

# Application of the Finite-Momentum Method

## 1.1 Decorated Graphene Model

#### **Critical Temperatures**

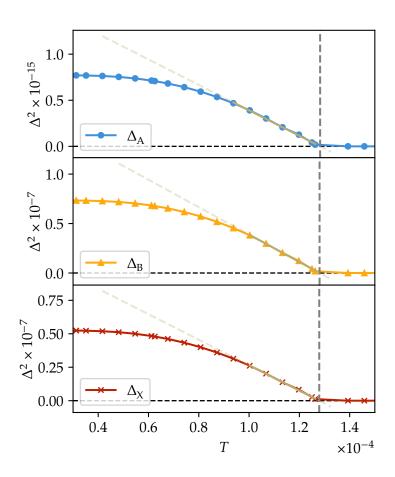


Figure 1.1 – Linear fit for extracting the critical temperature

Critical temperatures via ??:

$$|\Psi|^2 \propto T_C - T. \tag{1.1}$$

Fit and corresponding  $T_C$  are shown in fig. 1.1. Notable:

• the gaps  $\Delta_{\alpha}$  have very different orders of magnitude, but fall in the same way, i.e. have the same critical temperature

Can plot critical temperatures against V and U. Figure 1.2 shows  $T_C$  and gaps against V.

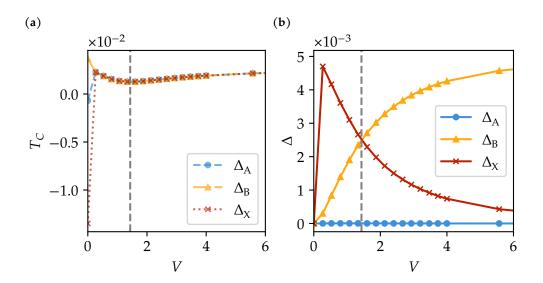


Figure 1.2 – T (a) Critical temperatures vs V. (b) Gaps vs V.

#### Notable:

- Miminum of  $T_C$  and gaps at some V=1.43, corresponds with metallic V in repulsive Hubbard model
- But no gap closure
- TC follows maximal gap
- What is happening at V = 0? New jobs

This

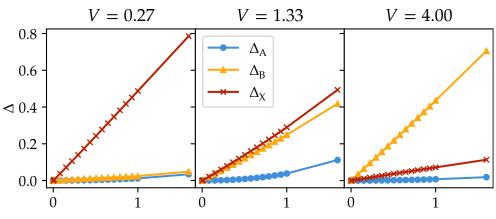


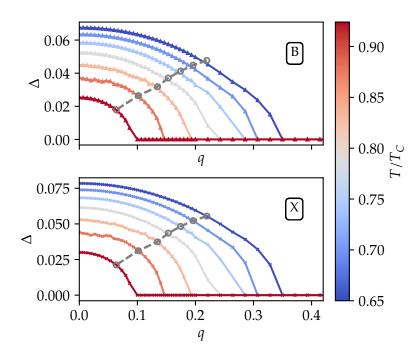
Figure 1.3 shows  $T_C$  and gaps against U for different V.

Figure 1.3 – Gaps vs U. for different V

- Low V: flat band on X, high V: flat band on Graphene B, medium V: both
- Linear with interaction strength, typical for flat band in BCS (reference)
- mirrors the switchover seen in the gaps against V and the band structure

#### **Extracting the Superconducting Length Scales**

Plot two important gaps against *q* in fig. 1.4 for a medium V



**Figure 1.4** – Gap vs q

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Plot two important gaps against q in fig. 1.5 for a high and low V

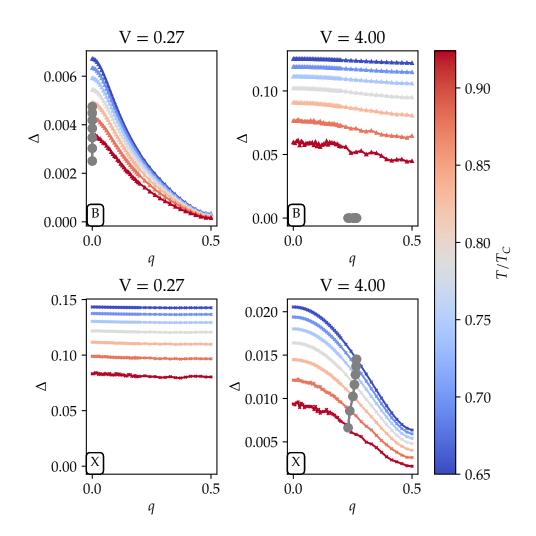


Figure 1.5 – Gap vs q

Take

$$\xi(T) = \frac{1}{\sqrt{2}|\mathbf{Q}|}\tag{1.2}$$

with **Q** such that

$$|\frac{\psi_{\mathbf{Q}}(T)}{\psi_0(T)}| = \frac{1}{\sqrt{2}} \tag{1.3}$$

Plot also current against q fig. 1.6

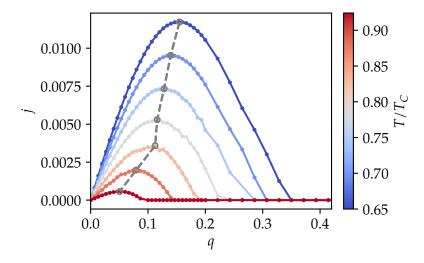


Figure 1.6 – Current against q

Notable:

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Calculate  $\xi(T)$  and  $\lambda_L(T)$ . Plot against T and fit to get  $\xi_0$ ,  $\lambda_{L,0}$ .

