

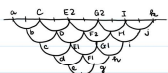
`In[ ]:= f[x_] := x^13 / (1 - x)^14`

`Sum[1, {a, 1, n - 10}, {b, a + 1, n - 9}, {c, b + 1, n - 8},  
{d, c + 1, n - 7}, {e, d + 1, n - 6}, {f, e + 1, n - 5}, {g, f + 1, n - 4},  
{h, g + 1, n - 3}, {i, h + 1, n - 2}, {j, i + 1, n - 1}, {k, j + 1, n}]`

`Out[ ]:= (3 628 800 n - 10 628 640 n^2 + 12 753 576 n^3 - 8 409 500 n^4 +  
3 416 930 n^5 - 902 055 n^6 + 157 773 n^7 - 18 150 n^8 + 1320 n^9 - 55 n^10 + n^11) / 39 916 800`

`In[ ]:= FullSimplify[(1 / 39 916 800) (3 628 800 n - 10 628 640 n^2 + 12 753 576 n^3 -  
8 409 500 n^4 + 3 416 930 n^5 - 902 055 n^6 + 157 773 n^7 - 18 150 n^8 + 1320 n^9 - 55 n^10 + n^11)]`

`Out[ ]:= 1  
39 916 800 (-10 + n) (-9 + n) (-8 + n) (-7 + n) (-6 + n) (-5 + n) (-4 + n) (-3 + n) (-2 + n) (-1 + n) n`

`In[ ]:= graph =` 

`Out[ ]:=` 

`In[ ]:= Sum[(C - a - 1) * (E2 - C - 1) * (G2 - E2 - 1) * (I - G2 - 1) * (k - I - 1) * (g - e - 1),  
{a, 1, n - 10}, {C, a + 2, n - 8}, {E2, C + 2, n - 6}, {G2, E2 + 2, n - 4}, {I, G2 + 2, n - 2},  
{k, I + 2, n}, {b, a + 1, C - 1}, {D, C + 1, E2 - 1}, {F2, E2 + 1, G2 - 1}, {H, G2 + 1, I - 1},  
{j, I + 1, k - 1}, {c, b + 1, D - 1}, {E1, D + 1, F2 - 1}, {G1, F2 + 1, H - 1}, {i, H + 1, j - 1},  
{d, c + 1, E1 - 1}, {F1, E1 + 1, G1 - 1}, {h, G1 + 1, i - 1}, {e, d + 1, F1 - 1}, {g, F1 + 1, h - 1}]`

`Out[ ]:= (-559 121 323 622 400 000 n + 3 401 517 236 060 160 000 n^2 -  
9 698 393 279 559 168 000 n^3 + 17 304 343 134 810 854 400 n^4 - 21 749 506 690 507 787 520 n^5 +  
20 539 198 819 797 499 584 n^6 - 15 171 179 338 268 712 000 n^7 + 9 005 548 196 457 282 800 n^8 -  
4 378 489 347 548 646 000 n^9 + 1 767 694 037 346 140 420 n^10 - 598 465 980 994 381 500 n^11 +  
171 092 005 786 051 025 n^12 - 41 490 587 106 783 600 n^13 + 8 555 985 678 275 480 n^14 -  
1 501 152 570 630 000 n^15 + 223 775 892 980 375 n^16 - 28 245 100 075 500 n^17 +  
3 001 244 399 450 n^18 - 266 150 197 500 n^19 + 19 454 882 975 n^20 - 1 151 706 600 n^21 +  
53 825 060 n^22 - 1 911 000 n^23 + 48 425 n^24 - 780 n^25 + 6 n^26) / 104 396 352 425 164 800 000`

`In[ ]:= FullSimplify[%5]`

`Out[ ]:= ((-10 + n) (-9 + n) (-8 + n)^2 (-7 + n)^2 (-6 + n)^3 (-5 + n)^4 (-4 + n)^3 (-3 + n)^2 (-2 + n)^2  
(-1 + n) n (6369 + (-10 + n) n (395 + 6 (-10 + n) n))) / 104 396 352 425 164 800 000`

In[\*]:= %6 / %3

$$\text{Out[*]} = \frac{1}{2\,615\,348\,736\,000} (-8+n) (-7+n) (-6+n)^2 (-5+n)^3 (-4+n)^2 (-3+n) (-2+n) (6369 + (-10+n) n (395 + 6 (-10+n) n))$$

In[\*]:= Expand[(-8+n) (-7+n) (-6+n)^2 (-5+n)^3 (-4+n)^2 (-3+n) (-2+n) (6369 + (-10+n) n (395 + 6 (-10+n) n))]

$$\text{Out[*]} = -154\,078\,848\,000 + 486\,074\,908\,800 n - 707\,402\,381\,760 n^2 + 631\,255\,103\,784 n^3 - 386\,929\,514\,500 n^4 + 172\,820\,905\,130 n^5 - 58\,182\,645\,455 n^6 + 15\,052\,116\,013 n^7 - 3\,020\,035\,425 n^8 + 470\,350\,815 n^9 - 56\,440\,835 n^{10} + 5\,127\,697 n^{11} - 341\,575 n^{12} + 15\,755 n^{13} - 450 n^{14} + 6 n^{15}$$

In[\*]:= **(-154078848000\*f(x)+486074908800\*x\*D[f(x),x]-707402381760\*x\*D[x\*D[f(x),x],x])/2615348736000**

**(-154078848000 \* f[x] + 486074908800 \* x \* D[f[x], x] - 707402381760 \* x \* D[x \* D[f[x], x], x]) / 2615348736000**

$$\text{Out[*]} = \frac{1}{2\,615\,348\,736\,000} \left( -\frac{154\,078\,848\,000 x^{13}}{(1-x)^{14}} + 486\,074\,908\,800 x \left( \frac{13 x^{12}}{(1-x)^{14}} + \frac{14 x^{13}}{(1-x)^{15}} \right) - 707\,402\,381\,760 x \left( \frac{13 x^{12}}{(1-x)^{14}} + \frac{14 x^{13}}{(1-x)^{15}} + x \left( \frac{156 x^{11}}{(1-x)^{14}} + \frac{364 x^{12}}{(1-x)^{15}} + \frac{210 x^{13}}{(1-x)^{16}} \right) \right) \right)$$

In[\*]:= **(631255103784\*x\*D[x\*D[x\*D[f(x),x],x],x]-386929514500\*x\*D[x\*D[x\*D[x\*D[f(x),x],x],x])/2615348736000**

**(631255103784 \* x \* D[x \* D[x \* D[f[x], x], x], x] - 386929514500 \* x \* D[x \* D[x \* D[x \* D[f[x], x], x], x]) / 2615348736000**

$$\text{Out[*]} = \frac{1}{2\,615\,348\,736\,000} \left( 631\,255\,103\,784 x \left( \frac{13 x^{12}}{(1-x)^{14}} + \frac{14 x^{13}}{(1-x)^{15}} + x \left( \frac{156 x^{11}}{(1-x)^{14}} + \frac{364 x^{12}}{(1-x)^{15}} + \frac{210 x^{13}}{(1-x)^{16}} \right) \right) + x \left( \frac{312 x^{11}}{(1-x)^{14}} + \frac{728 x^{12}}{(1-x)^{15}} + \frac{420 x^{13}}{(1-x)^{16}} + x \left( \frac{1716 x^{10}}{(1-x)^{14}} + \frac{6552 x^{11}}{(1-x)^{15}} + \frac{8190 x^{12}}{(1-x)^{16}} + \frac{3360 x^{13}}{(1-x)^{17}} \right) \right) \right) - 386\,929\,514\,500 x \left( \frac{13 x^{12}}{(1-x)^{14}} + \frac{14 x^{13}}{(1-x)^{15}} + x \left( \frac{156 x^{11}}{(1-x)^{14}} + \frac{364 x^{12}}{(1-x)^{15}} + \frac{210 x^{13}}{(1-x)^{16}} \right) + x \left( \frac{312 x^{11}}{(1-x)^{14}} + \frac{728 x^{12}}{(1-x)^{15}} + \frac{420 x^{13}}{(1-x)^{16}} + x \left( \frac{1716 x^{10}}{(1-x)^{14}} + \frac{6552 x^{11}}{(1-x)^{15}} + \frac{8190 x^{12}}{(1-x)^{16}} + \frac{3360 x^{13}}{(1-x)^{17}} \right) \right) \right) + x \left( \frac{624 x^{11}}{(1-x)^{14}} + \frac{1456 x^{12}}{(1-x)^{15}} + \frac{840 x^{13}}{(1-x)^{16}} + 2 x \left( \frac{1716 x^{10}}{(1-x)^{14}} + \frac{6552 x^{11}}{(1-x)^{15}} + \frac{8190 x^{12}}{(1-x)^{16}} + \frac{3360 x^{13}}{(1-x)^{17}} \right) + x \left( \frac{5148 x^{10}}{(1-x)^{14}} + \frac{19\,656 x^{11}}{(1-x)^{15}} + \frac{24\,570 x^{12}}{(1-x)^{16}} + \frac{10\,080 x^{13}}{(1-x)^{17}} + x \left( \frac{17\,160 x^9}{(1-x)^{14}} + \frac{96\,096 x^{10}}{(1-x)^{15}} + \frac{196\,560 x^{11}}{(1-x)^{16}} + \frac{174\,720 x^{12}}{(1-x)^{17}} + \frac{57\,120 x^{13}}{(1-x)^{18}} \right) \right) \right) \right)$$

