



University of  
Zurich<sup>UZH</sup>

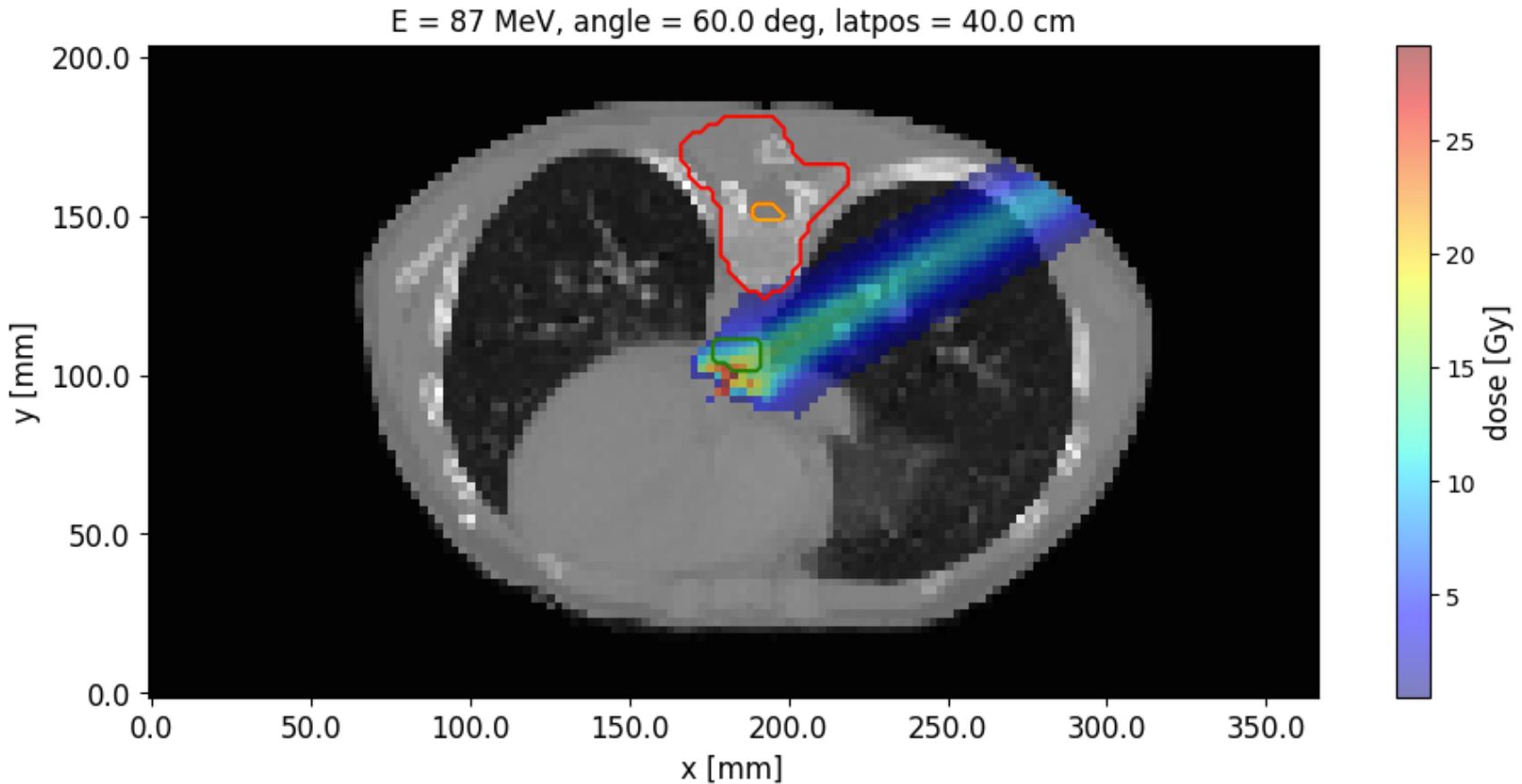
**USZ** Universitäts  
Spital Zürich

# Exercise class – Ex8

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## Exercise 6

