

Sa (x) = sin(x) / x
sinc function

Table of Fourier Transform Pairs

Function, f(t)	Fourier Transform, F(ω)
<i>Definition of Inverse Fourier Transform</i>	<i>Definition of Fourier Transform</i>
$f(t) = \frac{1}{2\pi} \int_{-\infty}^{\infty} F(\omega) e^{j\omega t} d\omega$	$F(\omega) = \int_{-\infty}^{\infty} f(t) e^{-j\omega t} dt$
$f(t - t_0)$	$F(\omega) e^{-j\omega t_0}$
$f(t) e^{j\omega_0 t}$	$F(\omega - \omega_0)$
$f(\alpha t)$	$\frac{1}{ \alpha } F\left(\frac{\omega}{\alpha}\right)$
$F(t)$	$2\pi f(-\omega)$
$\frac{d^n f(t)}{dt^n}$	$(j\omega)^n F(\omega)$
$(-jt)^n f(t)$	$\frac{d^n F(\omega)}{d\omega^n}$
$\int_{-\infty}^t f(\tau) d\tau$	$\frac{F(\omega)}{j\omega} + \pi F(0) \delta(\omega)$
$\delta(t)$	1
$e^{j\omega_0 t}$	$2\pi \delta(\omega - \omega_0)$
$\text{sgn}(t)$	$\frac{2}{j\omega}$

$j \frac{1}{\pi t}$	$\text{sgn}(\omega)$
$u(t)$	$\pi \delta(\omega) + \frac{1}{j\omega}$
$\sum_{n=-\infty}^{\infty} F_n e^{jn\omega_0 t}$	$2\pi \sum_{n=-\infty}^{\infty} F_n \delta(\omega - n\omega_0)$
$\text{rect}\left(\frac{t}{\tau}\right)$	$\tau \text{Sa}\left(\frac{\omega\tau}{2}\right)$
$\frac{B}{2\pi} \text{Sa}\left(\frac{Bt}{2}\right)$ Sa (x) = sin(x) / x sinc function	$\text{rect}\left(\frac{\omega}{B}\right)$
$\text{tri}(t)$ tri(t) = (1- t)rect(t/2) triangle function = rect(t)*rect(t)	$\text{Sa}^2\left(\frac{\omega}{2}\right)$ Sa (x) = sin(x) / x sinc function
$A \cos\left(\frac{\pi t}{2\tau}\right) \text{rect}\left(\frac{t}{2\tau}\right)$	$\frac{A\pi}{\tau} \frac{\cos(\omega\tau)}{(\pi/2\tau)^2 - \omega^2}$
$\cos(\omega_0 t)$	$\pi [\delta(\omega - \omega_0) + \delta(\omega + \omega_0)]$
$\sin(\omega_0 t)$	$\frac{\pi}{j} [\delta(\omega - \omega_0) - \delta(\omega + \omega_0)]$
$u(t) \cos(\omega_0 t)$	$\frac{\pi}{2} [\delta(\omega - \omega_0) + \delta(\omega + \omega_0)] + \frac{j\omega}{\omega_0^2 - \omega^2}$
$u(t) \sin(\omega_0 t)$	$\frac{\pi}{2j} [\delta(\omega - \omega_0) - \delta(\omega + \omega_0)] + \frac{\omega^2}{\omega_0^2 - \omega^2}$
$u(t) e^{-\alpha t} \cos(\omega_0 t)$	$\frac{(\alpha + j\omega)}{\omega_0^2 + (\alpha + j\omega)^2}$

$u(t)e^{-\alpha t} \sin(\omega_0 t)$	$\frac{\omega_0}{\omega_0^2 + (\alpha + j\omega)^2}$
$e^{-\alpha t }$	$\frac{2\alpha}{\alpha^2 + \omega^2}$
$e^{-t^2/(2\sigma^2)}$	$\sigma\sqrt{2\pi} e^{-\sigma^2\omega^2/2}$
$u(t)e^{-\alpha t}$	$\frac{1}{\alpha + j\omega}$
$u(t)te^{-\alpha t}$	$\frac{1}{(\alpha + j\omega)^2}$

➤ **Trigonometric Fourier Series**

$$f(t) = a_0 + \sum_{n=1}^{\infty} (a_n \cos(\omega_0 nt) + b_n \sin(\omega_0 nt))$$

where

$$a_0 = \frac{1}{T} \int_0^T f(t) dt \quad , \quad a_n = \frac{2}{T} \int_0^T f(t) \cos(\omega_0 nt) dt \quad , \text{ and}$$

$$b_n = \frac{2}{T} \int_0^T f(t) \sin(\omega_0 nt) dt$$

➤ **Complex Exponential Fourier Series**

$$f(t) = \sum_{n=-\infty}^{\infty} F_n e^{j\omega_0 nt} \quad , \text{ where } \quad F_n = \frac{1}{T} \int_0^T f(t) e^{-j\omega_0 nt} dt$$