In[\*]:=



(172820905130\*x\*D[x\*D[x\*D[x\*D[x\*D[f(x),x],x],x],x]-58182645455\*  
x\*D[x\*D[x\*D[x\*D[x\*D[f(x),x],x],x],x])/2615348736000



(172 820 905 130 \* x \* D [ x \* D [ x \* D [ x \* D [ f [ x ] , x ] , x ] , x ] -  
58 182 645 455 \* x \* D [ x \* D [ x \* D [ x \* D [ f [ x ] , x ] , x ] , x ] ) / 2 615 348 736 000

$$\begin{aligned} \text{Out[*]} = & \frac{1}{2\,615\,348\,736\,000} \left( 172\,820\,905\,130 \, x \left( \frac{13 \, x^{12}}{(1-x)^{14}} + \frac{14 \, x^{13}}{(1-x)^{15}} + x \left( \frac{156 \, x^{11}}{(1-x)^{14}} + \frac{364 \, x^{12}}{(1-x)^{15}} + \frac{210 \, x^{13}}{(1-x)^{16}} \right) + \right. \right. \\ & x \left( \frac{312 \, x^{11}}{(1-x)^{14}} + \frac{728 \, x^{12}}{(1-x)^{15}} + \frac{420 \, x^{13}}{(1-x)^{16}} + x \left( \frac{1716 \, x^{10}}{(1-x)^{14}} + \frac{6552 \, x^{11}}{(1-x)^{15}} + \frac{8190 \, x^{12}}{(1-x)^{16}} + \frac{3360 \, x^{13}}{(1-x)^{17}} \right) \right) + \\ & x \left( \frac{624 \, x^{11}}{(1-x)^{14}} + \frac{1456 \, x^{12}}{(1-x)^{15}} + \frac{840 \, x^{13}}{(1-x)^{16}} + 2 \, x \left( \frac{1716 \, x^{10}}{(1-x)^{14}} + \frac{6552 \, x^{11}}{(1-x)^{15}} + \frac{8190 \, x^{12}}{(1-x)^{16}} + \frac{3360 \, x^{13}}{(1-x)^{17}} \right) + \right. \\ & x \left( \frac{5148 \, x^{10}}{(1-x)^{14}} + \frac{19\,656 \, x^{11}}{(1-x)^{15}} + \frac{24\,570 \, x^{12}}{(1-x)^{16}} + \frac{10\,080 \, x^{13}}{(1-x)^{17}} + \right. \\ & x \left( \frac{17\,160 \, x^9}{(1-x)^{14}} + \frac{96\,096 \, x^{10}}{(1-x)^{15}} + \frac{196\,560 \, x^{11}}{(1-x)^{16}} + \frac{174\,720 \, x^{12}}{(1-x)^{17}} + \frac{57\,120 \, x^{13}}{(1-x)^{18}} \right) \left. \right) \left. \right) + \\ & x \left( \frac{1248 \, x^{11}}{(1-x)^{14}} + \frac{2912 \, x^{12}}{(1-x)^{15}} + \frac{1680 \, x^{13}}{(1-x)^{16}} + 4 \, x \left( \frac{1716 \, x^{10}}{(1-x)^{14}} + \frac{6552 \, x^{11}}{(1-x)^{15}} + \frac{8190 \, x^{12}}{(1-x)^{16}} + \frac{3360 \, x^{13}}{(1-x)^{17}} \right) + \right. \\ & 2 \, x \left( \frac{5148 \, x^{10}}{(1-x)^{14}} + \frac{19\,656 \, x^{11}}{(1-x)^{15}} + \frac{24\,570 \, x^{12}}{(1-x)^{16}} + \frac{10\,080 \, x^{13}}{(1-x)^{17}} + \right. \\ & x \left( \frac{17\,160 \, x^9}{(1-x)^{14}} + \frac{96\,096 \, x^{10}}{(1-x)^{15}} + \frac{196\,560 \, x^{11}}{(1-x)^{16}} + \frac{174\,720 \, x^{12}}{(1-x)^{17}} + \frac{57\,120 \, x^{13}}{(1-x)^{18}} \right) \left. \right) + \\ & x \left( \frac{12\,012 \, x^{10}}{(1-x)^{14}} + \frac{45\,864 \, x^{11}}{(1-x)^{15}} + \frac{57\,330 \, x^{12}}{(1-x)^{16}} + \frac{23\,520 \, x^{13}}{(1-x)^{17}} + \right. \\ & 3 \, x \left( \frac{17\,160 \, x^9}{(1-x)^{14}} + \frac{96\,096 \, x^{10}}{(1-x)^{15}} + \frac{196\,560 \, x^{11}}{(1-x)^{16}} + \frac{174\,720 \, x^{12}}{(1-x)^{17}} + \frac{57\,120 \, x^{13}}{(1-x)^{18}} \right) + \\ & 2 \left( \frac{1716 \, x^{10}}{(1-x)^{14}} + \frac{6552 \, x^{11}}{(1-x)^{15}} + \frac{8190 \, x^{12}}{(1-x)^{16}} + \frac{3360 \, x^{13}}{(1-x)^{17}} \right) + \\ & x \left( \frac{68\,640 \, x^9}{(1-x)^{14}} + \frac{384\,384 \, x^{10}}{(1-x)^{15}} + \frac{786\,240 \, x^{11}}{(1-x)^{16}} + \frac{698\,880 \, x^{12}}{(1-x)^{17}} + \frac{228\,480 \, x^{13}}{(1-x)^{18}} + x \left( \frac{154\,440 \, x^8}{(1-x)^{14}} + \right. \right. \\ & \left. \left. \frac{1\,201\,200 \, x^9}{(1-x)^{15}} + \frac{3\,603\,600 \, x^{10}}{(1-x)^{16}} + \frac{5\,241\,600 \, x^{11}}{(1-x)^{17}} + \frac{3\,712\,800 \, x^{12}}{(1-x)^{18}} + \frac{1\,028\,160 \, x^{13}}{(1-x)^{19}} \right) \right) \left. \right) \left. \right) - \\ & 58\,182\,645\,455 \, x \left( \frac{13 \, x^{12}}{(1-x)^{14}} + \frac{14 \, x^{13}}{(1-x)^{15}} + x \left( \frac{156 \, x^{11}}{(1-x)^{14}} + \frac{364 \, x^{12}}{(1-x)^{15}} + \frac{210 \, x^{13}}{(1-x)^{16}} \right) + \right. \\ & x \left( \frac{312 \, x^{11}}{(1-x)^{14}} + \frac{728 \, x^{12}}{(1-x)^{15}} + \frac{420 \, x^{13}}{(1-x)^{16}} + x \left( \frac{1716 \, x^{10}}{(1-x)^{14}} + \frac{6552 \, x^{11}}{(1-x)^{15}} + \frac{8190 \, x^{12}}{(1-x)^{16}} + \frac{3360 \, x^{13}}{(1-x)^{17}} \right) \right) \left. \right) + \end{aligned}$$

