## Assignment-1 Chapter-2 Complex Number

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Section-B JEE MAIN / AIE	EE
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14) If  $z^2+z+1=0$ , where z is an imaginary number, then the value of

$$\left(z + \frac{1}{z}\right)^2 + \left(z^2 + \frac{1}{z^2}\right)^2 + \left(z^3 + \frac{1}{z^3}\right)^2 + \dots + \left(z^6 + \frac{1}{z^6}\right)^2 = 0$$
 If  $\omega \neq 1$  is the cube root of unity, and  $(1 + \omega)^7 = A + B\omega$ . Then  $(A, B)$  equals: [2011]

is

[2006]

- a) 18 b) 54
- c) 6 d) 12
- 15) If  $|z+4| \le 3$ , then the maximum value of |z+1|[2007]
  - a) 6
- b) 0
- c) 4
- d) 10
- 16) The conjugate of a complex is  $\frac{1}{i-1}$  then that complex number is
- a)  $\frac{-1}{i-1}$  b)  $\frac{1}{i+1}$  c)  $\frac{-1}{i+1}$
- d)  $\frac{1}{i-1}$
- 17) Let R be the real line. Consider the following subsets of the real plane:

$$S = \{(x, y) : y = x + 1 \text{ and } 0 < x < 2\}$$
 (2)

$$T = \{(x, y) : x - yisaninteger\}, \qquad (3)$$

Which one of the following is true?

- a) Neither S nor T is an equivalence relation on R
- b) Both S and T are equivalence relation on R
- 18) The number of complex numbers z such that |z - 1| = |z + 1| = |z - i| equals [2010]
- b) 2
- $c) \infty$
- d) 0
- 19) Let  $\alpha, \beta$  be real and z be a complex number. If  $z^2 + z\alpha + \beta = 0$  has two distinct roots on the line Rez = 1, then it is necessary that: [2011]

- a)  $\beta \in (-1, 0)$
- b)  $|\beta| = 1$
- c)  $\beta \in (1, \infty)$
- d)  $\beta \in (0, 1)$

a) (1, 1)

- b) (1,0)
- c) (-1,1)
- d) (0, 1)
- 21) If  $z \neq 1$  and  $\frac{z^2}{z-1}$  is real, then the point represented by the complex number z lies:
  - a) either on the real axis or on a circle not passing through the origin
  - b) on a circle with centre at the origin
  - c) either on the real axis or on a circle not passing through the origin
  - d) on imaginary axis
- 22) If z is a complex number of unit modulus and arguement  $\theta$ , then the  $arg\left(\frac{1+z}{1+\overline{z}}\right)$  equals: [JEE M 20131

  - a)  $-\theta$  b)  $\frac{\pi}{2} \theta$  c)  $\theta$  d)  $\pi \theta$
- 23) If z is a complex number such that  $|z| \ge 2$ , then the minimum value of  $|z + \frac{1}{2}|$ : [JEE M 2014]

  - a) is strictly greater than  $\frac{5}{2}$ b) is strictly greater than  $\frac{3}{2}$  but less than  $\frac{5}{2}$
  - c) is equal to  $\frac{5}{2}$
- b) Both S and T are equivalence relation on R

  d) lies in the interval (1, 2)

  c) S is an equivalence relation on R but T is notT

  is an equivalence relation on R. but S is not

  24) A complex number z is said to be unimodular if |z| = 1. Suppose  $z_1 and z_2$  are complex numbers such that  $\frac{z_1-2z_2}{2-z_1\overline{z_2}}$  is unimodular and  $z_2$  is not unimodular. Then the point  $z_1$  lies on a: [JEE M 2016]
  - a) circle of radius 2
  - b) circle of radius  $\sqrt{2}$
  - c) straight line parallel to x-axis

- d) straight line parallel to y-axis
- 25) A value of  $\theta$  for which  $\frac{2+3i\sin(\theta)}{1-2i\sin(\theta)}$  is purely imaginary is: [JEE M2016]
  - a)  $\sin^{-1}\left(\frac{\sqrt{3}}{4}\right)$
- b)  $\sin^{-1}\left(\frac{1}{\sqrt{3}}\right)$
- c)  $\frac{\pi}{3}$

- d)  $\frac{\pi}{6}$
- 26) Let  $\{A = \theta \in \left(\frac{\pi}{2}, \pi\right) : \frac{3+2i\sin(\theta)}{1-2i\sin(\theta)} \text{ is purely imaginary. Then the sum of element in A is:}$ [JEE M 2019-9 Jan (M)]
  - a)  $\frac{5\pi}{6}$
- b) π
- c)  $\frac{3\pi}{4}$  d)  $\frac{2\pi}{3}$
- 27) let  $\alpha$  and  $\beta$  be two roots of the equation  $x^2$  + 2x + 2 = 0, then  $\alpha^{15} + \beta^{15}$  is equal to: [JEE M 2019-Jan (M)]
  - a) -256
- b) 512
- c) -512
- d) 256
- 28) All the points in the set (  $S = \left\{\frac{\alpha i}{\alpha + i} : \alpha \in R\right\}$  [JEE M 2019-9 April (M)]
  - a) straight line whose slope is 1
  - b) circle whose radius is 1
  - c) circle whose radius is  $\sqrt{2}$
  - d) straight line whose slope is -1