Plot also current for low and high V

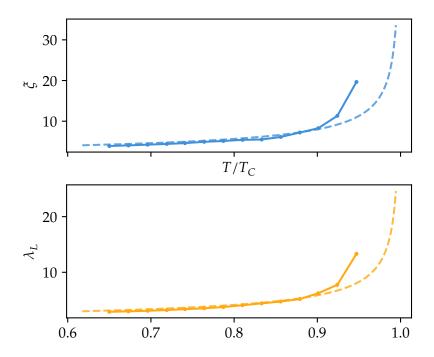
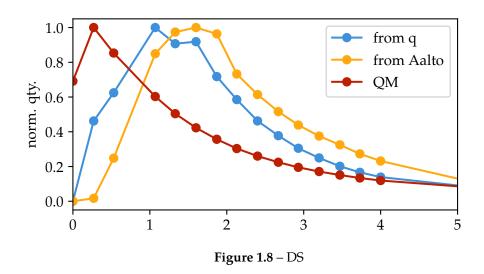


Figure 1.7 – Temperature fits for xi and lambda

#### **Length Scales**

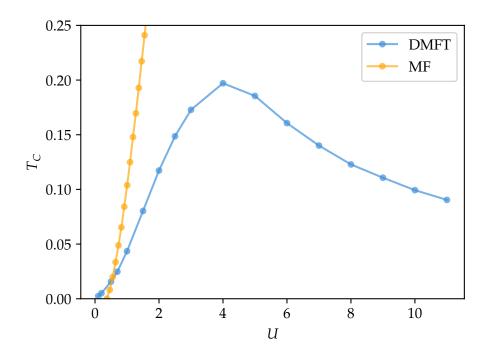
Plot SC length scales vs V, between different gaps

More data points for quantum metric, x axis



# 1.2 One-Band Hubbard Model on the Square Lattice

Can extract  $T_C$  same way as above. Plot it against U.

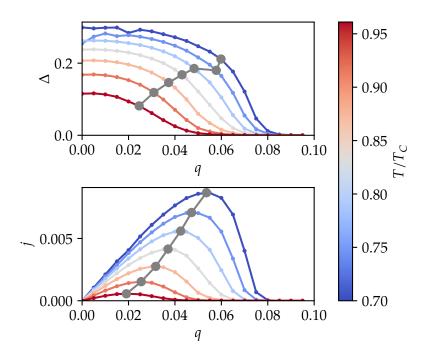


**Figure 1.9** – TC against U (also mean field results)

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#### **Extracting Superconducting Length Scales**

Extraction same as before, plot gap and current against q in section 1.2.



**Figure 1.10** – Gap and current vs q.

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Calculate  $\xi(T)$  and  $\lambda_L(T)$ . Plot against T and fit to get  $\xi_0$ ,  $\lambda_{L,0}$ .

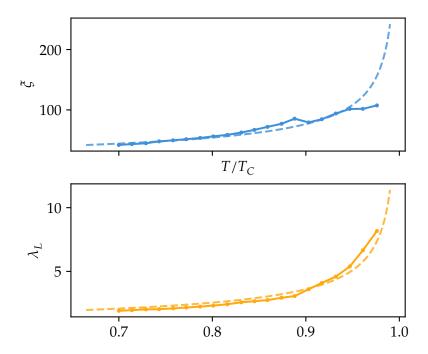
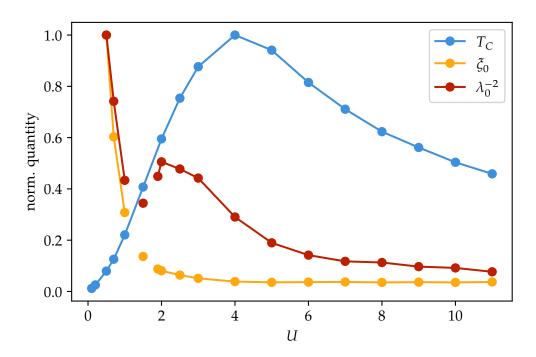


Figure 1.11 – Temperature fits for xi and lambda

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#### **BCS-BEC Crossover**



 $\textbf{Figure 1.12} - Normalized \ TC/xi/DS \ against \ U \ (to \ show \ BCS-BEC \ crossover)$ 

### **Comparison of MF and DMFT Data**

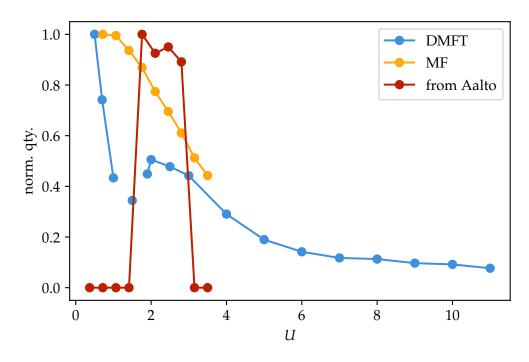


Figure 1.13

Plot MF and DMFT xi and lambda against U