$$\begin{aligned}
& \times \left( \frac{624 x^{11}}{(1-x)^{14}} + \frac{1456 x^{12}}{(1-x)^{15}} + \frac{840 x^{13}}{(1-x)^{16}} + 2 \times \left( \frac{1716 x^{10}}{(1-x)^{14}} + \frac{6552 x^{11}}{(1-x)^{15}} + \frac{8190 x^{12}}{(1-x)^{16}} + \frac{3360 x^{13}}{(1-x)^{17}} \right) + \right. \\
& \quad \times \left( \frac{5148 x^{10}}{(1-x)^{14}} + \frac{19656 x^{11}}{(1-x)^{15}} + \frac{24570 x^{12}}{(1-x)^{16}} + \frac{10080 x^{13}}{(1-x)^{17}} + \right. \\
& \quad \quad \times \left. \left( \frac{17160 x^9}{(1-x)^{14}} + \frac{96096 x^{10}}{(1-x)^{15}} + \frac{196560 x^{11}}{(1-x)^{16}} + \frac{174720 x^{12}}{(1-x)^{17}} + \frac{57120 x^{13}}{(1-x)^{18}} \right) \right) \Bigg) + \\
& \times \left( \frac{1248 x^{11}}{(1-x)^{14}} + \frac{2912 x^{12}}{(1-x)^{15}} + \frac{1680 x^{13}}{(1-x)^{16}} + 4 \times \left( \frac{1716 x^{10}}{(1-x)^{14}} + \frac{6552 x^{11}}{(1-x)^{15}} + \frac{8190 x^{12}}{(1-x)^{16}} + \frac{3360 x^{13}}{(1-x)^{17}} \right) + \right. \\
& \quad 2 \times \left( \frac{5148 x^{10}}{(1-x)^{14}} + \frac{19656 x^{11}}{(1-x)^{15}} + \frac{24570 x^{12}}{(1-x)^{16}} + \frac{10080 x^{13}}{(1-x)^{17}} + \right. \\
& \quad \quad \times \left. \left( \frac{17160 x^9}{(1-x)^{14}} + \frac{96096 x^{10}}{(1-x)^{15}} + \frac{196560 x^{11}}{(1-x)^{16}} + \frac{174720 x^{12}}{(1-x)^{17}} + \frac{57120 x^{13}}{(1-x)^{18}} \right) \right) \Bigg) + \\
& \quad \times \left( \frac{12012 x^{10}}{(1-x)^{14}} + \frac{45864 x^{11}}{(1-x)^{15}} + \frac{57330 x^{12}}{(1-x)^{16}} + \frac{23520 x^{13}}{(1-x)^{17}} + \right. \\
& \quad \quad 3 \times \left( \frac{17160 x^9}{(1-x)^{14}} + \frac{96096 x^{10}}{(1-x)^{15}} + \frac{196560 x^{11}}{(1-x)^{16}} + \frac{174720 x^{12}}{(1-x)^{17}} + \frac{57120 x^{13}}{(1-x)^{18}} \right) + \\
& \quad \quad 2 \left( \frac{1716 x^{10}}{(1-x)^{14}} + \frac{6552 x^{11}}{(1-x)^{15}} + \frac{8190 x^{12}}{(1-x)^{16}} + \frac{3360 x^{13}}{(1-x)^{17}} \right) + \\
& \quad \quad \times \left( \frac{68640 x^9}{(1-x)^{14}} + \frac{384384 x^{10}}{(1-x)^{15}} + \frac{786240 x^{11}}{(1-x)^{16}} + \frac{698880 x^{12}}{(1-x)^{17}} + \frac{228480 x^{13}}{(1-x)^{18}} + x \left( \frac{154440 x^8}{(1-x)^{14}} + \right. \right. \\
& \quad \quad \quad \left. \frac{1201200 x^9}{(1-x)^{15}} + \frac{3603600 x^{10}}{(1-x)^{16}} + \frac{5241600 x^{11}}{(1-x)^{17}} + \frac{3712800 x^{12}}{(1-x)^{18}} + \frac{1028160 x^{13}}{(1-x)^{19}} \right) \Bigg) \Bigg) + \\
& \times \left( \frac{2496 x^{11}}{(1-x)^{14}} + \frac{5824 x^{12}}{(1-x)^{15}} + \frac{3360 x^{13}}{(1-x)^{16}} + 8 \times \left( \frac{1716 x^{10}}{(1-x)^{14}} + \frac{6552 x^{11}}{(1-x)^{15}} + \frac{8190 x^{12}}{(1-x)^{16}} + \frac{3360 x^{13}}{(1-x)^{17}} \right) + \right. \\
& \quad 4 \times \left( \frac{5148 x^{10}}{(1-x)^{14}} + \frac{19656 x^{11}}{(1-x)^{15}} + \frac{24570 x^{12}}{(1-x)^{16}} + \frac{10080 x^{13}}{(1-x)^{17}} + \right. \\
& \quad \quad \times \left. \left( \frac{17160 x^9}{(1-x)^{14}} + \frac{96096 x^{10}}{(1-x)^{15}} + \frac{196560 x^{11}}{(1-x)^{16}} + \frac{174720 x^{12}}{(1-x)^{17}} + \frac{57120 x^{13}}{(1-x)^{18}} \right) \right) \Bigg) + \\
& \quad 2 \times \left( \frac{12012 x^{10}}{(1-x)^{14}} + \frac{45864 x^{11}}{(1-x)^{15}} + \frac{57330 x^{12}}{(1-x)^{16}} + \frac{23520 x^{13}}{(1-x)^{17}} + \right. \\
& \quad \quad 3 \times \left( \frac{17160 x^9}{(1-x)^{14}} + \frac{96096 x^{10}}{(1-x)^{15}} + \frac{196560 x^{11}}{(1-x)^{16}} + \frac{174720 x^{12}}{(1-x)^{17}} + \frac{57120 x^{13}}{(1-x)^{18}} \right) + \\
& \quad \quad 2 \left( \frac{1716 x^{10}}{(1-x)^{14}} + \frac{6552 x^{11}}{(1-x)^{15}} + \frac{8190 x^{12}}{(1-x)^{16}} + \frac{3360 x^{13}}{(1-x)^{17}} \right) + \\
& \quad \quad \times \left( \frac{68640 x^9}{(1-x)^{14}} + \frac{384384 x^{10}}{(1-x)^{15}} + \frac{786240 x^{11}}{(1-x)^{16}} + \frac{698880 x^{12}}{(1-x)^{17}} + \frac{228480 x^{13}}{(1-x)^{18}} + x \left( \frac{154440 x^8}{(1-x)^{14}} + \right. \right.
\end{aligned}$$

$$\begin{aligned} & \left. \left. \left. \left. \left. \frac{1201200x^9}{(1-x)^{15}} + \frac{3603600x^{10}}{(1-x)^{16}} + \frac{5241600x^{11}}{(1-x)^{17}} + \frac{3712800x^{12}}{(1-x)^{18}} + \frac{1028160x^{13}}{(1-x)^{19}} \right) \right) \right) \right) \right) + \\ & \times \left( \frac{25740x^{10}}{(1-x)^{14}} + \frac{98280x^{11}}{(1-x)^{15}} + \frac{122850x^{12}}{(1-x)^{16}} + \frac{50400x^{13}}{(1-x)^{17}} + 7 \times \left( \frac{17160x^9}{(1-x)^{14}} + \frac{96096x^{10}}{(1-x)^{15}} + \right. \right. \\ & \left. \left. \frac{196560x^{11}}{(1-x)^{16}} + \frac{174720x^{12}}{(1-x)^{17}} + \frac{57120x^{13}}{(1-x)^{18}} \right) + 6 \left( \frac{1716x^{10}}{(1-x)^{14}} + \frac{6552x^{11}}{(1-x)^{15}} + \frac{8190x^{12}}{(1-x)^{16}} + \right. \right. \\ & \left. \left. \frac{3360x^{13}}{(1-x)^{17}} \right) + 3 \times \left( \frac{68640x^9}{(1-x)^{14}} + \frac{384384x^{10}}{(1-x)^{15}} + \frac{786240x^{11}}{(1-x)^{16}} + \frac{698880x^{12}}{(1-x)^{17}} + \frac{228480x^{13}}{(1-x)^{18}} + \right. \right. \\ & \left. \left. \left( \frac{154440x^8}{(1-x)^{14}} + \frac{1201200x^9}{(1-x)^{15}} + \frac{3603600x^{10}}{(1-x)^{16}} + \frac{5241600x^{11}}{(1-x)^{17}} + \frac{3712800x^{12}}{(1-x)^{18}} + \right. \right. \right. \\ & \left. \left. \left. \frac{1028160x^{13}}{(1-x)^{19}} \right) \right) + 2 \left( \frac{5148x^{10}}{(1-x)^{14}} + \frac{19656x^{11}}{(1-x)^{15}} + \frac{24570x^{12}}{(1-x)^{16}} + \frac{10080x^{13}}{(1-x)^{17}} + \right. \right. \\ & \left. \left. \left( \frac{17160x^9}{(1-x)^{14}} + \frac{96096x^{10}}{(1-x)^{15}} + \frac{196560x^{11}}{(1-x)^{16}} + \frac{174720x^{12}}{(1-x)^{17}} + \frac{57120x^{13}}{(1-x)^{18}} \right) \right) \right) + \\ & \times \left( \frac{188760x^9}{(1-x)^{14}} + \frac{1057056x^{10}}{(1-x)^{15}} + \frac{2162160x^{11}}{(1-x)^{16}} + \frac{1921920x^{12}}{(1-x)^{17}} + \frac{628320x^{13}}{(1-x)^{18}} + 4 \right. \\ & \times \left( \frac{154440x^8}{(1-x)^{14}} + \frac{1201200x^9}{(1-x)^{15}} + \frac{3603600x^{10}}{(1-x)^{16}} + \frac{5241600x^{11}}{(1-x)^{17}} + \frac{3712800x^{12}}{(1-x)^{18}} + \right. \\ & \left. \left. \frac{1028160x^{13}}{(1-x)^{19}} \right) + 5 \left( \frac{17160x^9}{(1-x)^{14}} + \frac{96096x^{10}}{(1-x)^{15}} + \frac{196560x^{11}}{(1-x)^{16}} + \frac{174720x^{12}}{(1-x)^{17}} + \right. \right. \\ & \left. \left. \frac{57120x^{13}}{(1-x)^{18}} \right) + \times \left( \frac{772200x^8}{(1-x)^{14}} + \frac{6006000x^9}{(1-x)^{15}} + \frac{18018000x^{10}}{(1-x)^{16}} + \frac{26208000x^{11}}{(1-x)^{17}} + \right. \right. \\ & \left. \left. \frac{18564000x^{12}}{(1-x)^{18}} + \frac{5140800x^{13}}{(1-x)^{19}} + \times \left( \frac{1235520x^7}{(1-x)^{14}} + \frac{12972960x^8}{(1-x)^{15}} + \frac{54054000x^9}{(1-x)^{16}} + \right. \right. \right. \\ & \left. \left. \left. \frac{115315200x^{10}}{(1-x)^{17}} + \frac{133660800x^{11}}{(1-x)^{18}} + \frac{80196480x^{12}}{(1-x)^{19}} + \frac{19535040x^{13}}{(1-x)^{20}} \right) \right) \right) \right) \right) \right) \end{aligned}$$