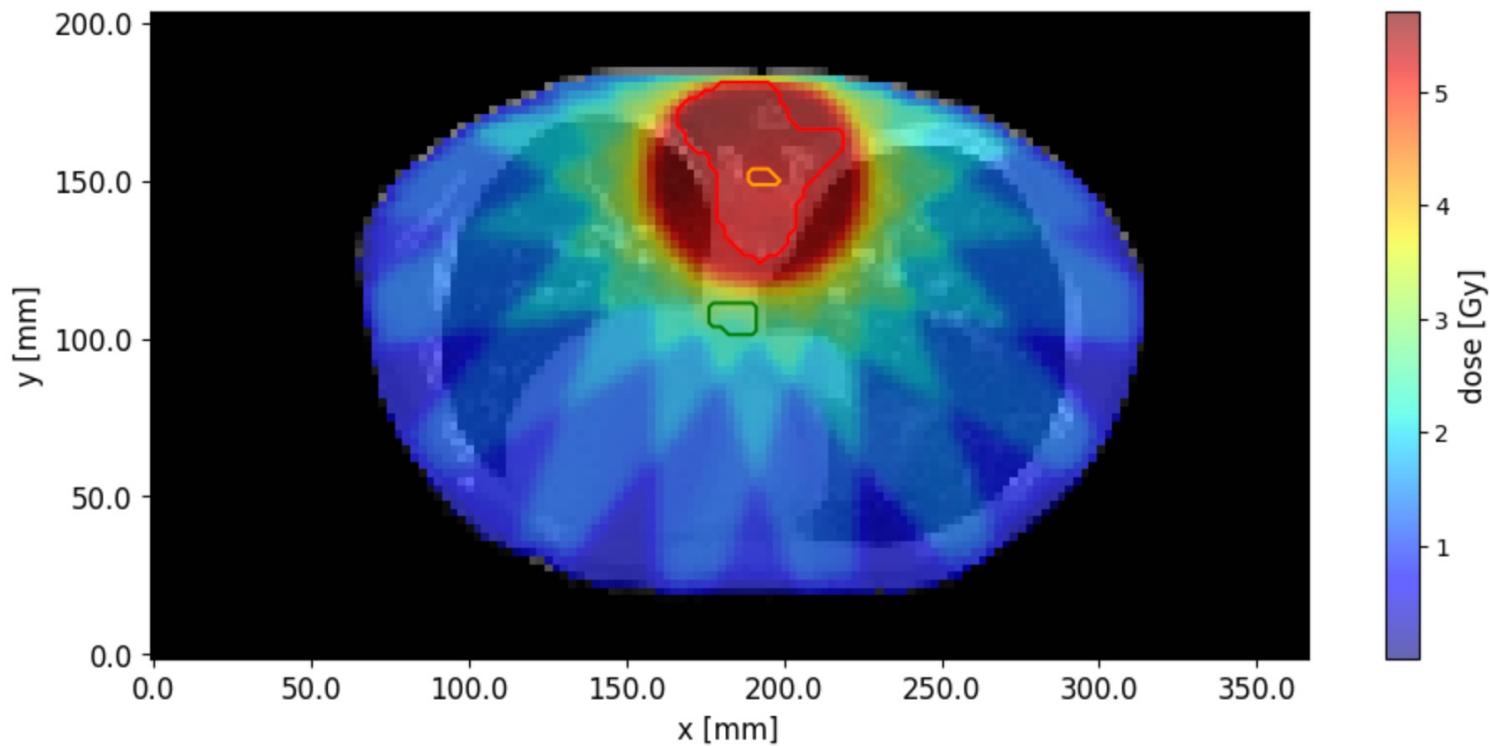
Mostly well solved!



## **Student solution for ex. 6**

## Exercise 7

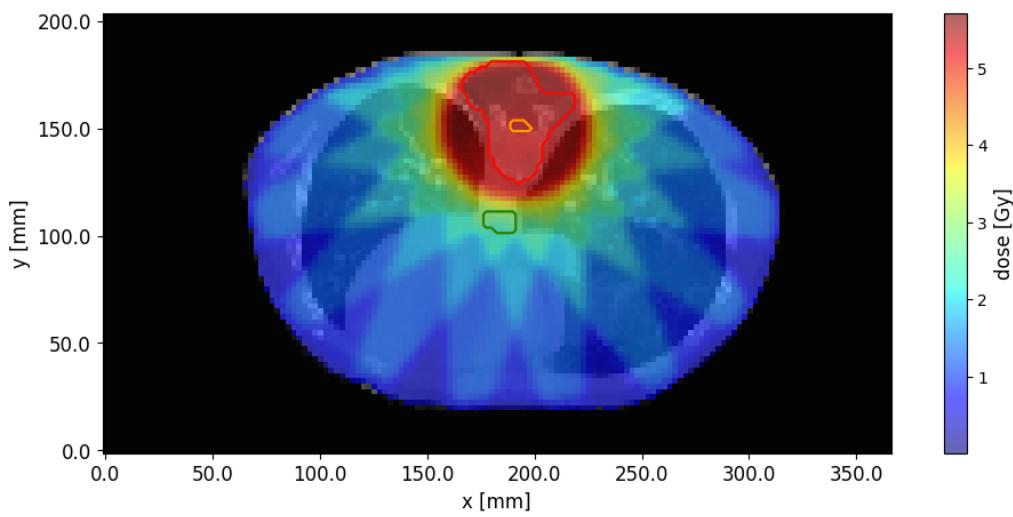
**Compute the photon dose-influence matrix!**



