## Harmonic Signals and Elementary Operations

## Exercise 1:

A harmonic signal has the form:

$$y(t) = A\cos(\omega t + \phi)$$

In this, A,  $\omega$  and  $\phi$  are parameters.

Note: Plot the graphs of exercises A) and E) in one figure using the  $\underline{subplot(2,1,1)}$  and  $\underline{subplot(2,1,2)}$  commands respectively.

For A = 1,  $\omega = 2\pi f$  with f = 5 Hz and  $\phi = 0$  rad,

- A) Plot the signal y(t) using a time vector ranging from 0 to 1 second that has 200 time steps per period of y(t).
- B) What is the effect of A in y(t)? (Vary this parameter in the code to see the effect)
- C) What is the effect of  $\omega$  in y(t)? (Vary this parameter in the code to see the effect)
- D) What is the effect of  $\phi$  in y(t)? (Vary this parameter in the code to see the effect)

In essence, our answer in A) is a discretization of the signal y(t). However, it is plotted versus  $nT_s$  instead of versus n. Moreover, the sample time  $T_s$  is taken so small that it looks as if it's a continuous-time signal. You can see this by plotting markers using "plot(t,y, '-x')". The marker '-x' can be replaced by a variety of other markers: '-o', '-s', etc.

For A = 1,  $\omega = 2\pi f$  with f = 5 Hz and  $\phi = 0$  rad,

- E) Plot y[n], the discrete version of y(t), versus n with  $\Omega = \frac{1}{10} * 2\pi$  using the stem(x,y) command. Make sure you choose n such that the domain in continuous time is  $0 \le t \le 1$  s.
- F) What is the sample time T<sub>s</sub> in E). ?

Using:

$$x_1(t) = 0.5\cos\left(2\pi 5t + \frac{1}{4}\pi\right)$$
 
$$x_2(t) = 0.3\cos(2\pi 10t)$$

- G) What is A in x<sub>1</sub>?
- H) What is φ in x<sub>2</sub>?
- What is ω in x<sub>1</sub>?
- J) What is the period of x<sub>2</sub>?

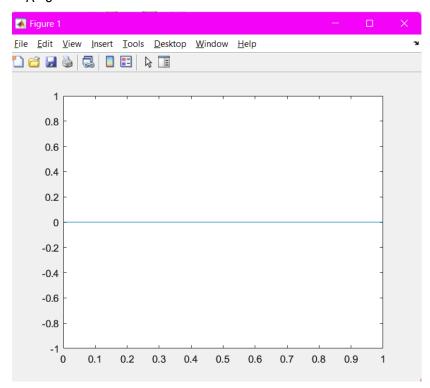
Assume now that we sample with a sample frequency of 7 Hz, which leaves us with  $x_1[n]$  and  $x_2[n]$ .

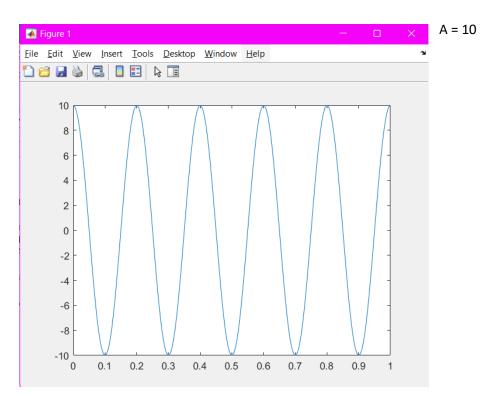
$$x_1[n] = 0.5 \cos\left(\frac{10\pi}{7}n + \frac{1}{4}\pi\right)$$
  