$$\ln[\bullet] :=$$


(15052116013\*x\*D[x\*D[x\*D[x\*D[x\*D[x\*D[f(x),x],x],x],x],x],x])/2615348736000

$$\frac{(15052116013 \cdot x \cdot D[x \cdot D[x \cdot D[x \cdot D[x \cdot D[x \cdot D[f[x], x], x], x], x], x], x)]}{2615348736000}$$

$$Out[n]=\frac{1}{237\,758\,976\,000}\times 1\,368\,374\,183\times\left(\frac{13\,x^{12}}{(1-x)^{14}}+\frac{14\,x^{13}}{(1-x)^{15}}+x\left(\frac{156\,x^{11}}{(1-x)^{14}}+\frac{364\,x^{12}}{(1-x)^{15}}+\frac{210\,x^{13}}{(1-x)^{16}}\right)+\right.\\ \left.\times\left(\frac{312\,x^{11}}{(1-x)^{14}}+\frac{728\,x^{12}}{(1-x)^{15}}+\frac{420\,x^{13}}{(1-x)^{16}}+x\left(\frac{1716\,x^{10}}{(1-x)^{14}}+\frac{6552\,x^{11}}{(1-x)^{15}}+\frac{8190\,x^{12}}{(1-x)^{16}}+\frac{3360\,x^{13}}{(1-x)^{17}}\right)\right)\right)+$$