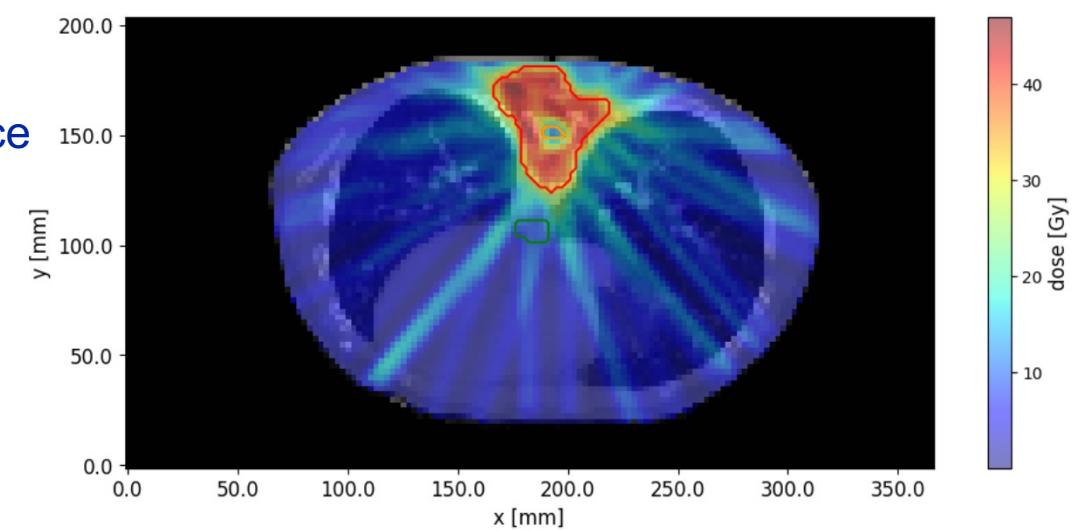
**Any questions regarding ex.7?**

## Exercise 8

Implement IMRT fluence map optimization algorithm!



Optimize fluence  
of beamlets  $F_j$



## Exercise 8

### How do we do that?

Minimize **quadratic objective function** with gradient descent:

$$f(d) = \sum_i w_i^o (d_i - D_i^{max})_+^2 + \sum_i w_i^u (D_i^{min} - d_i)_+^2$$

