

I Phonon mediated tunneling into TaS₂

I.1 Amplitude mode in TaS₂ charge density wave

From the 81 modes found in the phonon calculation at the Γ point in sec. ??, one particular mode has the effect of displacing the atoms in the direction of the symmetric phase, thus changing the amplitude of the charge density wave. This is depicted in fig. ??. The amplitude mode has an energy of $E_0 = 10.6$ meV.

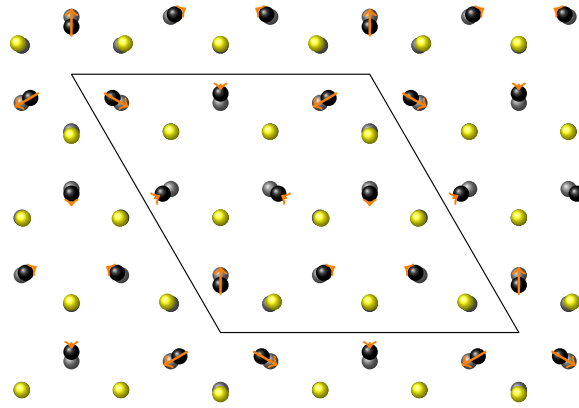


Figure I.1: Amplitude mode in TaS₂ charge density wave, visualized from QUANTUM ESPRESSO calculation. Gray dots are atoms in the symmetric phase, yellow/black dots are the Tantalum/Sulfide atoms in the charge density wave phase. The orange arrows show the displacement vectors.

I.2 Phonon mediated tunneling in Graphene

I.2.1 Scanning Tunneling Spectroscopy

The description in this section follows the textbook “Surface Science” by Oura et al. [1].

Scanning Tunneling Spectroscopy (STS) is an experimental technique in which a Scanning Tunneling Microscope (STM) is used to map the density of states of a material.

In an STM setup, a very sharp metallic tip is placed close to the probed surface, such that electrons can tunnel between the tip and the surface (around $5 - 10$ Å). By applying a bias voltage V between the tip and the surface, a current enabled by the tunneling process flows

through the gap. This tunneling current is sharply dependent on the size of the gap, so a extremely high vertical resolution can be achieved. Also due to this fact, 90 % of the tunneling current flows through the the single tip atom closest to the surface, so that very high lateral resolution is also possible. An **STM** can thus be used to map the topography of a surface with atomic resolution.

When varying the bias voltage V , an **STM** can also be used to obtain measurements of the density of electronic states in the material, the **STS** mode of operation. This is due to the tunneling current being determined by summing over electron states in an energy interval defined by the bias voltage. In general, a simple interpretation of **STS** data is not possible and need backing in theoretical calculations. This is due to the tunneling current depending on the tunneling matrix element between the state at the tip and the states in the probe, so the tunneling current can be suppressed if the states in the probe don't overlap with the tip.

I.2.2 Phonon mediated tunneling in Graphene

In a 2008 **STS** measurement on graphene, a gap feature around the fermi level was measured [2]. This gap is as an example of the problems with interpretation of **STS** data explained in sec. I.2.1, as it is not a feature of the density of states of graphene, but a result of the tunneling current being suppressed for the range of bias voltages in the gap.

The underlying mechanism, confirmed with **DFT** calculations by Wehling et al. [3] is as follows: generally, electrons can elastically tunnel into graphene at the Fermi level near the **K** point. This elastic process is suppressed because the wave function at the initial state i.e. the wave functions at the tip have a momentum distribution centered at $k_{\parallel} = 0$, so the tunneling matrix element is suppressed for large k [4]. For electron energies outside the gap, an inelastic tunneling channel opens, where the electrons first tunnels into the σ^* band and then transitions into an available **K** point through emission of a **K'** point phonon (pictured in fig. ??).

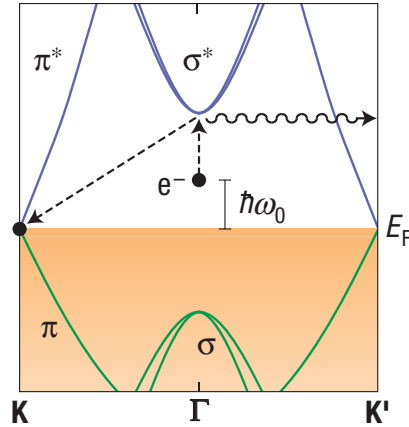


Figure I.2: Inelastic tunneling mechanism involving graphene phonon modes near the **K** point in reciprocal space. Reprinted by permission from Nature Publishing Group: Nature Physics [2], copyright 2008

I.3 Phonon mediated tunneling into TaS₂

In a 2019 paper by Hall et al. [5], a similar gap feature with a width of $2\Delta = (32 \pm 9)$ meV was recorded in an STS measurement on TaS₂.

This gap is attributed to partial gapping to the formation of the charge density wave, as explained in the one-dimensional case in sec. ??.

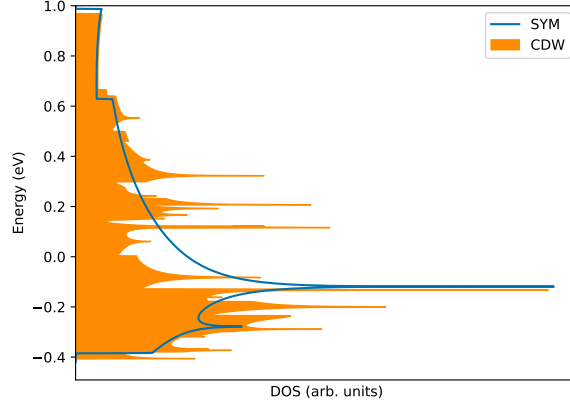


Figure I.3: Density of states for TaS₂ in the charge density wave (CDW) and undistorted (SYM) phase. The data was kindly provided by Dr. Jan Berges and has been calculated in QUANTUM ESPRESSO with the 2D tetrahedron method using 360^2 (1080^2) k points for the CDW (SYM) structure

The density of states shown in fig. ?? shows no symmetric gap around the Fermi level, so there is grounds to reject the explanation by partial gapping is not confirmed. An alternative explanation can be that the same process found in graphene in sec. I.2.2 produces the gap in TaS₂. The energy of the amplitude mode found in sec. I.1, $E_0 = 10.6$ meV fits to the width of the gap $\Delta = (16.0 \pm 4.5)$ meV.