$$\begin{aligned}
& \times \left( \frac{624 x^{11}}{(1-x)^{14}} + \frac{1456 x^{12}}{(1-x)^{15}} + \frac{840 x^{13}}{(1-x)^{16}} + 2 \times \left( \frac{1716 x^{10}}{(1-x)^{14}} + \frac{6552 x^{11}}{(1-x)^{15}} + \frac{8190 x^{12}}{(1-x)^{16}} + \frac{3360 x^{13}}{(1-x)^{17}} \right) + \right. \\
& \quad \times \left( \frac{5148 x^{10}}{(1-x)^{14}} + \frac{19656 x^{11}}{(1-x)^{15}} + \frac{24570 x^{12}}{(1-x)^{16}} + \frac{10080 x^{13}}{(1-x)^{17}} + \right. \\
& \quad \quad \times \left( \frac{17160 x^9}{(1-x)^{14}} + \frac{96096 x^{10}}{(1-x)^{15}} + \frac{196560 x^{11}}{(1-x)^{16}} + \frac{174720 x^{12}}{(1-x)^{17}} + \frac{57120 x^{13}}{(1-x)^{18}} \right) \left. \right) + \\
& \times \left( \frac{1248 x^{11}}{(1-x)^{14}} + \frac{2912 x^{12}}{(1-x)^{15}} + \frac{1680 x^{13}}{(1-x)^{16}} + 4 \times \left( \frac{1716 x^{10}}{(1-x)^{14}} + \frac{6552 x^{11}}{(1-x)^{15}} + \frac{8190 x^{12}}{(1-x)^{16}} + \frac{3360 x^{13}}{(1-x)^{17}} \right) + \right. \\
& \quad 2 \times \left( \frac{5148 x^{10}}{(1-x)^{14}} + \frac{19656 x^{11}}{(1-x)^{15}} + \frac{24570 x^{12}}{(1-x)^{16}} + \frac{10080 x^{13}}{(1-x)^{17}} + \right. \\
& \quad \quad \times \left( \frac{17160 x^9}{(1-x)^{14}} + \frac{96096 x^{10}}{(1-x)^{15}} + \frac{196560 x^{11}}{(1-x)^{16}} + \frac{174720 x^{12}}{(1-x)^{17}} + \frac{57120 x^{13}}{(1-x)^{18}} \right) \left. \right) + \\
& \quad \times \left( \frac{12012 x^{10}}{(1-x)^{14}} + \frac{45864 x^{11}}{(1-x)^{15}} + \frac{57330 x^{12}}{(1-x)^{16}} + \frac{23520 x^{13}}{(1-x)^{17}} + 3 \times \left( \frac{17160 x^9}{(1-x)^{14}} + \frac{96096 x^{10}}{(1-x)^{15}} + \frac{196560 x^{11}}{(1-x)^{16}} + \right. \right. \\
& \quad \quad \frac{174720 x^{12}}{(1-x)^{17}} + \frac{57120 x^{13}}{(1-x)^{18}} \left. \right) + 2 \left( \frac{1716 x^{10}}{(1-x)^{14}} + \frac{6552 x^{11}}{(1-x)^{15}} + \frac{8190 x^{12}}{(1-x)^{16}} + \frac{3360 x^{13}}{(1-x)^{17}} \right) + \\
& \quad \times \left( \frac{68640 x^9}{(1-x)^{14}} + \frac{384384 x^{10}}{(1-x)^{15}} + \frac{786240 x^{11}}{(1-x)^{16}} + \frac{698880 x^{12}}{(1-x)^{17}} + \frac{228480 x^{13}}{(1-x)^{18}} + x \left( \frac{154440 x^8}{(1-x)^{14}} + \right. \right. \\
& \quad \quad \frac{1201200 x^9}{(1-x)^{15}} + \frac{3603600 x^{10}}{(1-x)^{16}} + \frac{5241600 x^{11}}{(1-x)^{17}} + \frac{3712800 x^{12}}{(1-x)^{18}} + \frac{1028160 x^{13}}{(1-x)^{19}} \left. \right) \left. \right) + \\
& \times \left( \frac{2496 x^{11}}{(1-x)^{14}} + \frac{5824 x^{12}}{(1-x)^{15}} + \frac{3360 x^{13}}{(1-x)^{16}} + 8 \times \left( \frac{1716 x^{10}}{(1-x)^{14}} + \frac{6552 x^{11}}{(1-x)^{15}} + \frac{8190 x^{12}}{(1-x)^{16}} + \frac{3360 x^{13}}{(1-x)^{17}} \right) + \right. \\
& \quad 4 \times \left( \frac{5148 x^{10}}{(1-x)^{14}} + \frac{19656 x^{11}}{(1-x)^{15}} + \frac{24570 x^{12}}{(1-x)^{16}} + \frac{10080 x^{13}}{(1-x)^{17}} + \right. \\
& \quad \quad \times \left( \frac{17160 x^9}{(1-x)^{14}} + \frac{96096 x^{10}}{(1-x)^{15}} + \frac{196560 x^{11}}{(1-x)^{16}} + \frac{174720 x^{12}}{(1-x)^{17}} + \frac{57120 x^{13}}{(1-x)^{18}} \right) \left. \right) + 2 \times \\
& \quad \left( \frac{12012 x^{10}}{(1-x)^{14}} + \frac{45864 x^{11}}{(1-x)^{15}} + \frac{57330 x^{12}}{(1-x)^{16}} + \frac{23520 x^{13}}{(1-x)^{17}} + 3 \times \left( \frac{17160 x^9}{(1-x)^{14}} + \frac{96096 x^{10}}{(1-x)^{15}} + \frac{196560 x^{11}}{(1-x)^{16}} + \right. \right. \\
& \quad \quad \frac{174720 x^{12}}{(1-x)^{17}} + \frac{57120 x^{13}}{(1-x)^{18}} \left. \right) + 2 \left( \frac{1716 x^{10}}{(1-x)^{14}} + \frac{6552 x^{11}}{(1-x)^{15}} + \frac{8190 x^{12}}{(1-x)^{16}} + \frac{3360 x^{13}}{(1-x)^{17}} \right) + \\
& \quad \times \left( \frac{68640 x^9}{(1-x)^{14}} + \frac{384384 x^{10}}{(1-x)^{15}} + \frac{786240 x^{11}}{(1-x)^{16}} + \frac{698880 x^{12}}{(1-x)^{17}} + \frac{228480 x^{13}}{(1-x)^{18}} + x \left( \frac{154440 x^8}{(1-x)^{14}} + \right. \right. \\
& \quad \quad \frac{1201200 x^9}{(1-x)^{15}} + \frac{3603600 x^{10}}{(1-x)^{16}} + \frac{5241600 x^{11}}{(1-x)^{17}} + \frac{3712800 x^{12}}{(1-x)^{18}} + \frac{1028160 x^{13}}{(1-x)^{19}} \left. \right) \left. \right) + x \\
& \quad \left( \frac{25740 x^{10}}{(1-x)^{14}} + \frac{98280 x^{11}}{(1-x)^{15}} + \frac{122850 x^{12}}{(1-x)^{16}} + \frac{50400 x^{13}}{(1-x)^{17}} + 7 \times \left( \frac{17160 x^9}{(1-x)^{14}} + \frac{96096 x^{10}}{(1-x)^{15}} + \frac{196560 x^{11}}{(1-x)^{16}} + \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left( \frac{174\,720\,x^{12}}{(1-x)^{17}} + \frac{57\,120\,x^{13}}{(1-x)^{18}} \right) + 6 \left( \frac{1716\,x^{10}}{(1-x)^{14}} + \frac{6552\,x^{11}}{(1-x)^{15}} + \frac{8190\,x^{12}}{(1-x)^{16}} + \frac{3360\,x^{13}}{(1-x)^{17}} \right) + \\
& 3 \times \left( \frac{68\,640\,x^9}{(1-x)^{14}} + \frac{384\,384\,x^{10}}{(1-x)^{15}} + \frac{786\,240\,x^{11}}{(1-x)^{16}} + \frac{698\,880\,x^{12}}{(1-x)^{17}} + \frac{228\,480\,x^{13}}{(1-x)^{18}} + x \left( \frac{154\,440\,x^8}{(1-x)^{14}} + \right. \right. \\
& \quad \left. \left. \frac{1\,201\,200\,x^9}{(1-x)^{15}} + \frac{3\,603\,600\,x^{10}}{(1-x)^{16}} + \frac{5\,241\,600\,x^{11}}{(1-x)^{17}} + \frac{3\,712\,800\,x^{12}}{(1-x)^{18}} + \frac{1\,028\,160\,x^{13}}{(1-x)^{19}} \right) \right) + \\
& 2 \left( \frac{5148\,x^{10}}{(1-x)^{14}} + \frac{19\,656\,x^{11}}{(1-x)^{15}} + \frac{24\,570\,x^{12}}{(1-x)^{16}} + \frac{10\,080\,x^{13}}{(1-x)^{17}} + x \left( \frac{17\,160\,x^9}{(1-x)^{14}} + \frac{96\,096\,x^{10}}{(1-x)^{15}} + \right. \right. \\
& \quad \left. \left. \frac{196\,560\,x^{11}}{(1-x)^{16}} + \frac{174\,720\,x^{12}}{(1-x)^{17}} + \frac{57\,120\,x^{13}}{(1-x)^{18}} \right) \right) + \\
& x \left( \frac{188\,760\,x^9}{(1-x)^{14}} + \frac{1\,057\,056\,x^{10}}{(1-x)^{15}} + \frac{2\,162\,160\,x^{11}}{(1-x)^{16}} + \frac{1\,921\,920\,x^{12}}{(1-x)^{17}} + \frac{628\,320\,x^{13}}{(1-x)^{18}} + \right. \\
& \quad 4 \times \left( \frac{154\,440\,x^8}{(1-x)^{14}} + \frac{1\,201\,200\,x^9}{(1-x)^{15}} + \frac{3\,603\,600\,x^{10}}{(1-x)^{16}} + \frac{5\,241\,600\,x^{11}}{(1-x)^{17}} + \frac{3\,712\,800\,x^{12}}{(1-x)^{18}} + \right. \\
& \quad \left. \frac{1\,028\,160\,x^{13}}{(1-x)^{19}} \right) + 5 \left( \frac{17\,160\,x^9}{(1-x)^{14}} + \frac{96\,096\,x^{10}}{(1-x)^{15}} + \frac{196\,560\,x^{11}}{(1-x)^{16}} + \frac{174\,720\,x^{12}}{(1-x)^{17}} + \frac{57\,120\,x^{13}}{(1-x)^{18}} \right) + \\
& \quad x \left( \frac{772\,200\,x^8}{(1-x)^{14}} + \frac{6\,006\,000\,x^9}{(1-x)^{15}} + \frac{18\,018\,000\,x^{10}}{(1-x)^{16}} + \frac{26\,208\,000\,x^{11}}{(1-x)^{17}} + \frac{18\,564\,000\,x^{12}}{(1-x)^{18}} + \right. \\
& \quad \left. \frac{5\,140\,800\,x^{13}}{(1-x)^{19}} + x \left( \frac{1\,235\,520\,x^7}{(1-x)^{14}} + \frac{12\,972\,960\,x^8}{(1-x)^{15}} + \frac{54\,054\,000\,x^9}{(1-x)^{16}} + \right. \right. \\
& \quad \left. \left. \frac{115\,315\,200\,x^{10}}{(1-x)^{17}} + \frac{133\,660\,800\,x^{11}}{(1-x)^{18}} + \frac{80\,196\,480\,x^{12}}{(1-x)^{19}} + \frac{19\,535\,040\,x^{13}}{(1-x)^{20}} \right) \right) \right) + \\
& x \left( \frac{4992\,x^{11}}{(1-x)^{14}} + \frac{11\,648\,x^{12}}{(1-x)^{15}} + \frac{6720\,x^{13}}{(1-x)^{16}} + 16 \times \left( \frac{1716\,x^{10}}{(1-x)^{14}} + \frac{6552\,x^{11}}{(1-x)^{15}} + \frac{8190\,x^{12}}{(1-x)^{16}} + \frac{3360\,x^{13}}{(1-x)^{17}} \right) + \right. \\
& \quad 8 \times \left( \frac{5148\,x^{10}}{(1-x)^{14}} + \frac{19\,656\,x^{11}}{(1-x)^{15}} + \frac{24\,570\,x^{12}}{(1-x)^{16}} + \frac{10\,080\,x^{13}}{(1-x)^{17}} + \right. \\
& \quad \left. x \left( \frac{17\,160\,x^9}{(1-x)^{14}} + \frac{96\,096\,x^{10}}{(1-x)^{15}} + \frac{196\,560\,x^{11}}{(1-x)^{16}} + \frac{174\,720\,x^{12}}{(1-x)^{17}} + \frac{57\,120\,x^{13}}{(1-x)^{18}} \right) \right) + \\
& \quad 4 \times \left( \frac{12\,012\,x^{10}}{(1-x)^{14}} + \frac{45\,864\,x^{11}}{(1-x)^{15}} + \frac{57\,330\,x^{12}}{(1-x)^{16}} + \frac{23\,520\,x^{13}}{(1-x)^{17}} + \right. \\
& \quad 3 \times \left( \frac{17\,160\,x^9}{(1-x)^{14}} + \frac{96\,096\,x^{10}}{(1-x)^{15}} + \frac{196\,560\,x^{11}}{(1-x)^{16}} + \frac{174\,720\,x^{12}}{(1-x)^{17}} + \frac{57\,120\,x^{13}}{(1-x)^{18}} \right) + \\
& \quad 2 \left( \frac{1716\,x^{10}}{(1-x)^{14}} + \frac{6552\,x^{11}}{(1-x)^{15}} + \frac{8190\,x^{12}}{(1-x)^{16}} + \frac{3360\,x^{13}}{(1-x)^{17}} \right) + \\
& \quad x \left( \frac{68\,640\,x^9}{(1-x)^{14}} + \frac{384\,384\,x^{10}}{(1-x)^{15}} + \frac{786\,240\,x^{11}}{(1-x)^{16}} + \frac{698\,880\,x^{12}}{(1-x)^{17}} + \frac{228\,480\,x^{13}}{(1-x)^{18}} + x \left( \frac{154\,440\,x^8}{(1-x)^{14}} + \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left( \frac{1\,201\,200\,x^9}{(1-x)^{15}} + \frac{3\,603\,600\,x^{10}}{(1-x)^{16}} + \frac{5\,241\,600\,x^{11}}{(1-x)^{17}} + \frac{3\,712\,800\,x^{12}}{(1-x)^{18}} + \frac{1\,028\,160\,x^{13}}{(1-x)^{19}} \right) \Bigg) \Bigg) + \\
& 2 \times \left( \frac{25\,740\,x^{10}}{(1-x)^{14}} + \frac{98\,280\,x^{11}}{(1-x)^{15}} + \frac{122\,850\,x^{12}}{(1-x)^{16}} + \frac{50\,400\,x^{13}}{(1-x)^{17}} + \right. \\
& 7 \times \left( \frac{17\,160\,x^9}{(1-x)^{14}} + \frac{96\,096\,x^{10}}{(1-x)^{15}} + \frac{196\,560\,x^{11}}{(1-x)^{16}} + \frac{174\,720\,x^{12}}{(1-x)^{17}} + \frac{57\,120\,x^{13}}{(1-x)^{18}} \right) + \\
& 6 \left( \frac{1716\,x^{10}}{(1-x)^{14}} + \frac{6552\,x^{11}}{(1-x)^{15}} + \frac{8190\,x^{12}}{(1-x)^{16}} + \frac{3360\,x^{13}}{(1-x)^{17}} \right) + \\
& 3 \times \left( \frac{68\,640\,x^9}{(1-x)^{14}} + \frac{384\,384\,x^{10}}{(1-x)^{15}} + \frac{786\,240\,x^{11}}{(1-x)^{16}} + \frac{698\,880\,x^{12}}{(1-x)^{17}} + \frac{228\,480\,x^{13}}{(1-x)^{18}} + x \left( \frac{154\,440\,x^8}{(1-x)^{14}} + \right. \right. \\
& \left. \left. \frac{1\,201\,200\,x^9}{(1-x)^{15}} + \frac{3\,603\,600\,x^{10}}{(1-x)^{16}} + \frac{5\,241\,600\,x^{11}}{(1-x)^{17}} + \frac{3\,712\,800\,x^{12}}{(1-x)^{18}} + \frac{1\,028\,160\,x^{13}}{(1-x)^{19}} \right) \right) \Bigg) + \\
& 2 \left( \frac{5148\,x^{10}}{(1-x)^{14}} + \frac{19\,656\,x^{11}}{(1-x)^{15}} + \frac{24\,570\,x^{12}}{(1-x)^{16}} + \frac{10\,080\,x^{13}}{(1-x)^{17}} + x \left( \frac{17\,160\,x^9}{(1-x)^{14}} + \frac{96\,096\,x^{10}}{(1-x)^{15}} + \right. \right. \\
& \left. \left. \frac{196\,560\,x^{11}}{(1-x)^{16}} + \frac{174\,720\,x^{12}}{(1-x)^{17}} + \frac{57\,120\,x^{13}}{(1-x)^{18}} \right) \right) \Bigg) + \\
& x \left( \frac{188\,760\,x^9}{(1-x)^{14}} + \frac{1\,057\,056\,x^{10}}{(1-x)^{15}} + \frac{2\,162\,160\,x^{11}}{(1-x)^{16}} + \frac{1\,921\,920\,x^{12}}{(1-x)^{17}} + \frac{628\,320\,x^{13}}{(1-x)^{18}} + \right. \\
& 4 \times \left( \frac{154\,440\,x^8}{(1-x)^{14}} + \frac{1\,201\,200\,x^9}{(1-x)^{15}} + \frac{3\,603\,600\,x^{10}}{(1-x)^{16}} + \frac{5\,241\,600\,x^{11}}{(1-x)^{17}} + \frac{3\,712\,800\,x^{12}}{(1-x)^{18}} + \right. \\
& \left. \frac{1\,028\,160\,x^{13}}{(1-x)^{19}} \right) + 5 \left( \frac{17\,160\,x^9}{(1-x)^{14}} + \frac{96\,096\,x^{10}}{(1-x)^{15}} + \frac{196\,560\,x^{11}}{(1-x)^{16}} + \frac{174\,720\,x^{12}}{(1-x)^{17}} + \frac{57\,120\,x^{13}}{(1-x)^{18}} \right) + \\
& x \left( \frac{772\,200\,x^8}{(1-x)^{14}} + \frac{6\,006\,000\,x^9}{(1-x)^{15}} + \frac{18\,018\,000\,x^{10}}{(1-x)^{16}} + \frac{26\,208\,000\,x^{11}}{(1-x)^{17}} + \frac{18\,564\,000\,x^{12}}{(1-x)^{18}} + \right. \\
& \left. \frac{5\,140\,800\,x^{13}}{(1-x)^{19}} + x \left( \frac{1\,235\,520\,x^7}{(1-x)^{14}} + \frac{12\,972\,960\,x^8}{(1-x)^{15}} + \frac{54\,054\,000\,x^9}{(1-x)^{16}} + \right. \right. \\
& \left. \left. \frac{115\,315\,200\,x^{10}}{(1-x)^{17}} + \frac{133\,660\,800\,x^{11}}{(1-x)^{18}} + \frac{80\,196\,480\,x^{12}}{(1-x)^{19}} + \frac{19\,535\,040\,x^{13}}{(1-x)^{20}} \right) \right) \Bigg) \Bigg) + \\
& x \left( \frac{53\,196\,x^{10}}{(1-x)^{14}} + \frac{203\,112\,x^{11}}{(1-x)^{15}} + \frac{253\,890\,x^{12}}{(1-x)^{16}} + \frac{104\,160\,x^{13}}{(1-x)^{17}} + 15 \times \left( \frac{17\,160\,x^9}{(1-x)^{14}} + \right. \right. \\
& \left. \left. \frac{96\,096\,x^{10}}{(1-x)^{15}} + \frac{196\,560\,x^{11}}{(1-x)^{16}} + \frac{174\,720\,x^{12}}{(1-x)^{17}} + \frac{57\,120\,x^{13}}{(1-x)^{18}} \right) + \right. \\
& 14 \left( \frac{1716\,x^{10}}{(1-x)^{14}} + \frac{6552\,x^{11}}{(1-x)^{15}} + \frac{8190\,x^{12}}{(1-x)^{16}} + \frac{3360\,x^{13}}{(1-x)^{17}} \right) + \\
& 7 \times \left( \frac{68\,640\,x^9}{(1-x)^{14}} + \frac{384\,384\,x^{10}}{(1-x)^{15}} + \frac{786\,240\,x^{11}}{(1-x)^{16}} + \frac{698\,880\,x^{12}}{(1-x)^{17}} + \frac{228\,480\,x^{13}}{(1-x)^{18}} + x \left( \frac{154\,440\,x^8}{(1-x)^{14}} + \right. \right.
\end{aligned}$$



