol1 = str(solution[1])
96. else:
97.     pr_sol1 = "+" + str(solution[1])
98. if solution[2] < 0:
99.     pr_sol2 = str(solution[2])
100. else:
101.     pr_sol2 = abs(solution[2])
102.
103. Equation = ["Equation:", "x^2+y^2{0}x{1}y = {2}".format(pr_sol0,
    pr_sol1, pr_sol2)]
104. print(Equation[0], Equation[1])
105.
106. #This code is writing the equation of the circle calculated
107. # earlier to a new CSV file named "outputfile AS1.csv".
108. f = open("outputfile AS1.csv", "w")
109.
110. writer = csv.writer(f)
111. writer.writerow(Equation)
112.
113. f.close()
114. # [\]
115.

```