$D_i^{max}$  is the maximum dose to voxel  $i$ ,

$D_i^{min}$  is the minimum dose to voxel  $i$ ,

$w_i^o$  is the overdose penalty factor for voxel  $i$ ,

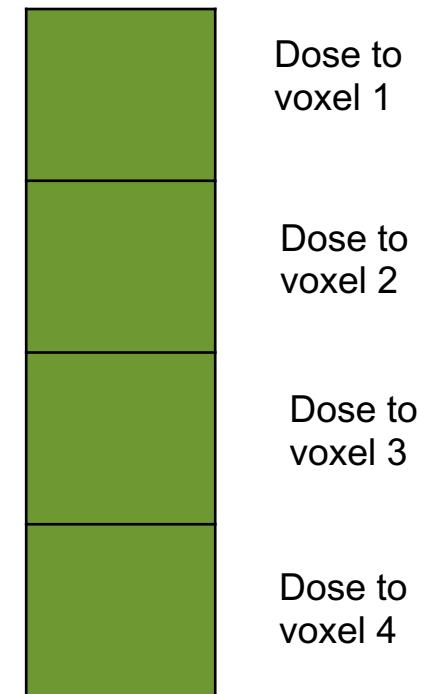
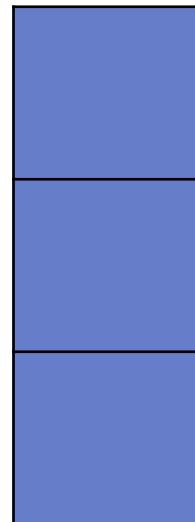
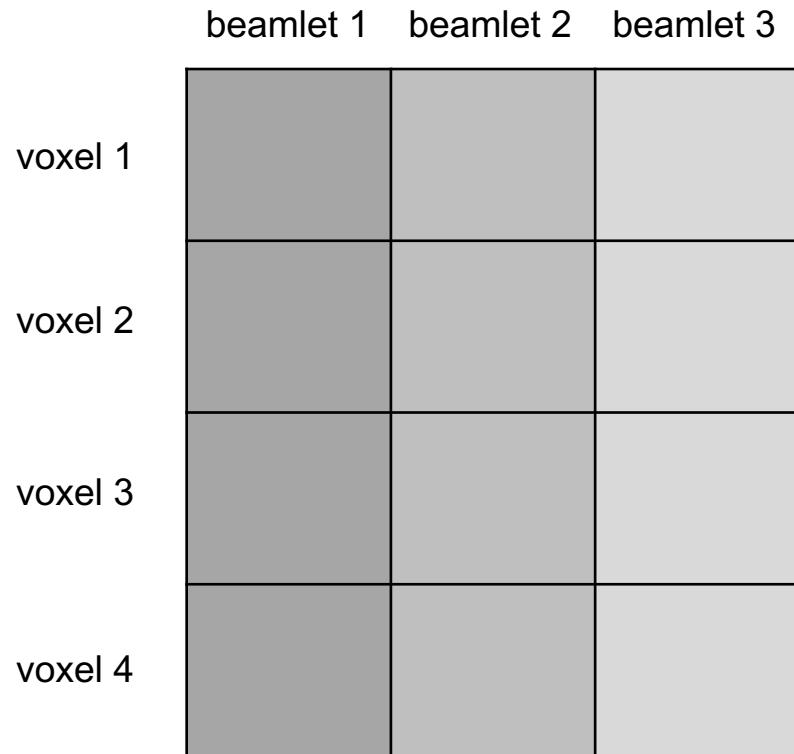
$w_i^u$  is the underdose penalty factor for voxel  $i$

## Exercise 8

**Note:** Dose  $d$  is a 1-d vector!

$$f(d) = \sum_i w_i^o (d_i - D_i^{max})_+^2 + \sum_i w_i^u (D_i^{min} - d_i)_+^2$$

$$d_i = \sum_j D_{ij} * F_j$$



$D_{ij}$  with 3 beamlets

Fluence vector  $F$

Total dose to every voxel  $d$

## Exercise 8

### Step 1

Define dictionary **TPopt** holding all parameters for each structure

```
TPopt['vois'][1] = {  
    'name': 'normal tissue',  
    'nVoxels': np.sum(voi == 1),  
    'maxdose': 50,  
    'overdosepenalty': 1,  
    'mindose': 0,  
    'underdosepenalty': 0,  
}
```

and summarize them to vectors the same size the dose vector

```
TPopt['maxdose']  
TPopt['mindose']  
TPopt['overdosepenalty']  
TPopt['underdosepenalty']
```



Reshape to 1d arrays!

## Exercise 7

### Step 2

Write a function `calculate_quadratic_objective(bixelweights)` that computes the **value of the objective function**, give a vector of beamlet intensities.

$$f(d) = \sum_i w_i^o (d_i - D_i^{max})_+^2 + \sum_i w_i^u (D_i^{min} - d_i)_+^2$$

### Step 3

Write a function `calculate_quadratic_objective_gradient(bixelweights)` that computes the **gradient of the objective function**, give a vector of beamlet intensities.

## Exercise 7

### Step 4

Write a function `optimize_gradient_descent(nIterations, stepsize)` which implements **gradient descent** to minimise the quadratic penalty function.

0. Initialize the beamlet intensities  $F_j = 0 \forall j$   
Choose a step size  $\alpha$ .

The algorithm consists of iterating the following steps until convergence:

1. Given the beamlet intensities  $F^k$  of the current iteration  $k$ , calculate the gradient

$$\frac{\partial f}{\partial F_j} \Big|_{F^k} \tag{2}$$

of the objective function with respect to the beam intensities.

2. Update the beamlet intensities according to

$$F_j^{k+1} = F_j^k - \alpha \frac{\partial f}{\partial F_j} \Big|_{F^k} \tag{3}$$

## Exercise 8 – What we expect!