$$\begin{aligned}
& \left( \frac{1\,201\,200\,x^9}{(1-x)^{15}} + \frac{3\,603\,600\,x^{10}}{(1-x)^{16}} + \frac{5\,241\,600\,x^{11}}{(1-x)^{17}} + \frac{3\,712\,800\,x^{12}}{(1-x)^{18}} + \frac{1\,028\,160\,x^{13}}{(1-x)^{19}} \right) + \\
& 6 \left( \frac{5148\,x^{10}}{(1-x)^{14}} + \frac{19\,656\,x^{11}}{(1-x)^{15}} + \frac{24\,570\,x^{12}}{(1-x)^{16}} + \frac{10\,080\,x^{13}}{(1-x)^{17}} + x \left( \frac{17\,160\,x^9}{(1-x)^{14}} + \frac{96\,096\,x^{10}}{(1-x)^{15}} + \right. \right. \\
& \quad \left. \left. \frac{196\,560\,x^{11}}{(1-x)^{16}} + \frac{174\,720\,x^{12}}{(1-x)^{17}} + \frac{57\,120\,x^{13}}{(1-x)^{18}} \right) \right) + \\
& 3 \times \left( \frac{188\,760\,x^9}{(1-x)^{14}} + \frac{1\,057\,056\,x^{10}}{(1-x)^{15}} + \frac{2\,162\,160\,x^{11}}{(1-x)^{16}} + \frac{1\,921\,920\,x^{12}}{(1-x)^{17}} + \frac{628\,320\,x^{13}}{(1-x)^{18}} + \right. \\
& 4 \times \left( \frac{154\,440\,x^8}{(1-x)^{14}} + \frac{1\,201\,200\,x^9}{(1-x)^{15}} + \frac{3\,603\,600\,x^{10}}{(1-x)^{16}} + \frac{5\,241\,600\,x^{11}}{(1-x)^{17}} + \frac{3\,712\,800\,x^{12}}{(1-x)^{18}} + \right. \\
& \quad \left. \frac{1\,028\,160\,x^{13}}{(1-x)^{19}} \right) + 5 \left( \frac{17\,160\,x^9}{(1-x)^{14}} + \frac{96\,096\,x^{10}}{(1-x)^{15}} + \frac{196\,560\,x^{11}}{(1-x)^{16}} + \frac{174\,720\,x^{12}}{(1-x)^{17}} + \frac{57\,120\,x^{13}}{(1-x)^{18}} \right) + \\
& x \left( \frac{772\,200\,x^8}{(1-x)^{14}} + \frac{6\,006\,000\,x^9}{(1-x)^{15}} + \frac{18\,018\,000\,x^{10}}{(1-x)^{16}} + \frac{26\,208\,000\,x^{11}}{(1-x)^{17}} + \frac{18\,564\,000\,x^{12}}{(1-x)^{18}} + \right. \\
& \quad \frac{5\,140\,800\,x^{13}}{(1-x)^{19}} + x \left( \frac{1\,235\,520\,x^7}{(1-x)^{14}} + \frac{12\,972\,960\,x^8}{(1-x)^{15}} + \frac{54\,054\,000\,x^9}{(1-x)^{16}} + \frac{115\,315\,200\,x^{10}}{(1-x)^{17}} + \right. \\
& \quad \left. \frac{133\,660\,800\,x^{11}}{(1-x)^{18}} + \frac{80\,196\,480\,x^{12}}{(1-x)^{19}} + \frac{19\,535\,040\,x^{13}}{(1-x)^{20}} \right) \left. \right) + 2 \left( \frac{12\,012\,x^{10}}{(1-x)^{14}} + \right. \\
& \frac{45\,864\,x^{11}}{(1-x)^{15}} + \frac{57\,330\,x^{12}}{(1-x)^{16}} + \frac{23\,520\,x^{13}}{(1-x)^{17}} + 3 \times \left( \frac{17\,160\,x^9}{(1-x)^{14}} + \frac{96\,096\,x^{10}}{(1-x)^{15}} + \frac{196\,560\,x^{11}}{(1-x)^{16}} + \right. \\
& \quad \left. \frac{174\,720\,x^{12}}{(1-x)^{17}} + \frac{57\,120\,x^{13}}{(1-x)^{18}} \right) + 2 \left( \frac{1716\,x^{10}}{(1-x)^{14}} + \frac{6552\,x^{11}}{(1-x)^{15}} + \frac{8190\,x^{12}}{(1-x)^{16}} + \frac{3360\,x^{13}}{(1-x)^{17}} \right) + \\
& x \left( \frac{68\,640\,x^9}{(1-x)^{14}} + \frac{384\,384\,x^{10}}{(1-x)^{15}} + \frac{786\,240\,x^{11}}{(1-x)^{16}} + \frac{698\,880\,x^{12}}{(1-x)^{17}} + \frac{228\,480\,x^{13}}{(1-x)^{18}} + x \left( \frac{154\,440\,x^8}{(1-x)^{14}} + \right. \right. \\
& \quad \left. \left. \frac{1\,201\,200\,x^9}{(1-x)^{15}} + \frac{3\,603\,600\,x^{10}}{(1-x)^{16}} + \frac{5\,241\,600\,x^{11}}{(1-x)^{17}} + \frac{3\,712\,800\,x^{12}}{(1-x)^{18}} + \frac{1\,028\,160\,x^{13}}{(1-x)^{19}} \right) \right) \left. \right) + \\
& x \left( \frac{446\,160\,x^9}{(1-x)^{14}} + \frac{2\,498\,496\,x^{10}}{(1-x)^{15}} + \frac{5\,110\,560\,x^{11}}{(1-x)^{16}} + \frac{4\,542\,720\,x^{12}}{(1-x)^{17}} + \frac{1\,485\,120\,x^{13}}{(1-x)^{18}} + \right. \\
& 11 \times \left( \frac{154\,440\,x^8}{(1-x)^{14}} + \frac{1\,201\,200\,x^9}{(1-x)^{15}} + \frac{3\,603\,600\,x^{10}}{(1-x)^{16}} + \frac{5\,241\,600\,x^{11}}{(1-x)^{17}} + \frac{3\,712\,800\,x^{12}}{(1-x)^{18}} + \right. \\
& \quad \left. \frac{1\,028\,160\,x^{13}}{(1-x)^{19}} \right) + 18 \left( \frac{17\,160\,x^9}{(1-x)^{14}} + \frac{96\,096\,x^{10}}{(1-x)^{15}} + \frac{196\,560\,x^{11}}{(1-x)^{16}} + \frac{174\,720\,x^{12}}{(1-x)^{17}} + \right. \\
& \quad \left. \frac{57\,120\,x^{13}}{(1-x)^{18}} \right) + 4 \times \left( \frac{772\,200\,x^8}{(1-x)^{14}} + \frac{6\,006\,000\,x^9}{(1-x)^{15}} + \frac{18\,018\,000\,x^{10}}{(1-x)^{16}} + \frac{26\,208\,000\,x^{11}}{(1-x)^{17}} + \right. \\
& \quad \left. \frac{18\,564\,000\,x^{12}}{(1-x)^{18}} + \frac{5\,140\,800\,x^{13}}{(1-x)^{19}} + x \left( \frac{1\,235\,520\,x^7}{(1-x)^{14}} + \frac{12\,972\,960\,x^8}{(1-x)^{15}} + \frac{54\,054\,000\,x^9}{(1-x)^{16}} + \right. \right.
\end{aligned}$$



