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Design and Analysis of Algorithms

Assignment - 1

Ques-1 What do you understand by Asymptotic notations. Define different asymptotic notation with examples.

Ans 1 Asymptotic notations are languages that allow us to analyze an algorithm running time by identifying its behaviour as the input size of the algorithm.

Types :-

1. Big O :- It is commonly used for worst case, and gives us upper bound for the growth rate of runtime of algorithm.
   Example :- Big O notation for linear search is $O(n)$

2. Big Omega :- It is notation used for least case complexity, it provides us with an asymptotic lower bound.
   Ex - Big omega of linear search is $\Omega(1)$

3. Theta :- It is used for tight bound on the growth rate of runtime of algo
   Ex - Theta of linear search is $O(n)$

4. Small Omega :- It is used to denote the upper bound (i.e. not asymptotic tight)
   $f(n) = o(g(n)) \Rightarrow f(n) < c(g(n)) \quad c > 0$

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5. Small Omega - To denote lower bound (that is not asymptotic)

Ques-2 Time complexity of - for (i=1 to n) { i = i*2 }

=) O(log n)

Ques-3 T(n) = { 3 T(n-1) if n>0 otherwise 1 }

Tn = 3T(n-1)
T(1) = ~~3T(1-1)~~ 1
T(2) = 3 T(1) = 3
T(3) = 3T(2) = 9
T(4) = 3T(3) = 27
!

T(n) = (n-1)^3
Time complexity → O(3^n)

Ques-4 T(n) = { 2T(n-1) - 1 if n>0 otherwise }

Ans

T(n) = 2T(n-1) - 1
T(n-1) = 2T(n-2) - 1
T(n) = 4T(n-2) - 2 - 1
T(n-2) = 2T(n-3) - 1
T(n) = 8T(n-3) - 4 - 2 - 1
T(n-3) = 2T(n-4) - 1
T(n) = 16T(n-4) - 8 - 4 - 2 - 1
T(n) = 2^k - ... - 2^3 - 2^2 - 2^1 - 2^0
TC = O(1)

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Ques-5

```
int i=1, S=1;
while(S<=n){
  i++;
  S=S+i;
  printf("#");
}
```

i	S	n
1	1	10
2	3	
3	6	
4	10	

$TC = O(\sqrt{n})$

Ques-6

```
void function(int n){
int i, count=0;
  for(i=1; i*i<=n; i++)
    count++;
}
```

Ans $TC = O(\sqrt{n})$

Ques-7

```
void function(int n){
  int i, count=0;
  for(i=n/2; i<=n; i++)
    for(j=1; j<=n; j=j*2)
      for(k=1; k<=n; k=k*2)
        count++;
}
```

Ans- $O(n \log^2 n)$

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Ques 9 void function (int n){
for(i = 0 to n)
for(j = 1; j <= n; j = j+1){
printf("*");
}

Ans → Total time complexity of problem is.
TC = O(n log n)

Ques-10 for the functions, n^k and a^n, what is the asymptotic relation between these functions?
Assume that $k >= 1$, and $a > 1$ are constants.
find out the value of c and n_0 for which relation holds.

Ans n^k is $\Theta(c^n)$ as for example
If we take $n = 2$ $K = 2$, $c = 2$
Then $2^2 \leq 2^2$ so c^n is upper limit of n^k