

Assignment

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Semester :- 3^r III

Subject :- Data structure and Algorithm.

Q1) Why Quick Sort is preferred for Arrays and Merge Sort for Linked List?

- Ans} • Quick sort in its general form is an in-place sort whereas merge sort requires $O(N)$ extra storage, N denoting the array size which may be quite expensive. Allocating and de-allocating the extra space used for merge sort increases the running time of the algorithm.
- Comparing average complexity we find that both type of sorts have $O(N \log N)$ average complexity but the constants differ. For arrays, merge sort is faster due to the use of extra $O(N)$ storage space.
 - Quick sort is also a cache friendly sorting algorithm as it has good locality of reference when used for array.
 - Quick sort is also tail recursive, therefore tail call optimization is done.

Now tell some of the reasons why Merge Sort is preferred for Linked List

- In case of linked list the case is different mainly mainly

due to difference in memory allocation of arrays and linked lists. Unlike arrays, linked list nodes may not be adjacent in memory.

- Unlike array, in linked list, we can insert items in the middle in $O(1)$ extra space and $O(1)$ time if we are given reference / pointer to the previous node. Therefore merge operation of merge sort can be implemented without extra space for linked lists.
- In arrays, we can do random access as elements are continuous in memory. Let us say we have an integer (4-byte) array A and let the address of $A[0]$ be X then the access $A[i]$, we can directly access the memory at $(x + i * 4)$. ($x + i * 4$) Unlike arrays, we can not do random access in linked list.
- Quick Sort requires a lot of this kind of access in linked list. To access i^{th} index, we have to travel each and every node from the head to i^{th} node as we don't have continuous block of memory.

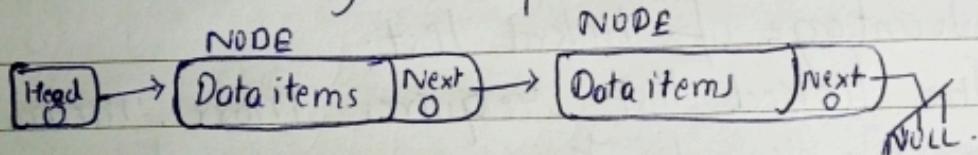
Q2) What is linked list? How will you represent a linked list in a graphical view?

Ans) A. Linked list is a linear data structure, in which the elements are not stored at contiguous memory locations. The elements in a linked list are linked using using using

Using pointers.. In simple words , a linked list consists of nodes . Likewise each node contains a data field and a reference (link) to the next node in the list.

Linked List Representation ~~as graph~~

- Linked list can be visualized as a chain of nodes, likewise, every node points to the next node.



As per the above illustration, following are the important points to be considered

- Linked list contains a link element called first
- Each link carries a data field(s) and a link field, called, @next
- Each link @ is linked with its next.link using its.next link.
- Last link carries a link as null, to mark the end of the list

Q3) How many pointers are necessary to implement a simple linked list? Mention some drawbacks of the linked list.

Ans, There are generally three type of pointers required to implement a simple linked list:

- A 'head' pointer, which is used for pointing to the start of the record in a list.
- A 'tail' pointer, which is used for pointing to the last node. The key factor in the last node is that its subsequent pointer points to nothing (NULL).
- A pointer in every node which is used for pointing to the next node element.

Disadvantage of linked list.

- 1) The linked list requires more memory to store the elements than an array, because each node of the linked list points a pointer, due to which it requires more memory.
- 2) It is very difficult to traverse the nodes in a linked list, in this, we cannot access randomly to any one node.
- 3) Reverse traversing in a linked list is a very difficult, because it requires more memory for the pointer.

Q4) How can we find the sum of two linked list. Using stack in Java?