 $x_2[n] = 0.3 \cos\left(\frac{20\pi}{7}n\right)$ 

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Exercise 1
 Task A
 A=1;
 f=5;
 fi=0;
 w=2*pi()*f;
 t=linspace(0,1,200);
 for ii=1:length(t)
  y(ii)=A*cos(w*t(ii)+fi);
  end
 %y=A*cos(w*t+fi); (Another solution to make a graph)
 plot(t,y)
Figure 1
                                                                                  X
<u>F</u>ile <u>E</u>dit <u>V</u>iew <u>I</u>nsert <u>T</u>ools <u>D</u>esktop <u>W</u>indow <u>H</u>elp
               🛃 📘 📰
        1
       0.8
       0.6
       0.4
       0.2
        0
      -0.2
      -0.4
      -0.6
      -0.8
       -1<sub>0</sub>
                 0.1
                        0.2
                                0.3
                                       0.4
                                              0.5
                                                      0.6
                                                              0.7
                                                                     8.0
                                                                            0.9
```

Task B

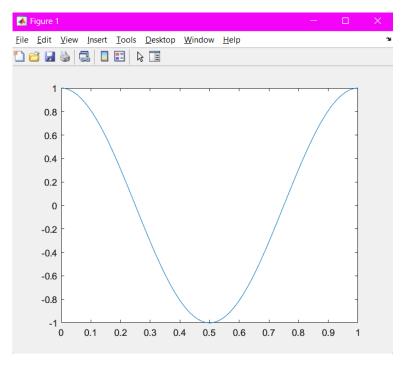
A= 0





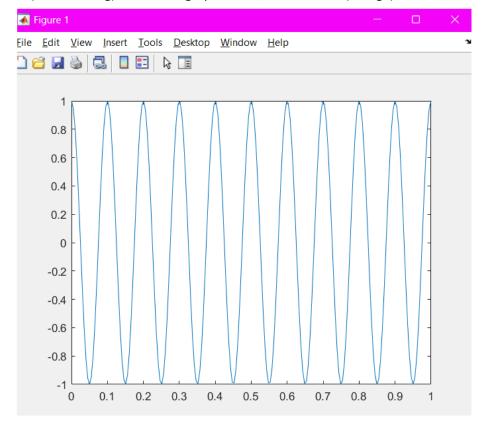
If you change A, then Y axis increases, amplitude becomes higher.

Task C

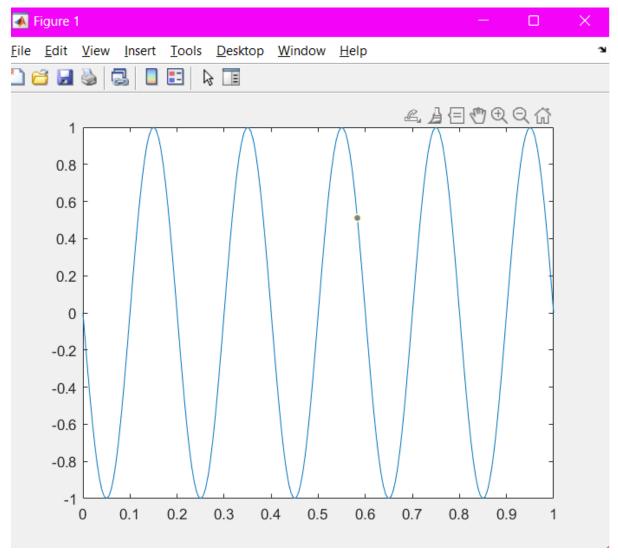


W=6.28 if f=1

If you change f, then omega also changes and if omega is changed, then period of the graph decreases (is decreasing). Check the graph under, in this case w(omega) = 62.83, f = 10 Hz



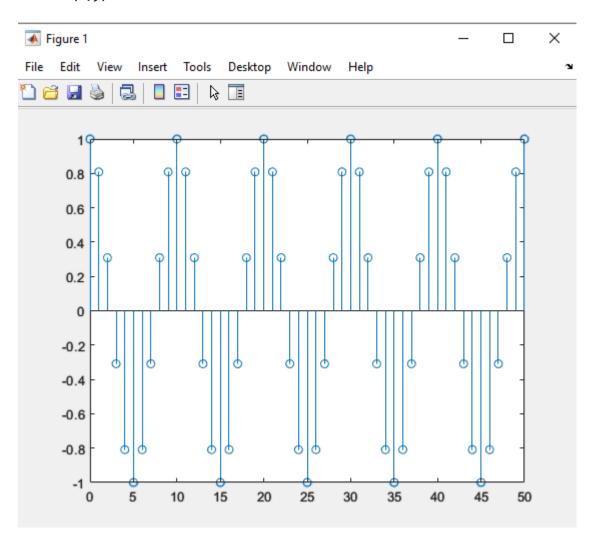
Task D  $\label{eq:definition}$  If you change  $\phi$ , then graph shifts on horizontal axis making phase shifts.



In this case graph fi is pi/2, so graph shifts for 90 degrees from Task A graph.

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Task E

t=linspace(0,1,201);
%t=0:1;
A=1;
f=5;
fi=0;
w=2*pi()*f;
W=((1/10)*2*pi());
Ts=(W/w);
n=(t./Ts);
n1=round(n);
N=unique(n1);
y=A*cos(W*N+fi);
stem(N,y)
```



