

# I Dynamical Mean-Field Theory

Source: **Georges\_Kotliar\_Krauth\_Rozenberg\_1996 - Georges\_Kotliar\_Krauth\_Rozenberg\_1996**

Most general non-interacting electronic Hamiltonian in second quantization:

$$H_0 = \sum_{i,j,\sigma} \quad (\text{I.1})$$

with lattice coordinates  $i, j$  and spin  $\sigma$ .

One particle Green's function (many-body object, coming from the Hubbard model):

$$G(\mathbf{k}, i\omega_n) = \frac{1}{i\omega_n + \mu - \epsilon_{\mathbf{k}} - \Sigma(\mathbf{k}, i\omega_n)} \quad (\text{I.2})$$

with the self energy  $\Sigma(i\omega_n)$  coming from the solution of the effect on-site problem:

The Dyson equation

$$G(\mathbf{k}, i\omega_n) = (G_0(\mathbf{k}, i\omega_n) - \Sigma(\mathbf{k}, i\omega_n))^{-1} \quad (\text{I.3})$$

relates the non-interacting Greens function  $G_0(\mathbf{k}, i\omega_n)$  and the fully-interacting Greens function  $G(\mathbf{k}, i\omega_n)$  (inversion of a matrix!).