

### Useful Combinations of Constants

$$\hbar = h/2\pi = 1.0546 \times 10^{-34} \text{ J} \cdot \text{s} = 6.5821 \times 10^{-16} \text{ eV} \cdot \text{s}$$

$$\hbar c = 1.9864 \times 10^{-25} \text{ J} \cdot \text{m} = 1239.8 \text{ eV} \cdot \text{nm}$$

$$\hbar c = 3.1615 \times 10^{-26} \text{ J} \cdot \text{m} = 197.33 \text{ eV} \cdot \text{nm}$$

$$\frac{1}{4\pi\epsilon_0} = 8.9876 \times 10^9 \text{ N} \cdot \text{m}^2 \cdot \text{C}^{-2}$$

$$\text{Compton wavelength } \lambda_c = \frac{h}{m_e c} = 2.4263 \times 10^{-12} \text{ m}$$

$$\frac{e^2}{4\pi\epsilon_0} = 2.3071 \times 10^{-28} \text{ J} \cdot \text{m} = 1.4400 \times 10^{-9} \text{ eV} \cdot \text{m}$$

$$\text{Fine structure constant } \alpha = \frac{e^2}{4\pi\epsilon_0 \hbar c} = 0.0072974 \approx \frac{1}{137}$$

$$\text{Bohr magneton } \mu_B = \frac{e\hbar}{2m_e} = 9.2740 \times 10^{-24} \text{ J/T} = 5.7884 \times 10^{-5} \text{ eV/T}$$

$$\text{Nuclear magneton } \mu_N = \frac{e\hbar}{2m_p} = 5.0508 \times 10^{-27} \text{ J/T} \\ = 3.1525 \times 10^{-8} \text{ eV/T}$$

$$\text{Bohr radius } a_0 = \frac{4\pi\epsilon_0 \hbar^2}{m_e e^2} = 5.2918 \times 10^{-11} \text{ m}$$

$$\text{Hydrogen ground state } E_0 = \frac{e^2}{8\pi\epsilon_0 a_0} = 13.606 \text{ eV} = 2.1799 \times 10^{-18} \text{ J}$$

$$\text{Rydberg constant } R_\infty = \frac{\alpha^2 m_e c}{2\hbar} = 1.09737 \times 10^7 \text{ m}^{-1}$$

$$\text{Hydrogen Rydberg } R_H = \frac{\mu}{m_e} R_\infty = 1.09678 \times 10^7 \text{ m}^{-1}$$

$$\text{Gas constant } R = N_A k = 8.3145 \text{ J} \cdot \text{mol}^{-1} \cdot \text{K}^{-1}$$

$$\text{Magnetic flux quantum } \Phi_0 = \frac{h}{2e} = 2.0678 \times 10^{-15} \text{ T} \cdot \text{m}^2$$

$$\text{Classical electron radius } r_e = \alpha^2 a_0 = 2.8179 \times 10^{-15} \text{ m}$$

$$kT = 2.5249 \times 10^{-2} \text{ eV} \approx \frac{1}{40} \text{ eV at } T = 293 \text{ K}$$

*Note:* The latest values of the fundamental constants can be found at the National Institute of Standards and Technology website at <http://physics.nist.gov/cuu/Constants>

**Table 3.3** Work Functions

Element	$\phi$ (eV)	Element	$\phi$ (eV)	Element	$\phi$ (eV)
Ag	4.64	K	2.29	Pd	5.22
Al	4.20	Li	2.93	Pt	5.64
C	5.0	Na	2.36	W	4.63
Cs	1.95	Nd	3.2	Zr	4.05
Cu	4.48	Ni	5.22		
Fe	4.67	Pb	4.25		

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Fundamental Constants		
Quantity	Symbol	Value(s)
Elementary charge	$e$	$1.6022 \times 10^{-19} \text{ C}$
Speed of light in vacuum	$c$	$2.9979 \times 10^8 \text{ m/s}$
Permeability of vacuum (magnetic constant)	$\mu_0$	$4\pi \times 10^{-7} \text{ N} \cdot \text{A}^{-2}$
Permittivity of vacuum (electric constant)	$\epsilon_0$	$8.8542 \times 10^{-12} \text{ F} \cdot \text{m}^{-1}$
Gravitation constant	$G$	$6.6738 \times 10^{-11} \text{ N} \cdot \text{m}^2 \cdot \text{kg}^{-2}$
Planck constant	$h$	$6.6261 \times 10^{-34} \text{ J} \cdot \text{s}$ $4.1357 \times 10^{-15} \text{ eV} \cdot \text{s}$
Avogadro constant	$N_A$	$6.0221 \times 10^{23} \text{ mol}^{-1}$
Boltzmann constant	$k$	$1.3807 \times 10^{-23} \text{ J} \cdot \text{K}^{-1}$
Stefan-Boltzmann constant	$\sigma$	$5.6704 \times 10^{-8} \text{ W} \cdot \text{m}^{-2} \cdot \text{K}^{-4}$
Atomic mass unit	$u$	$1.66053886 \times 10^{-27} \text{ kg}$ $931.494061 \text{ MeV}/c^2$

Conversion Factors	
$1 \text{ y} = 3.156 \times 10^7 \text{ s}$	$1 \text{ T} = 10^4 \text{ G}$
$1 \text{ lightyear} = 9.461 \times 10^{15} \text{ m}$	$1 \text{ Ci} = 3.7 \times 10^{10} \text{ Bq}$
$1 \text{ cal} = 4.186 \text{ J}$	$1 \text{ barn} = 10^{-28} \text{ m}^2$
$1 \text{ MeV}/c = 5.344 \times 10^{-22} \text{ kg} \cdot \text{m/s}$	$1 \text{ u} = 1.66054 \times 10^{-27} \text{ kg}$
$1 \text{ eV} = 1.6022 \times 10^{-19} \text{ J}$	

Particle	Mass in units of		
	kg	MeV/c <sup>2</sup>	u
Electron	$9.1094 \times 10^{-31}$	0.51100	$5.4858 \times 10^{-4}$
Muon	$1.8835 \times 10^{-28}$	105.66	0.11343
Proton	$1.6726 \times 10^{-27}$	938.27	1.00728
Neutron	$1.6749 \times 10^{-27}$	939.57	1.00866
Deuteron	$3.3436 \times 10^{-27}$	1875.61	2.01355
$\alpha$ particle	$6.6447 \times 10^{-27}$	3727.38	4.00151

**Table 3.4** Results of Compton Scattering

Energy or Momentum	Initial System	Final System
Photon energy	$hf$	$hf'$
Photon momentum in $x$ direction ( $p_x$ )	$\frac{h}{\lambda}$	$\frac{h}{\lambda'} \cos \theta$
Photon momentum in $y$ direction ( $p_y$ )	0	$\frac{h}{\lambda'} \sin \theta$
Electron energy	$mc^2$	$E_e = mc^2 + \text{K.E.}$
Electron momentum in $x$ direction ( $p_x$ )	0	$p_e \cos \phi$
Electron momentum in $y$ direction ( $p_y$ )	0	$-p_e \sin \phi$

**Table 3.2** Hydrogen Series of Spectral Lines

Discoverer (year)	Wavelength	$n$	$k$
Lyman (1916)	Ultraviolet	1	$>1$
Balmer (1885)	Visible, ultraviolet	2	$>2$
Paschen (1908)	Infrared	3	$>3$
Brackett (1922)	Infrared	4	$>4$
Pfund (1924)	Infrared	5	$>5$