~~import Java.util.Stack;~~
~~public class AddNumbersLinkedList~~
~~{~~
~~private class ListNode~~

- Ans:
- 1) Create stack ' s_1 '. by pushing all node. Values of the first. linked list . to a stack
 - 2) Create stack ' s_2 '. by pushing all node. Values of the second. linked list to a stack
 - 3) Create an empty. stack ' s_3 '. to store the result of addition
 - 4) Initialize sum and carry. to 0.
 - 5) Pop the top. element. from stack ' s_1 '. Let this top .element be 'Value1'
 - 6) Pop. the top .element from stack ' s_2 '. Let. this top .element be 'Value2'
 - 7) Make ' $Sum = (Value_1 + Value_2 + Value_3) \text{ carry} \% 10$ '. And push. this. 'Sum'. to Stack. ' s_3 '. And make ' $Carry = (Value_1 + Value_2 + Carry) / 10$ '.
 - 8) Repeat. steps 5-7 till. one of the stacks become. empty. if both stacks .are .of same size, .the both of the .stacks .should .become empty. at the same time.
 - 9) if. stack. ' s_1 '. has elements .left .in it then.
 - a) pop. the top element. .from. stack. ' s_1 '. Let this top. element be 'Value1'
 - b) Make ' $Sum = (Value_1 + Carry) \% 10$. and push. this. 'Sum'. to Stack. ' s_3 '. and make '(carry)'
 $= (Value_1 + Carry) / 10$
 - c) Repeat Steps. 9a .and 9b Until stack. ' s_1 ' is not .empty..
 - 10) Similarly., if stacks. ' s_2 ' .has elements. left left left left left

in. it then -

a. Pop. the top. element, from stack 's2'. Let this top. element. be 'value2'

b. Make 'Sum' = (value2 + carry) % 10. and push this 'Sum' to stack 's3'. And make, 'carry':
= .(Value2 + carry) / 10.

c. Repeat. steps. 10a and 10b. Until stack. 's2'
is not empty.

11). After all. the above. steps. are executed. if
carry. is greater. than 0, push it to the
resultant stack 's3'.

12) Create an empty. linked. list 'Result'. Now.
Pop. elements one by one. from the stack 's3',
and keep. appending. them to the 'Result'
linked. list. Until. stack. 's3'. is not empty. Return
R. the output. as 'Result'. linked. list.

Q5) Explain why stack is a recursive data structure

Ans) Recursive. functions. use something. Called "the

.. . Call stack". When. a program. calls a function,
that. function goes. on top. of the Call. stack.
This. similar. to. a stack. of books. You add
things. One at.. a time. Then, When you are
ready. to take. Something. off.. you always
take off. the top item.

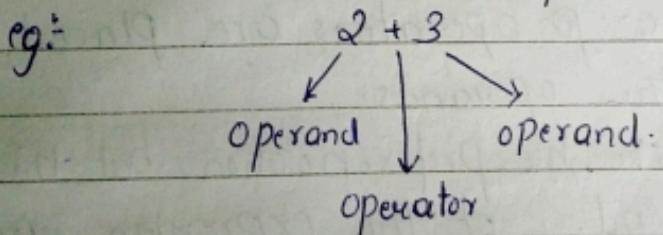
The. factorial. Call. stack. in action. With the
factorial. function.. factorial(5) is. written as

5!. And it is defined like this: $5! = 5 * 4 * 3 * 2 * 1$. Here is a recursive function to calculate the factorial of a number:

```
function fact(x) {
    if (x == 1) {
        return 1;
    } else {
        return x * fact(x-1);
    }
}
```

The top ~~no~~ topmost box in the stack tells you what call to fact you're currently on.

Q6} Explain what are infix, prefix and postfix. Of Expression
 Ans) infix :- infix notation is seen as the "normal" way to create mathematical formulae.



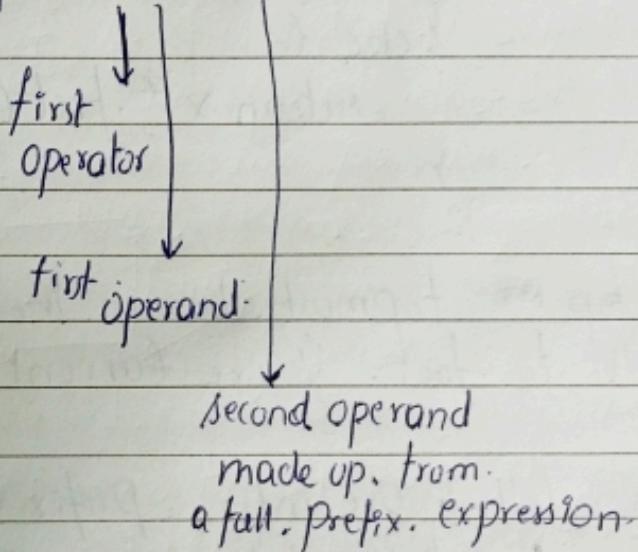
prefix:- Prefix notation puts the operator before all of the operands. This means that the precedence is always clear. We are going to compare the infix notation to this prefix notation.