$\ln[f^*] :=$ 

(470350815\*x\*D[x\*D[x\*D[x\*D[x\*D[x\*D[x\*D[x\*D[f(x),x],x],x],x],x],x],x])/2615348736000



(470 350 815 \* x \*

D[x\*D[x\*D[x\*D[x\*D[x\*D[x\*D[x\*D[f[x], x], x], x], x], x], x], x], x], x], x] ) / 2 615 348 736 000

 $\text{Out}[^*] :=$ 

$$\frac{1}{15850598400} \times 2850611x$$

$$\left( \frac{13x^{12}}{(1-x)^{14}} + \frac{\dots 8 \dots}{\dots 1 \dots^{15}} + x \left( \frac{19968x^{11}}{(1-x)^{14}} + \frac{\dots 8 \dots}{\dots 1 \dots^{15}} + x \left( \frac{217932x^{10}}{(1-x)^{14}} + \frac{832104 \dots 1 \dots}{\dots 1 \dots^{15}} + \frac{\dots 11 \dots}{\dots 1 \dots^{15}} + \right. \right.$$

$$2 \frac{\dots 1 \dots}{\dots 1 \dots^{15}} + x \left( \frac{2059200x^9}{(1-x)^{14}} + \frac{\dots 12 \dots}{\dots 1 \dots^{15}} + x \left( \frac{15289560x^8}{(1-x)^{14}} + \frac{\dots 11 \dots}{\dots 1 \dots^{15}} + x \left( \frac{79073280x^7}{(1-x)^{14}} + \frac{\dots 10 \dots}{\dots 1 \dots^{15}} + x \left( \frac{250810560x^6}{(1-x)^{14}} + \frac{\dots 9 \dots}{\dots 1 \dots^{15}} + x \left( \frac{415134720x^5}{(1-x)^{14}} + \right. \right. \right.$$

$$\left. \left. \left. \frac{\dots 8 \dots}{\dots 1 \dots^{15}} + x \left( \frac{259459200x^4}{\dots 1 \dots^{14}} + \frac{\dots 8 \dots}{\dots 1 \dots^{15}} + \frac{\dots 1 \dots}{\dots 1 \dots^{15}} \right) \right) \right) \right) \right) \right) \right) \right) \right)$$

large output

[show less](#)[show more](#)[show all](#)[set size limit...](#) $\ln[f^*] :=$ 

(-56440835\*x\*D[x\*D[x\*D[x\*D[x\*D[x\*D[x\*D[x\*D[f(x),x],x],x],x],x],x],x])/2615348736000



(-56 440 835 \* x \*

D[x\*D[x\*D[x\*D[x\*D[x\*D[x\*D[x\*D[f[x], x], x], x], x], x], x], x], x], x], x] ) / 2 615 348 736 000

 $\text{Out}[^*] :=$ 

$$-\frac{1}{47551795200} \times 1026197 \frac{\dots 1 \dots}{\dots 1 \dots^{15}}$$

$$\left( \frac{13x^{12}}{(1-x)^{14}} + \frac{14 \frac{\dots 1 \dots}{\dots 1 \dots^{15}}}{\dots 1 \dots^{15}} + \frac{\dots 7 \dots}{\dots 1 \dots^{15}} + x \frac{\dots 1 \dots}{\dots 1 \dots^{15}} + x \left( \frac{39936x^{11}}{(1-x)^{14}} + \frac{\dots 9 \dots}{\dots 1 \dots^{15}} + x \left( \frac{437580x^{10}}{(1-x)^{14}} + \frac{\dots 15 \dots}{\dots 1 \dots^{15}} + \right. \right.$$

$$x \left( \frac{4238520x^9}{(1-x)^{14}} + \frac{\dots 14 \dots}{\dots 1 \dots^{15}} + x \left( \frac{33822360x^8}{(1-x)^{14}} + \frac{\dots 13 \dots}{\dots 1 \dots^{15}} + x \left( \frac{201389760x^7}{(1-x)^{14}} + \frac{\dots 1 \dots}{\dots 1 \dots^{15}} + \right. \right.$$

$$\left. \left. \frac{\dots 10 \dots}{\dots 1 \dots^{15}} + 14 \frac{\dots 1 \dots}{\dots 1 \dots^{15}} + x \left( \frac{804323520x^6}{(1-x)^{14}} + \frac{\dots 11 \dots}{\dots 1 \dots^{15}} + x \left( \frac{1919998080x^5}{(1-x)^{14}} + \right. \right. \right.$$

$$\left. \left. \left. \frac{\dots 10 \dots}{\dots 1 \dots^{15}} + x \left( \frac{2335132800x^4}{\dots 1 \dots^{14}} + \frac{\dots 9 \dots}{\dots 1 \dots^{15}} + x \left( \frac{\dots 1 \dots}{\dots 1 \dots^{15}} \right) \right) \right) \right) \right) \right) \right) \right)$$

large output

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In[ ]:=



(5127697\*x\*D[x\*D[x\*D[x\*D[x\*D[x\*D[x\*D[x\*D[x\*D[x\*D[f(x),x],x],x],  
x],x],x],x],x],x],x])/2615348736000



(5 127 697 \* x \* D [ x \*

D [ x \* D [ x \* D [ x \* D [ x \* D [ x \* D [ x \* D [ x \* D [ f [ x ] , x ] , x ] , x ] , x ] , x ] , x ] , x ] , x ] , x ] , x ] , x ] ) / 2 6 1 5 3 4 8 7 3 6 0 0 0

Out[ ]:=

$$\frac{1}{2615348736000} \times 5127697 x$$

$$\left( \frac{13 x^{12}}{(1-x)^{14}} + \dots 10 \dots + x \left( \frac{79872 x^{11}}{(1-x)^{14}} + \dots 10 \dots + x \left( \frac{876876 x^{10}}{(1-x)^{14}} + \dots 17 \dots + x \left( \frac{8614320 x^9}{(1-x)^{14}} + \dots 16 \dots + x \left( \frac{71969040 x^8}{(1-x)^{14}} + \frac{\dots 1 \dots}{\dots 1 \dots^{15}} + \dots 13 \dots + 9 \dots 1 \dots + x \left( \frac{471968640 x^7}{(1-x)^{14}} + \dots 14 \dots + x \left( \frac{2214051840 x^6}{(1-x)^{14}} + \dots 13 \dots + x \left( \frac{6745939200 x^5}{(1-x)^{14}} + \dots 12 \dots + x \left( \frac{11935123200 \dots 1 \dots}{\dots 1 \dots^{14}} + \dots 11 \dots + x \dots 1 \dots \right) \right) \right) \right) \right) \right) \right) \right)$$

large output

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 $x * D [$ [illegible]

set size limit...

$$\ln[\bullet] :=$$
$$\begin{aligned}
& - \frac{1}{8047226880} \times 1051 \times \\
& \left( \frac{13 x^{12}}{(1-x)^{14}} + \dots 11 \dots + x \left( \frac{159744 x^{11}}{(1-x)^{14}} + \dots 11 \dots + x \left( \frac{1755468 x^{10}}{(1-x)^{14}} + \frac{6702696 \dots 1 \dots}{\dots 1 \dots^{15}} + \dots 17 \dots + \right. \right. \right. \\
& 2 \dots 1 \dots + x \left( \frac{17383080 x^9}{(1-x)^{14}} + \dots 18 \dots + x \left( \frac{149497920 x^8}{(1-x)^{14}} + \dots 17 \dots + x \right. \right. \\
& \left. \left( \frac{1047720960 x^7}{(1-x)^{14}} + \dots 16 \dots + x \left( \frac{5517832320 x^6}{(1-x)^{14}} + \dots 15 \dots + x \left( \frac{20030250240 x^5}{(1-x)^{14}} + \right. \right. \right. \\
& \left. \left. \left. \dots 14 \dots + x \left( \frac{45664819200 \dots 1 \dots}{\dots 1 \dots^{14}} + \dots 13 \dots + x \dots 1 \dots \right) \right) \right) \right)
\end{aligned}$$

set size limit...

