

I Coherence length and penetration depth in strongly correlated superconductors

Put in source

Order parameter (OP) of a superconducting condensate with FMP has the form

$$\Psi_{\mathbf{q}}(\mathbf{r}) = |\Psi_{\mathbf{q}}|e^{i\mathbf{q}\mathbf{r}} \quad (\text{I.1})$$

where \mathbf{q} is the center-of-mass momentum of Cooper pairs.

FMP is well known from Fulde-Ferrel-Larkin-Ovchinnikov (FFLO) theory, where the single-momentum phase used here corresponds to FF-type pairing.

What does that mean? More details on FFLO theory

I.1 Ginzburg-Landau description

First: Motivate how the FMP constraint relates to λ_L and ξ_0 .

GL low-order expansion of the free energy density f_{GL} in terms of the FMP-constrained OP reads

$$1 \quad (\text{I.2})$$

Fill in equation

The temperature dependent correlation length ξ appears as the natural length scale of the amplitude mode ($\propto \alpha$) and kinetic energy term

More details on GL theory in general

$$\xi(T) = \quad (\text{I.3})$$

with the zero temperature value ξ_0 being the coherence length.

Fill in equation

I.2 Phase transitions and broken symmetry

Following [colemanIntroductionManyBodyPhysics2015].

I.2.1 Order parameter concept

Landau theory: phase transitions (e.g. iron becomes magnetic, water freezes, superfluidity/superconductivity) are associated with the development of an order parameter when the temperature drops below the transition temperature T_C

$$|\psi| = \begin{cases} 0, & T > T_C \\ |\psi_0| > 0, & T < T_C \end{cases} \quad (\text{I.4})$$

Landau theory does not need microscopic expression for order parameter, it provides coarse-grained description of the properties of matter. The order parameter description is good at length scales above ξ_0 , the coherence length (e.g. size of Cooper pairs for SC).

This works also for phase transitions not dependent of temperatures, so e.g. in pressures?

I.2.2 Landau theory

Landau theory

Going from a one to a n -component order parameters, we can actually

Particularly important example: complex or two component order parameter in superfluids and superconductors:

$$\psi = \psi_1 + i\psi_2 = |\psi|e^{i\phi} \quad (\text{I.5})$$

The Landau free energy takes the form:

$$f[\psi] = r(\psi^*\psi) + \frac{u}{2}(\psi^*\psi)^2 \quad (\text{I.6})$$

Figure I.1 shows the Landau free energy as function of ψ .

In this ‘Mexican hat’ potential: order parameter can be rotated continuously from one broken-symmetry state to another. If we want the phase to be rigid, we need to introduce an There is a topological argument for the fact that the phase is rigid. This leads to Ginzburg-Landau theory. Will see later: well-defined phase is associated with persistent currents or superflow.

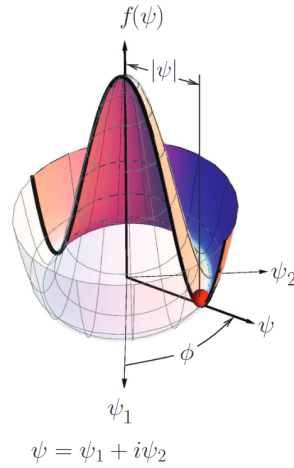


Figure I.1: Mexican hat potential

I.2.3 Ginzburg-Landau theory I: Ising order

I.2.4 Ginzburg-Landau theory II: complex order and superflow

Now: G-L theory of complex or two-component order parameters, so superfluids and superconductors. Heart of discussion: emergence of a ‘macroscopic wavefunction’, where the microscopic field operators $\hat{\psi}(x)$ acquire an expectation value:

$$\langle \hat{\psi}(x) \rangle = \psi(x) = |\psi(x)|e^{i\theta(x)} \quad (\text{I.7})$$

Magnitude determines density of particles in the superfluid:

$$|\psi(x)|^2 = n_s(x) \quad (\text{I.8})$$

Twist/gradient of phase determines superfluid velocity:

$$\mathbf{v}_s(x) = \frac{\hbar}{m} \nabla \phi(x) \quad (\text{I.9})$$

We will derive this later in the chapter. Counterintuitive from quantum mechanics: GL suggested that $\Phi(x)$ is a macroscopic manifestation of a macroscopic number of particles condensed into precisely the same quantum

Short introduction for one-component order parameter, so the connection to complex order parameters gets clear

What exactly are field operators again?

More info on that? Does that come later in chapter?

Here: rest of notes
from Goodnotes

Coherent states/In-
terpretation of
states/Off-diagonal
long-range order

Here: particle-
current operator,
especially for coher-
ent state, connection
with phase twist

Here: Meissner ef-
fect, etc

state. Emergent phenomenon, collective properties of mater not a-priori self-evident from microscopic physics.

Phase rigidity and superflow: in GL theory, energy is sensitive to a twist of the phase. Substitute $\psi = |\psi|e^{i\phi}$ into GL free energy, gradient term is:

$$\Delta\psi = () \quad (\text{I.10})$$

I.2.5 Ginzburg-Landau theory III: charged fields