prefix. Example of $2+3$

in prefix. equivalent like simply. take the operator then move from. left to right. reading off the operands. in left to. right order.

Prefix: $+23$

Some Prefix is $+2+34$



Postfix:- ~~It is~~ It is an expression in which the operators are placed before all the operands.

- This is just like the prefix notation, but the operand comes at the end. of the expression, and ~~from~~ similarly removes the need for brackets. Within any expression,
- So like take the bottom two operand first from left to right. Then append the operator at the end.
- Similarly when we have two expressive expressions, take have to expression expressions

We have to remember the operators to append to the end.

prefix :- 2 3 4 ++

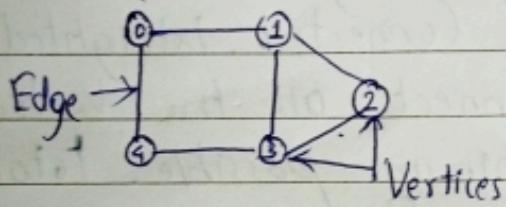
Q7) Explain minimum spanning tree.

- Ans)**
- A. Minimum Spanning Tree (MST) is a subset of edges of a connected weighted undirected graph that connects all the vertices together with the minimum possible total edge weight. To derive an MST, Prim's algorithm can be used. Hence, we will discuss Prim's algorithm in this chapter.
 - As we have discussed, one graph may have more than one spanning tree if there are n number of vertices, the spanning tree should have $n-1$ number of edges. In this context, if each edge of the graph in this context, if each of the graph is associated with a weight, and there exists more than one spanning tree, we need to find the minimum spanning tree of the graph.
 - Moreover, if there exist any duplicate weighted edges, the graph may have multiple minimum spanning trees.
 - In the above graph, we have shown a spanning tree though it's not the minimum spanning tree.

Q8) Mention the applications of graph and map.

Ans) i) Application of Graph

- A graph is a non-linear data structure, which consists of vertices (or nodes) connected by edges (or arcs). All these edges may be directed or Undirected.

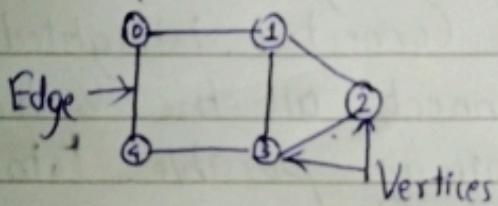


- In Computer Science graphs are used to represent the flow of computation.
- Google maps uses graphs for building transportation systems. Where ~~inter~~ intersection of two (or more) roads are considered to be a vertex and the road connecting two vertices is considered to be an edge.
- In World Wide Web, Web pages are considered to be the vertices. There is an edge from a page U to other page V , if there is a link of page V if there is a link of page V on page U .
- In similar manner it is used in Facebook.
- In operating system, we come across the Resource Allocation Graph. Where each process and resources are considered to be vertices. Edges are drawn from the resources to the allocated processes, or from requesting processes.

Q8) Mention the applications of graph and ~~map~~. heap.

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to the requested resource.

ii) Application of Heap Data Structure -

- Heap Data Structure is generally taught with Heapsort. Heapsort algorithm has limited uses because Quicksort is better in practice. Nevertheless, the Heap data structure itself is enormously used other than Heapsort Priority Queues:- Priority Queues can be efficiently implemented using Binary Heap because it supports insert(), delete() and extractmax(), decreasekey() operations in $O(\log n)$ time.

Order Statistics :- The Heap data structure can be used to efficiently find the kth smallest (or largest) element in an array. ~~Average method~~.

Binomial Heap and Fibonacci Heap are variation of Binary Heap.