In[ ]:=



$$(15755 \cdot x \cdot D[x \cdot D[\%18, x], x]) / 2615348736000$$


$$(15755 \cdot x \cdot D[x \cdot D[\%18, x], x]) / 2615348736000$$

Out[ ]:=

$$\frac{1}{523069747200} \times 3151 x$$

$$\left( \frac{13 x^{12}}{(1-x)^{14}} + \dots 12 \dots + x \left( \frac{319488 x^{11}}{(1-x)^{14}} + \dots 12 \dots + x \left( \frac{3512652 x^{10}}{(1-x)^{14}} + \dots 21 \dots + x \left( \frac{34937760 x^9}{(1-x)^{14}} + \right. \right. \right. \right.$$

$$\left. \frac{\dots 1 \dots}{\dots 1 \dots^{15}} + \dots 18 \dots + 5 \dots 1 \dots + x \left( \frac{305945640 x^8}{(1-x)^{14}} + \dots 19 \dots + x \left( \frac{2243704320 x^7}{(1-x)^{14}} + \right. \right. \right.$$

$$\left. \dots 18 \dots + x \left( \frac{12851879040 x^6}{(1-x)^{14}} + \dots 17 \dots + x \left( \frac{53137244160 x^5}{(1-x)^{14}} + \dots 16 \dots + \right. \right.$$

$$\left. \left. \left. x \left( \frac{145816070400 \dots 1 \dots}{\dots 1 \dots^{14}} + \dots 15 \dots + x \dots 1 \dots \right) \right) \right) \right)$$

large output

show less

show more

show all

set size limit...

In[ ]:=



$$(-450 \cdot x \cdot D[x \cdot D[x \cdot D[\%18, x], x], x]) / 2615348736000$$


$$(-450 \cdot x \cdot D[x \cdot D[x \cdot D[\%18, x], x], x]) / 2615348736000$$

Out[ ]:=

$$- \frac{1}{5811886080} x$$

$$\left( \frac{13 x^{12}}{(1-x)^{14}} + \dots 13 \dots + x \left( \frac{638976 x^{11}}{(1-x)^{14}} + \dots 13 \dots + x \left( \frac{7027020 x^{10}}{(1-x)^{14}} + \frac{26830440 \dots 1 \dots}{\dots 1 \dots^{15}} + \dots 21 \dots + \right. \right. \right.$$

$$2 \dots 1 \dots + x \left( \frac{70064280 x^9}{(1-x)^{14}} + \dots 22 \dots + x \left( \frac{620385480 x^8}{(1-x)^{14}} + \dots 21 \dots + x \left( \frac{4691269440 x^7}{(1-x)^{14}} + \right. \right. \right.$$

$$\left. \dots 20 \dots + x \left( \frac{28557809280 x^6}{(1-x)^{14}} + \dots 19 \dots + x \left( \frac{130248518400 x^5}{(1-x)^{14}} + \dots 18 \dots + \right. \right.$$

$$\left. \left. \left. x \left( \frac{411502291200 \dots 1 \dots}{\dots 1 \dots^{14}} + \dots 17 \dots + x \dots 1 \dots \right) \right) \right) \right)$$

large output

show less

show more

show all

set size limit...



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Out[•]=

[illegible]

set size limit...

$$\ln f^* := \%10 + \%11 + \%12 + \%13 + \%14 + \%15 + \%16 + \%17 + \%19 + \%20 + \%21 + \%22$$

*Out[•]=*

$$\begin{aligned} & \frac{1}{2\,615\,348\,736\,000} \left( -\frac{154\,078\,848\,000\,x^{13}}{(1-x)^{14}} + 486\,074\,908\,800\,x \left( \frac{13\,x^{12}}{(1-x)^{14}} + \frac{14\,x^{13}}{(1-x)^{15}} - \right. \right. \\ & \quad \left. \left. 707\,402\,381\,760\,x \left( \frac{13\,x^{12}}{(1-x)^{14}} + \frac{14\,x^{13}}{(1-x)^{15}} + x \left( \frac{156\,x^{11}}{(1-x)^{14}} + \frac{364\,x^{12}}{(1-x)^{15}} + \frac{210\,x^{13}}{(1-x)^{16}} \right) \right) \right) + \right. \\ & \quad \left. \frac{1}{2\,615\,348\,736\,000} \left( 631\,255\,103\,784\,x \left( \frac{13\,x^{12}}{(1-x)^{14}} + \dots 2 \dots + \right. \right. \right. \\ & \quad \left. \left. x \left( \frac{312\,x^{11}}{(1-x)^{14}} + \dots 1 \dots + \dots 1 \dots + x \left( \frac{1716\,x^{10}}{\dots 1 \dots^{14}} + \dots 2 \dots + \frac{\dots 1 \dots}{\dots 1 \dots^{17}} \right) \right) \right) - \dots 1 \dots \right) + \\ & \quad \frac{1\,368\,374\,183\,x \left( \dots 1 \dots \right)}{237\,758\,976\,000} + \dots 9 \dots + \frac{3151\,x \left( \dots 1 \dots \right)}{523\,069\,747\,200} - \frac{x \left( \left( \frac{13\,x^{12}}{\dots 1 \dots^{14}} + \dots 13 \dots + x \left( \dots 1 \dots \right) \right) \right)}{5\,811\,886\,080} + \\ & \quad \frac{1}{435\,891\,456\,000} x \\ & \quad \left( \frac{13\,x^{12}}{(1-x)^{14}} + \frac{14\,x^{13}}{\dots 1 \dots^{15}} + \dots 12 \dots + x \left( \dots 1 \dots \right) + x \left( \frac{1277\,952\,x^{11}}{(1-x)^{14}} + \dots 14 \dots + x \left( \frac{14\,055\,756\,x^{10}}{(1-x)^{14}} + \right. \right. \right. \\ & \quad \left. \left. \dots 25 \dots + x \left( \frac{140\,334\,480\,x^9}{(1-x)^{14}} + \dots 24 \dots + x \left( \frac{1\,250\,964\,000\,x^8}{(1-x)^{14}} + \dots 23 \dots + x \left( \frac{9\,654\,353\,280\,x^7}{(1-x)^{14}} + \right. \right. \right. \right. \\ & \quad \left. \left. \left. \dots 22 \dots + x \left( \frac{61\,396\,695\,360\,x^6}{\dots 1 \dots^{14}} + \dots 21 \dots + x \left( \dots 1 \dots \right) \right) \right) \right) \right) \right) \right) \end{aligned}$$

set size limit...

$$\ln[\bullet] :=$$

$$\text{Out}[^*]= -\frac{1}{39(-1+x)^{29}} x^{13} (3090 + x(165837 + x(3196632 + x(30131967 + x(158053587 + x(494273208 + x(958555598 + x(1177541573 + x(923581373 + 3x(153594806 + x(47984060 + x(9106889 + x(997974 + x(58009 + 13x(118 + x)))))))))))))$$

$\text{In}[*]:=$  **Expand** [  
 $x^{11} (1 + x) (1 + x (98 + x (3031 + x (41708 + x (295111 + x (1155650 + x (2598191 + x (3401660 +$   
 $x (2598191 + x (1155650 + x (295111 +$   
 $x (41708 + x (3031 + x (98 + x)))))))))))]$

$\text{Out}[*]=$   $x^{11} + 99 x^{12} + 3129 x^{13} + 44739 x^{14} + 336819 x^{15} + 1450761 x^{16} + 3753841 x^{17} + 5999851 x^{18} +$   
 $5999851 x^{19} + 3753841 x^{20} + 1450761 x^{21} + 336819 x^{22} + 44739 x^{23} + 3129 x^{24} + 99 x^{25} + x^{26}$

$\text{In}[*]:=$  **Series** [  
 $x^2 (x^{11} + 99 x^{12} + 3129 x^{13} + 44739 x^{14} + 336819 x^{15} + 1450761 x^{16} + 3753841 x^{17} + 5999851 x^{18} +$   
 $5999851 x^{19} + 3753841 x^{20} + 1450761 x^{21} + 336819 x^{22} +$   
 $44739 x^{23} + 3129 x^{24} + 99 x^{25} + x^{26}) / (1 - x)^{29}, \{x, 0, 20\}]$

$\text{Out}[*]=$   $x^{13} + 128 x^{14} + 6435 x^{15} + 183040 x^{16} + 3476330 x^{17} +$   
 $48542208 x^{18} + 530803988 x^{19} + 4751252480 x^{20} + O[x]^{21}$