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Task F
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Sample time Ts = 0.02 s
```

Tasks G, H, I, J

G) 
$$A = 0.5$$

H) fi = 0 degrees

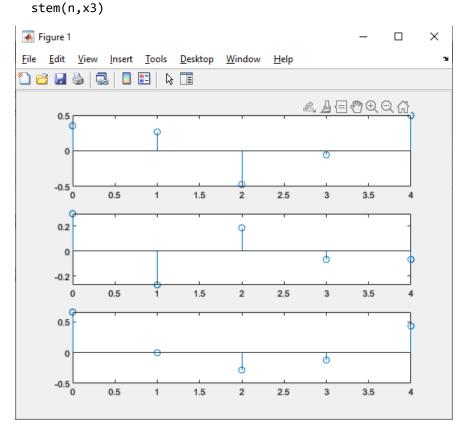
I) 
$$w = 2*pi*5$$

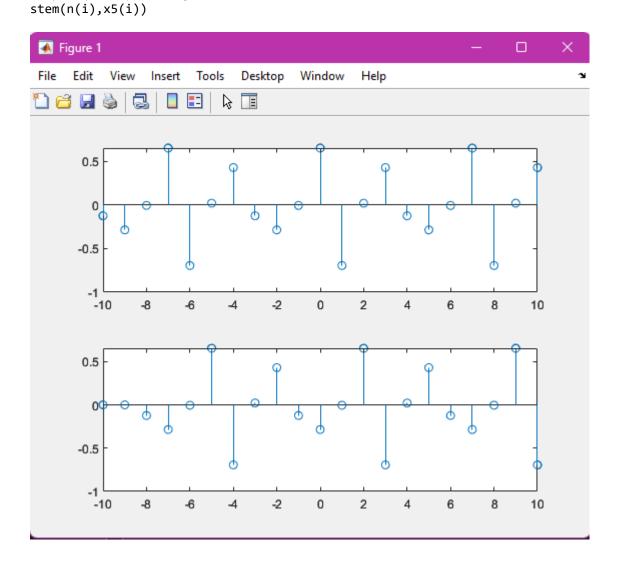
J) 
$$w=2*pi/T \rightarrow 2*pi*10 = 2*pi/T \rightarrow T = 1/10 = 0.1 s$$

## Exercise 2

```
Tasks K and L
```

```
n=0:4;
subplot(3,1,1);
x1=0.5*cos(((10*pi)/7)*n+(1/4)*pi);
stem(n,x1)
subplot(3,1,2);
x2=0.3*cos(((20*pi)/7)*n);
stem(n,x2)
subplot(3,1,3); %sum
x3=x1+x2;
```





Exercise 3

